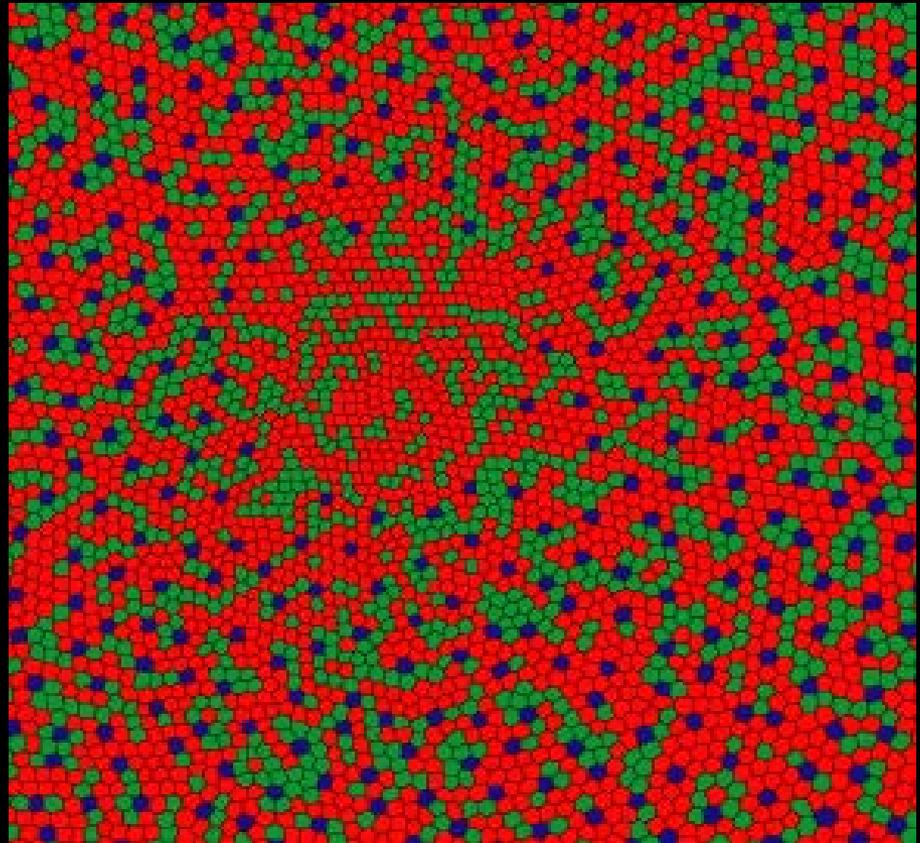


Physiological optics and the photoreceptor mosaic

Andrew Stockman



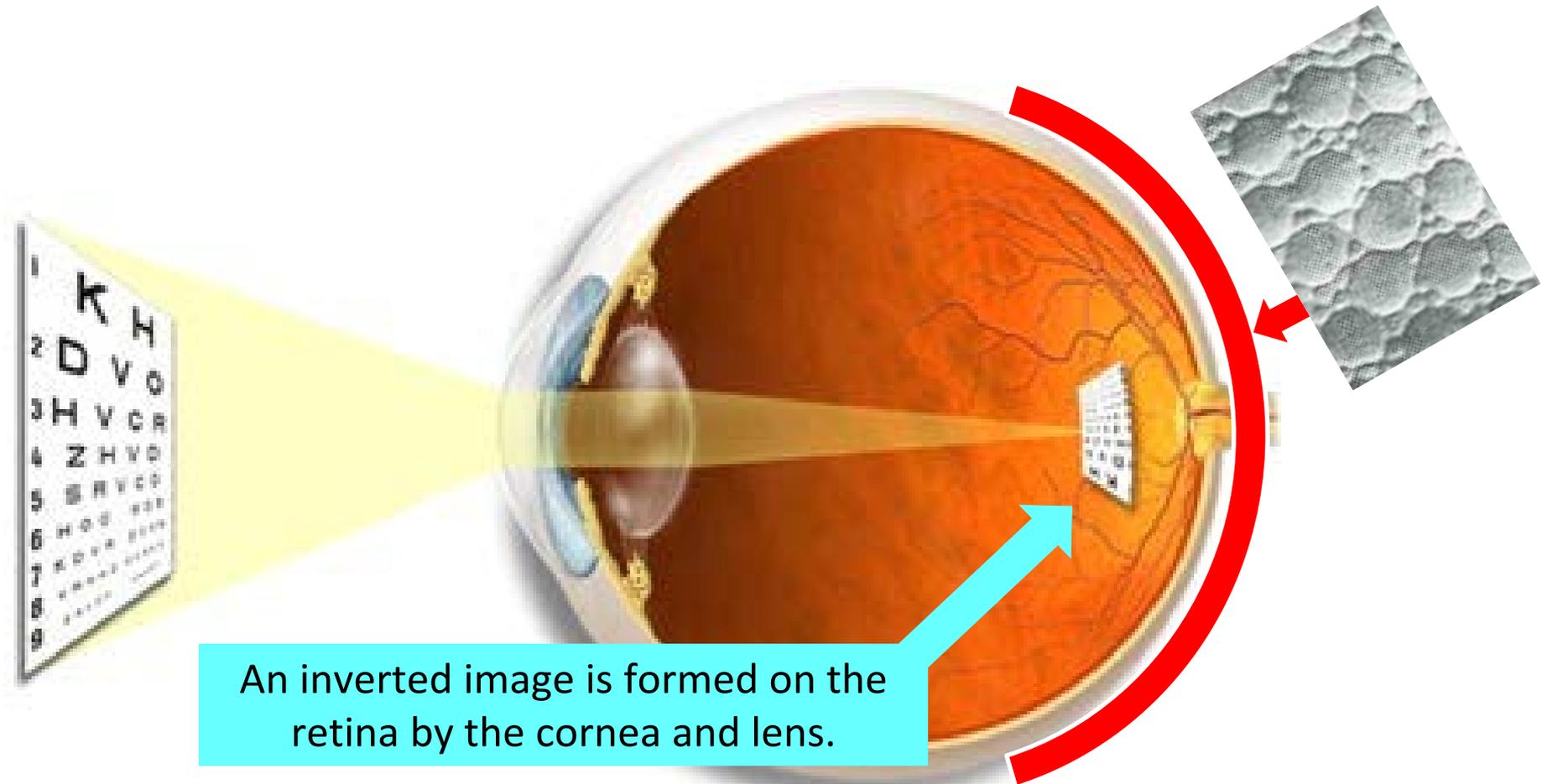
NEUR 3045
Visual Neuroscience

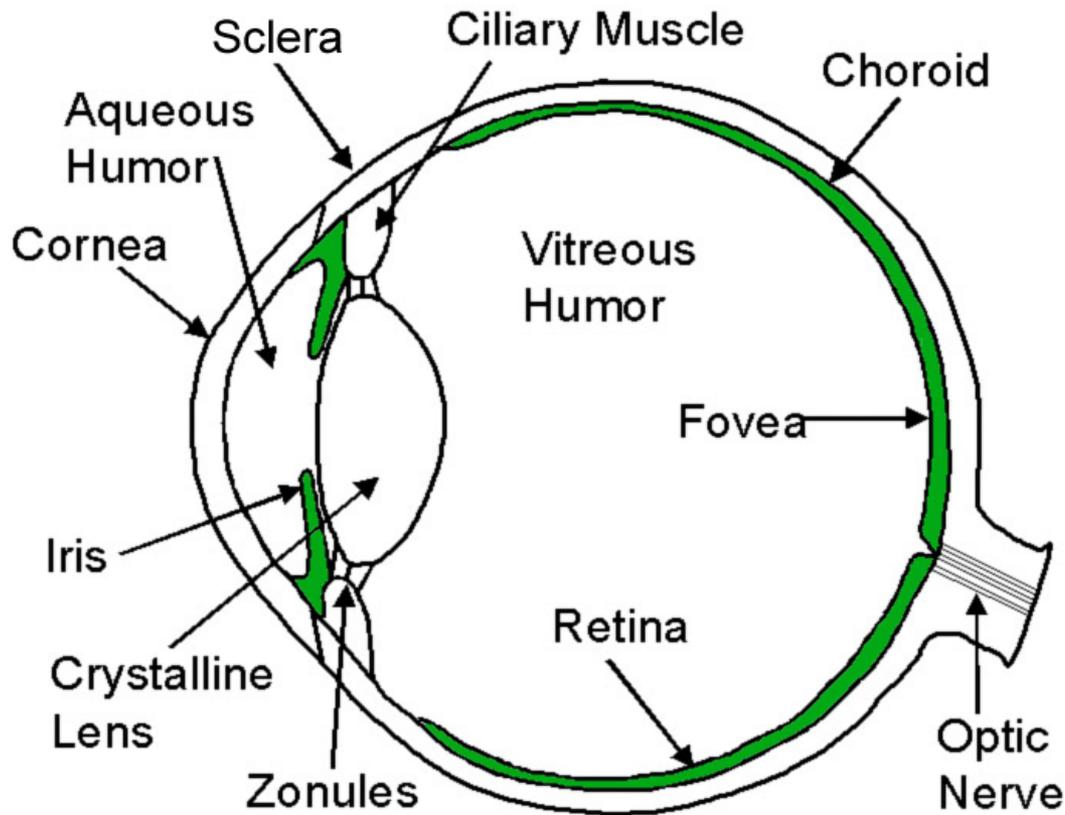


Outline

- ▶ The eye
- ▶ Visual optics
- ▶ Image quality
- ▶ Measuring image quality
- ▶ What limits visual performance?
- ▶ Refractive errors
- ▶ Sampling
- ▶ Why visual acuity should be limited by the optics and sampling
- ▶ Adaptive optics
- ▶ Chromatic aberrations

The retina is carpeted with light-sensitive rods and cones





Cornea – Clear membrane on the front of the eye.

Crystalline Lens – Lens that can change shape to alter focus.

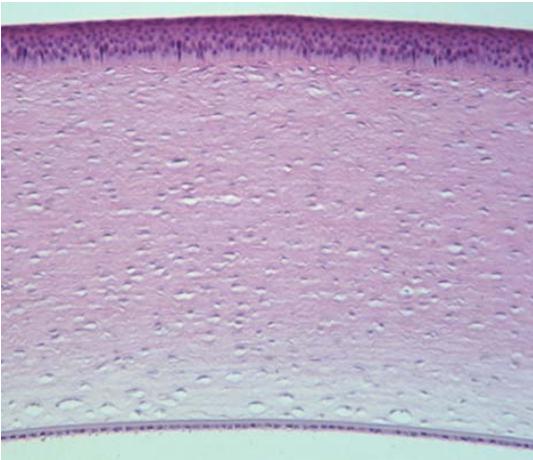
Retina – Photosensitive inner lining of eye

Fovea – central region of retina with sharpest vision.

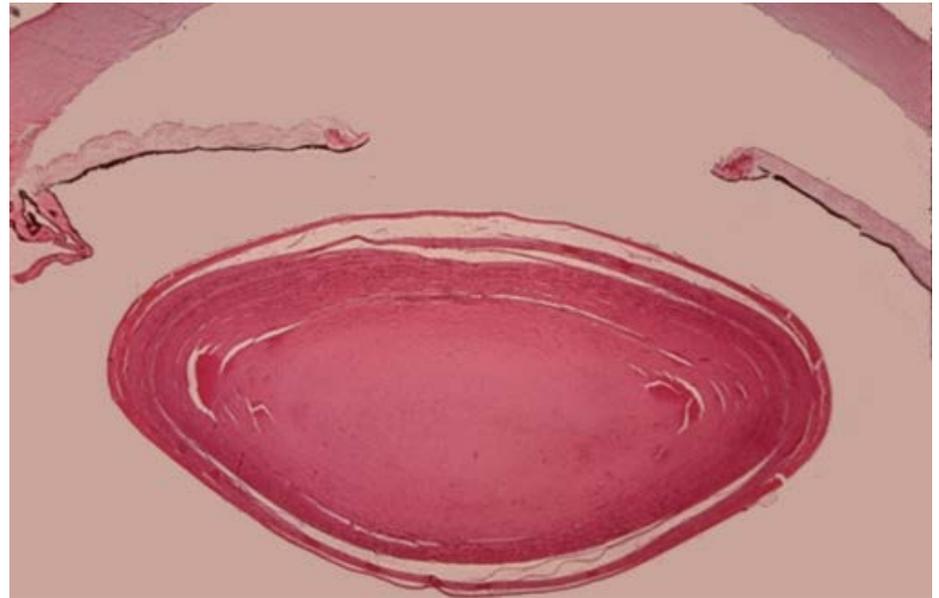
Optic Nerve – bundle of nerve fibers that carry information to the brain.

Visual optics

Cornea



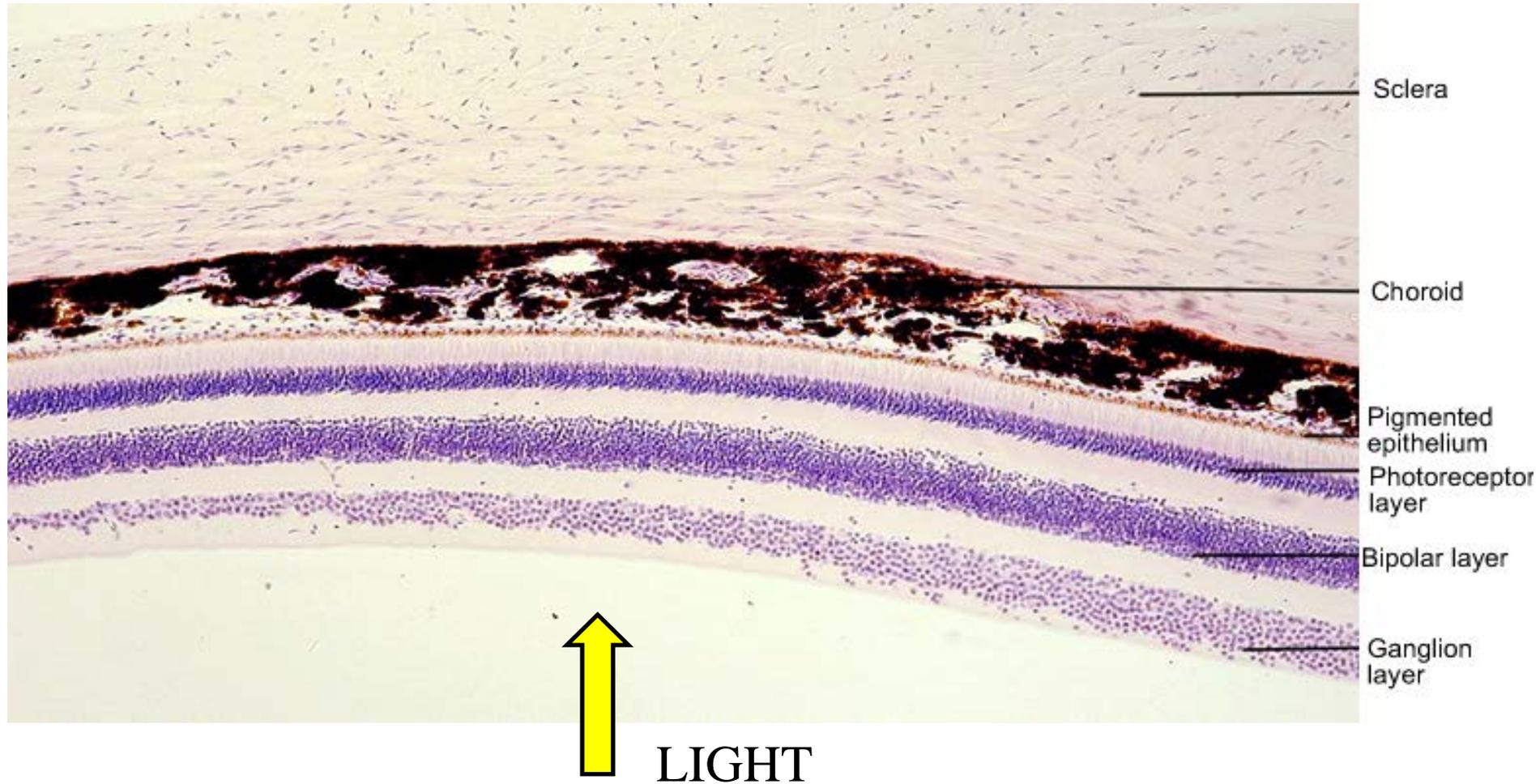
Crystalline lens



Jim Bowmaker dissecting an eye...



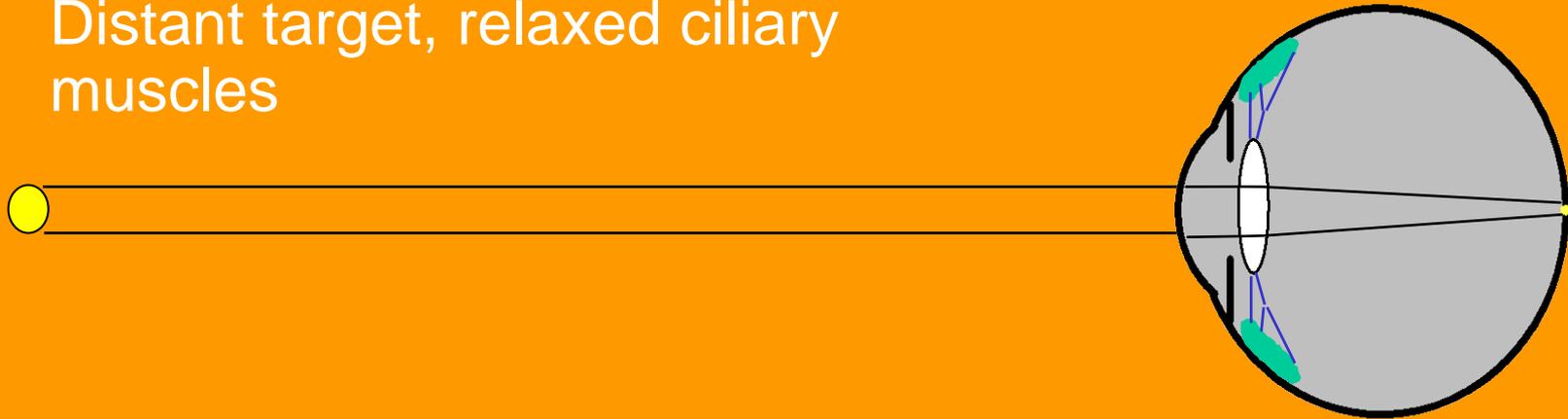
Retinal cross-section



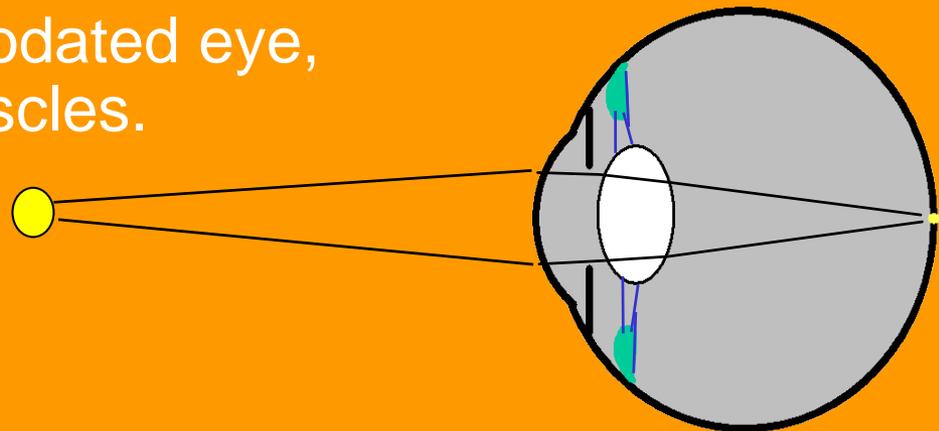
Retina 200 ×

Accommodation to Target Distance

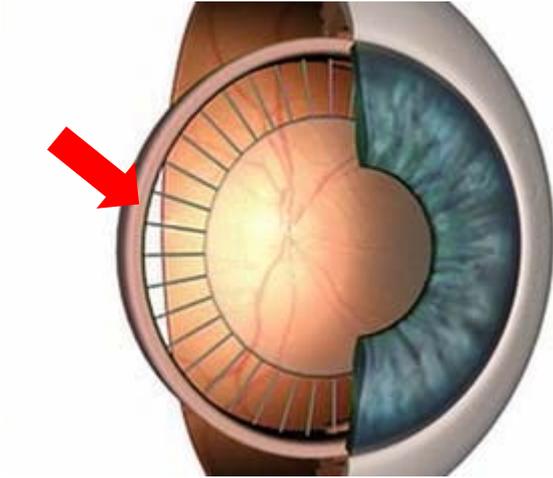
Distant target, relaxed ciliary muscles



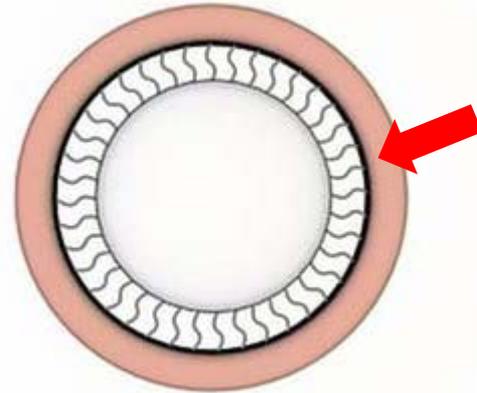
Near target, accommodated eye, constricted ciliary muscles.



Accommodation



Relaxed ciliary muscle
pulls zonules taut and
flattens crystalline lens.



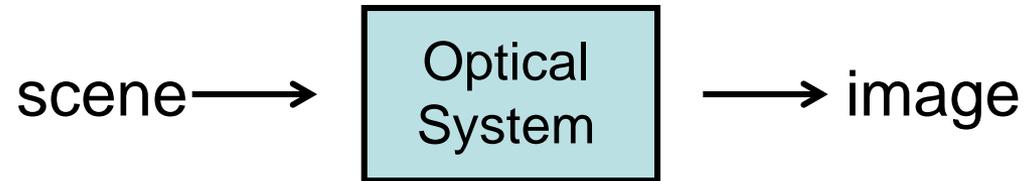
Constricted ciliary muscle
releases tension on zonules
and crystalline lens bulges.



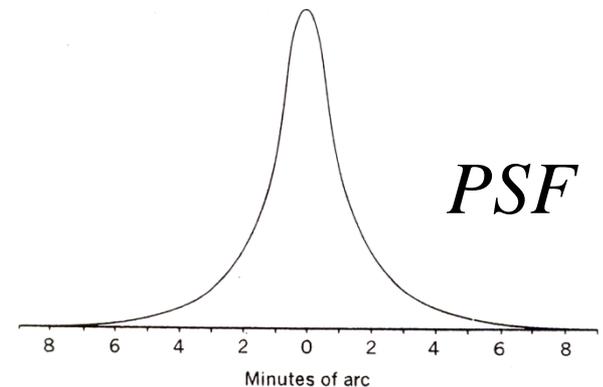
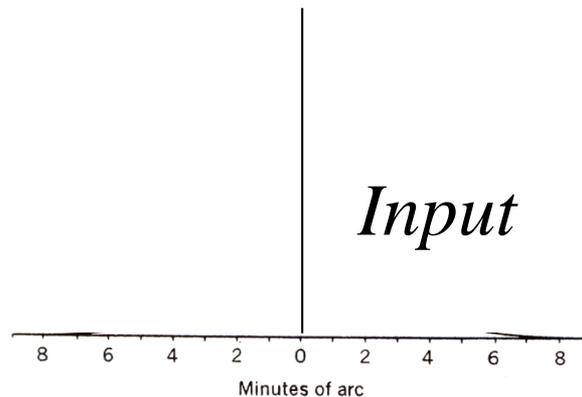
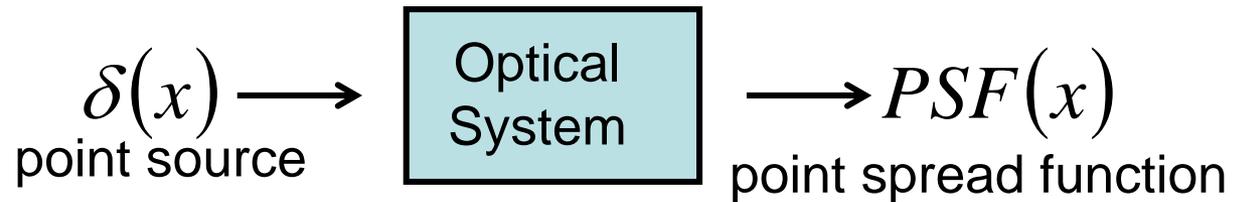
Image quality

Point spread function

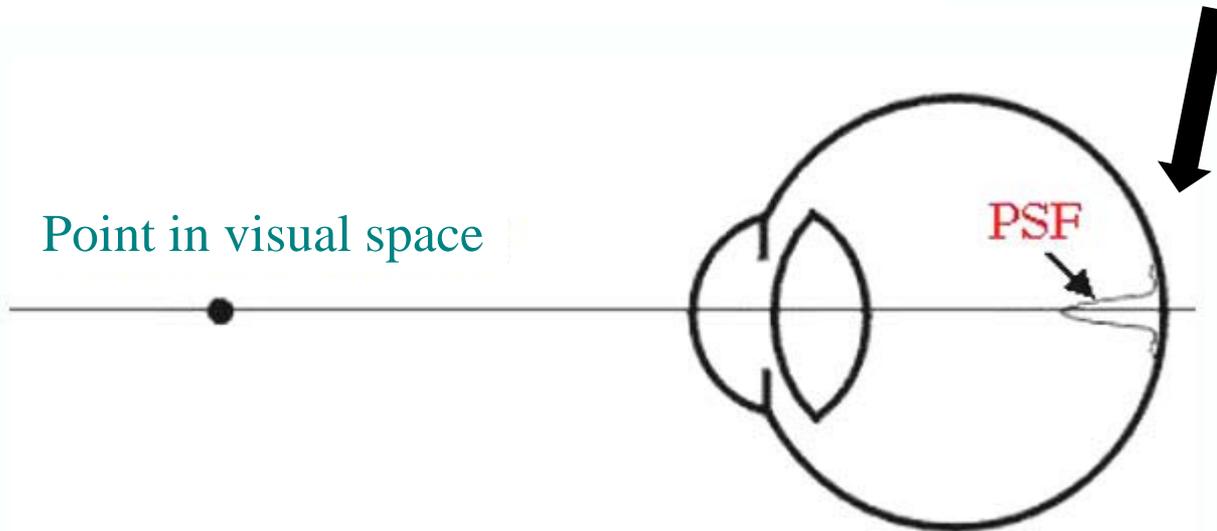
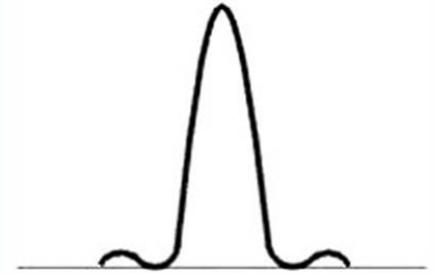
Optical systems are rarely ideal.



Point spread function of Human Eyes



Point spread function (PSF)



The Point Spread Function (PSF) characterizes the optical performance of the eye.

Measuring image quality “psychophysically”

1. Visual acuity measures

E	1	20/200	6/60
F P	2	20/100	6/30
T O Z	3	20/70	6/21
L P E D	4	20/50	6/15
P E C F D	5	20/40	6/12
E D F C Z P	6	20/30	6/9
F E L O P Z D	7	20/25	6/7.5
D E F P O T E C	8	20/20	6/6
L E F O D P C T	9		
F D P L T C E O	10		
F E Z O L C F T D	11		

Smallest resolvable black and white target. Many different types of tests are available , but the letter chart introduced by Snellen in 1862 is the most common.

E

1 20/200 6/60

F P

2 20/100 6/30

T O Z

3 20/70 6/21

L P E D

4 20/50 6/15

P E C F D

5 20/40 6/12

E D F C Z P

6 20/30 6/9

F E L O P Z D

7 20/25 6/7.5

D E F P O T E C

8 20/20 6/6

L E F O D P C T

9

F D P L T C E O

10

F E Z O L C F T D

11



NORMAL ACUITY

Snellen defined "standard vision" as the ability to recognize one of his optotypes when it subtended 5 minutes of arc. Thus, the optotype can only be recognized if the person viewing it can discriminate a spatial patterns separated by visual angles of 1 minute of arc.

A Snellen chart is placed at a standard distance, twenty feet in the US (6 metres in Europe). At this distance, the symbols on the line representing "normal" acuity subtend an angle of five minutes of arc, and the thickness of the lines and of the spaces between the lines subtends one minute of arc. This line, designated 20/20, is the smallest line that a person with normal acuity can read at a distance of twenty feet.

The letters on the 20/40 line are twice as large. A person with normal acuity could be expected to read these letters at a distance of forty feet. This line is designated by the ratio 20/40. If this is the smallest line a person can read, the person's acuity is "20/40."

E
F P
T O Z
L P E D
P E C F D
E D F C Z P
FELOPZD
DEFPOTEC
LEFODPCT
FDPLTCEO
FEZOLCFTD

1 20/200 6/60
 2 20/100 6/30
 3 20/70 6/21
 4 20/50 6/15
 5 20/40 6/12
 6 20/30 6/9
 7 20/25 6/7.5
 8 20/20 6/6
 9
 10
 11

E
F P
T O Z
L P E D
P E C F D
E D F C Z P
FELOPZD
DEFPOTEC
LEFODPCT
FDPLTCEO
FEZOLCFTD

1 20/200
 2 20/100
 3 20/70
 4 20/50
 5 20/40
 6 20/30
 7 20/25
 8 20/20
 9
 10
 11

E	1	20/200
F P	2	20/100
T O Z	3	20/70
L P E D	4	20/50
P E C F D	5	20/40
E D F C Z P	6	20/30
FELOPZD	7	20/25
DEFPOTEC	8	20/20
L E F O D F C T	9	
F D P L T C E O	10	
F E X O L C F T D	11	

E	1	20/200
F P	2	20/100
T O Z	3	20/70
L P E D	4	20/50
P E C F D	5	20/40
E D F C Z P	6	20/30
FELOPZD	7	20/25
DEFPOTEC	8	20/20
L E F O D F C T	9	
F D P L T C E O	10	
F E X O L C F T D	11	

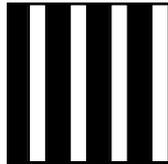
Visual Acuity: four standard methods

Letter
acuity
(Snellen)

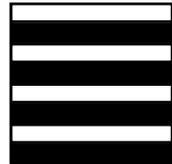


Can the subject correctly identify the letter or the letter orientation?

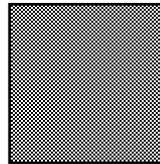
Grating
acuity



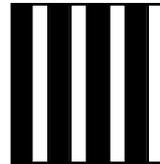
vs.



Orientation resolution acuity



vs.



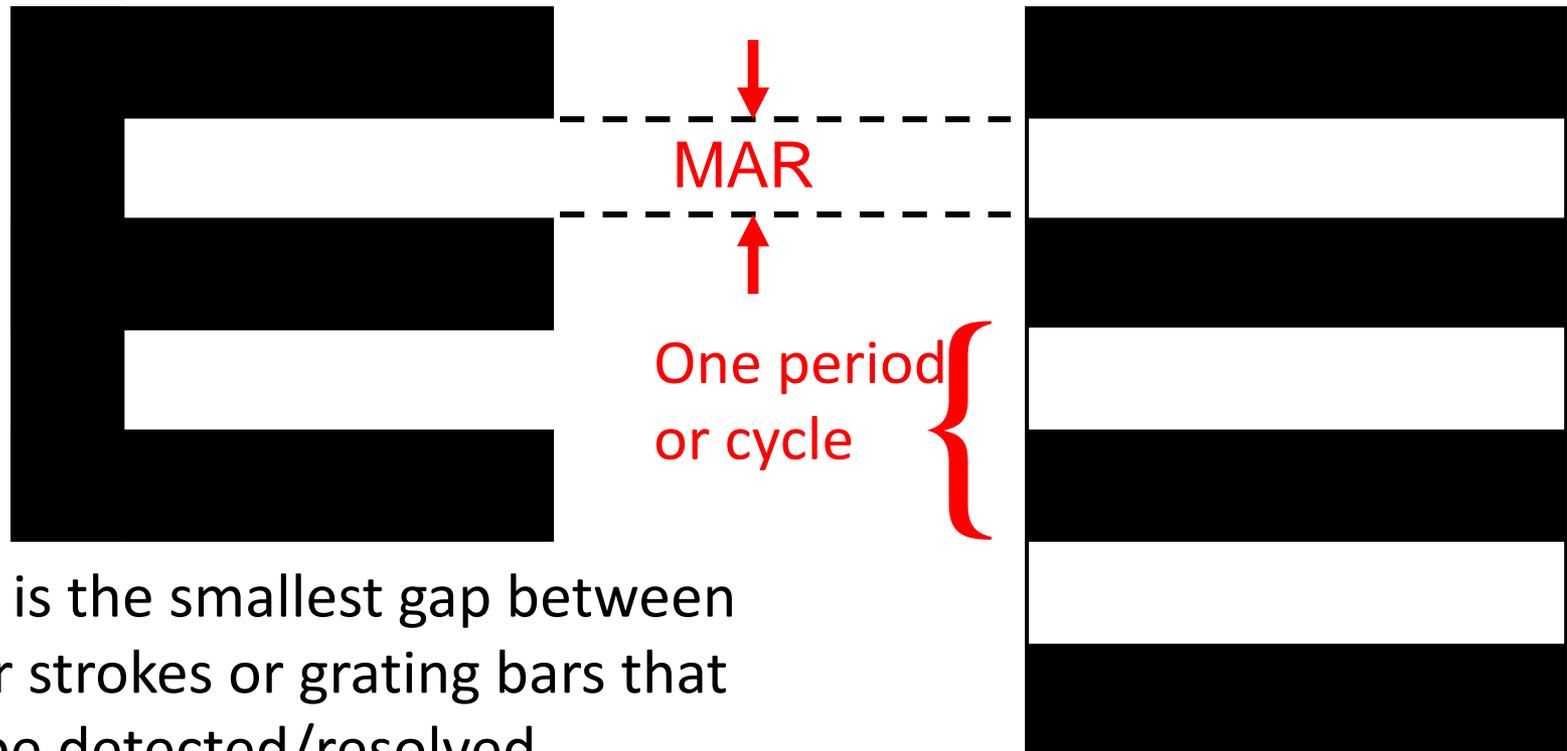
Detection acuity

2-line
resolution
2-point
resolution



Can the subject see two lines or points rather than one?

MAR = Minimum Angle of Resolution



MAR is the smallest gap between letter strokes or grating bars that can be detected/resolved.

6/6 (20/20) letter: bar/stroke width = 1 arc minute, letter height = 5 min
 Grating period = 2 arc minute (1/30 degree) when bar = 1 min,
 and grating SF = 1/period = 30 c/deg,

Comparison of seven different visual acuity measures

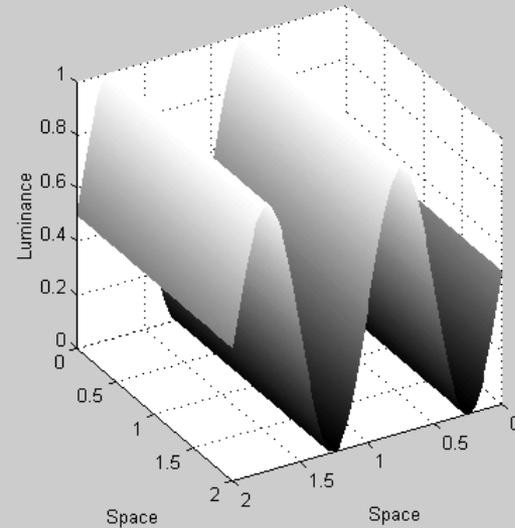
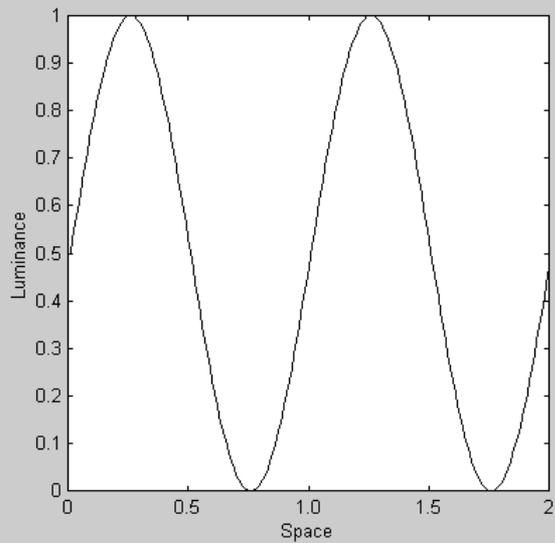
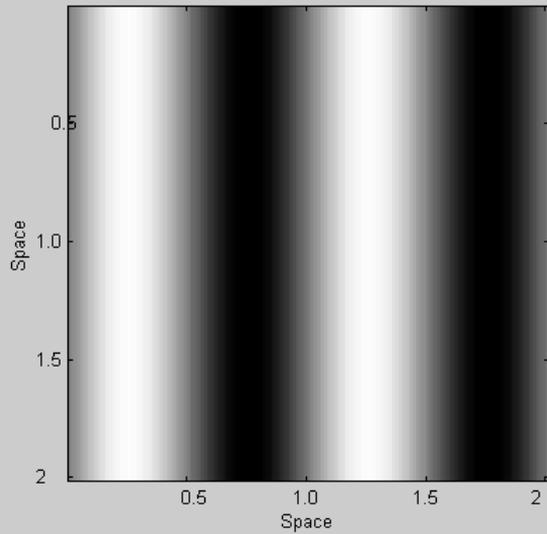

NORMAL
ACUITY

Snellen	Metric Snellen	MAR in arc minutes	Log MAR	Decimal	Grating VA c/deg
20/10	6/3	0.5	-0.3	2.0	60
20/15	6/4.5	0.75	-.12	1.33	40
20/20	6/6	1	0.0	1.0	30
20/25	6/7.5	1.25	0.1	0.8	24
20/30	6/9	1.5	0.18	0.7	21
20/40	6/12	2	0.3	0.5	15
20/50	6/15	2.5	0.4	0.4	12
20/70	6/21	3.5	0.54	0.3	9
20/100	6/30	5	0.7	0.2	6
20/200	6/60	10	1.0	0.1	3

Measuring image quality psychophysically

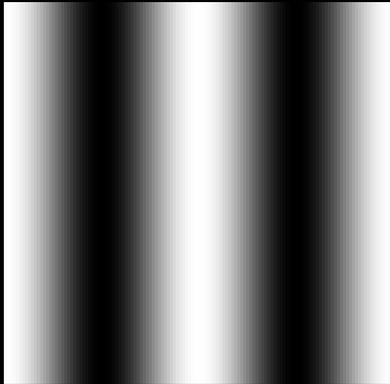
2. Spatial contrast sensitivity measures

Spatial frequency

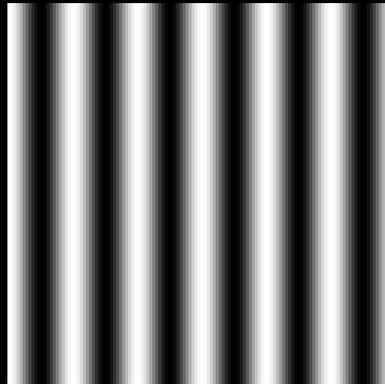


Harmonics of a square wave

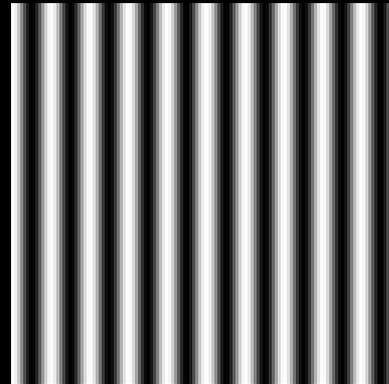
1



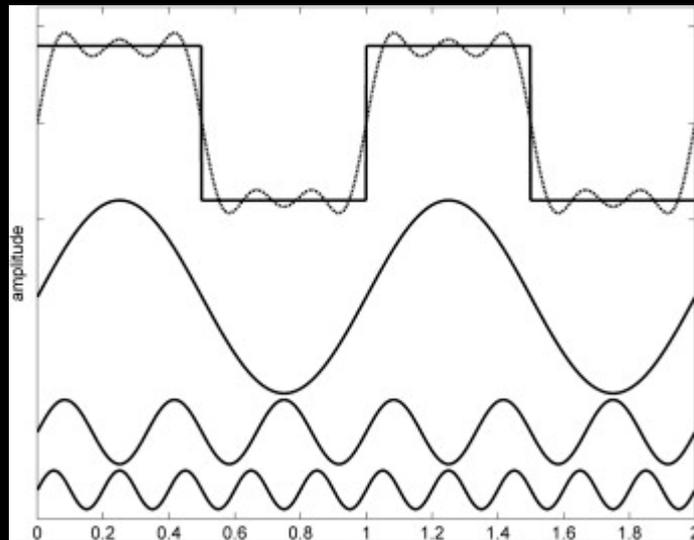
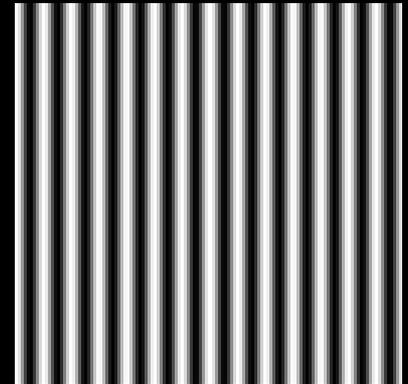
3



5



7



$$1+3+5$$

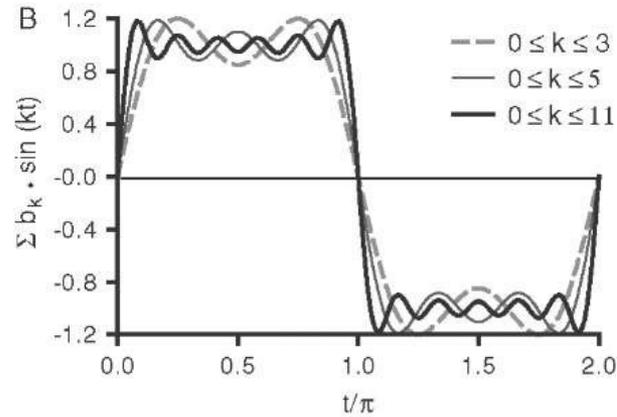
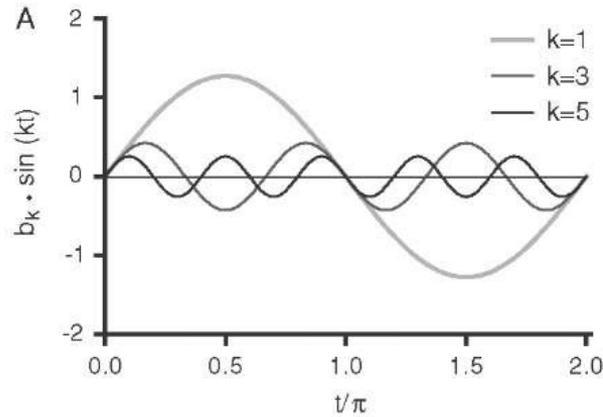
1

3

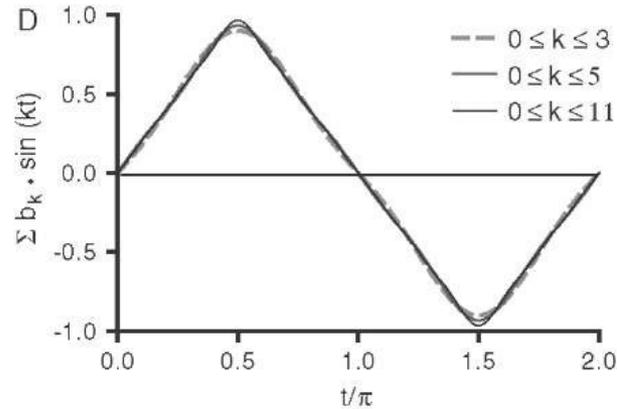
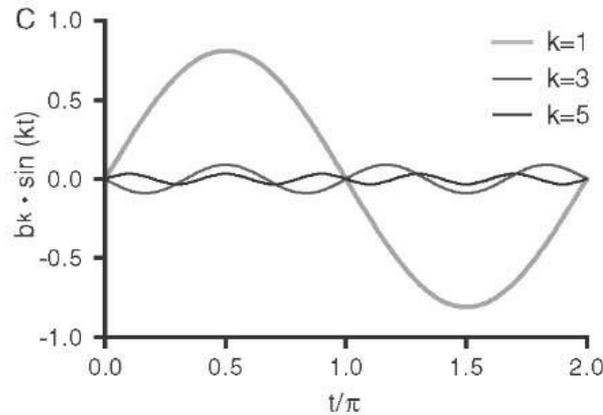
5

Steven Lehars

Harmonics of a square and triangle wave



Square



Triangle

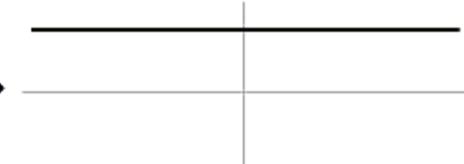
Fourier transform



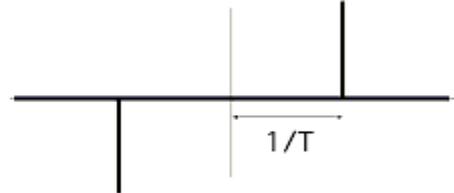
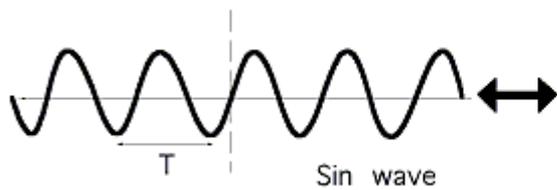
Inverse Fourier transform

Space

Spatial Frequency



All frequencies



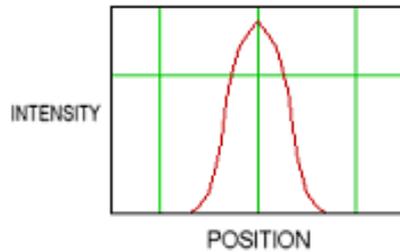
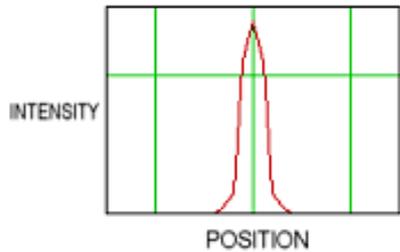
One frequency

Fourier transform



Image of line

Inverse Fourier transform

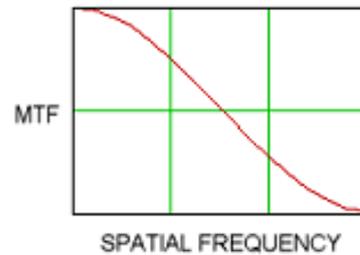
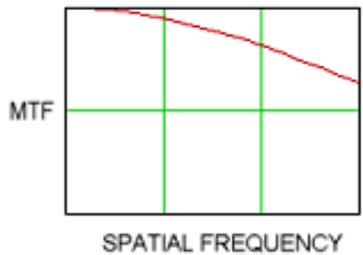


PSF

BETTER LENS

GOOD LENS

CALCULATED MTF



Spatial MTF



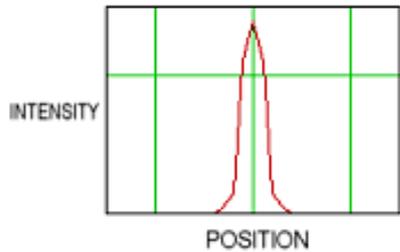
What would the results for a perfect lens look like?

Fourier transform

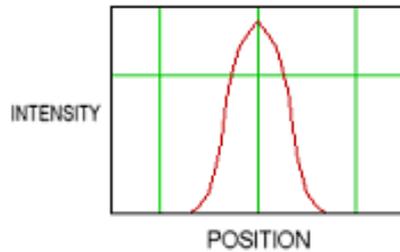


Image of line

Inverse Fourier transform



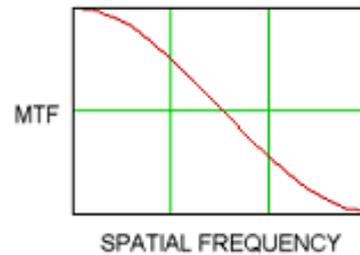
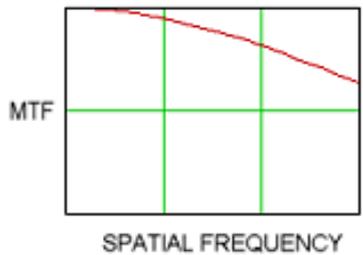
BETTER LENS



GOOD LENS

PSF

CALCULATED MTF



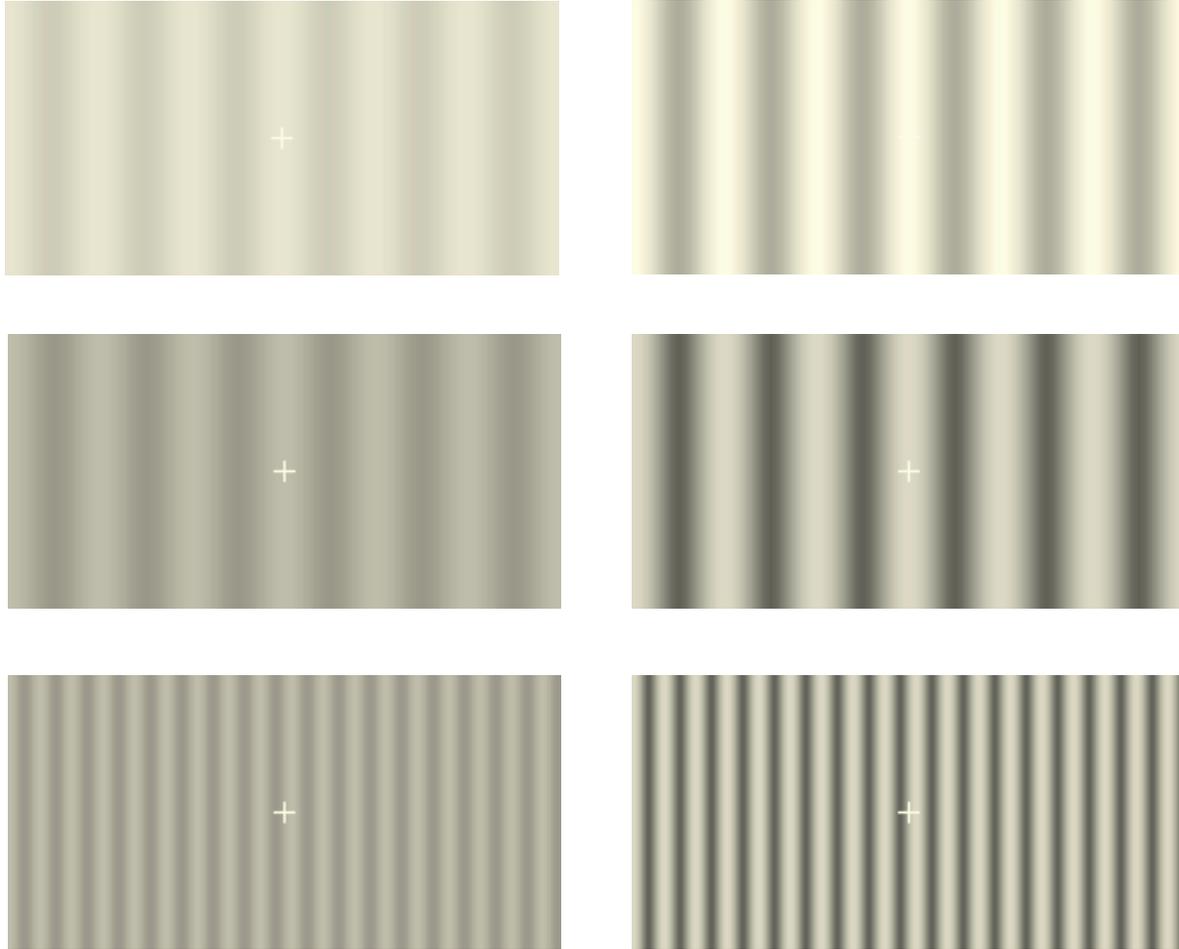
Spatial MTF

We can measure this "psychophysically"



Spatial frequency gratings

Increasing spatial frequency

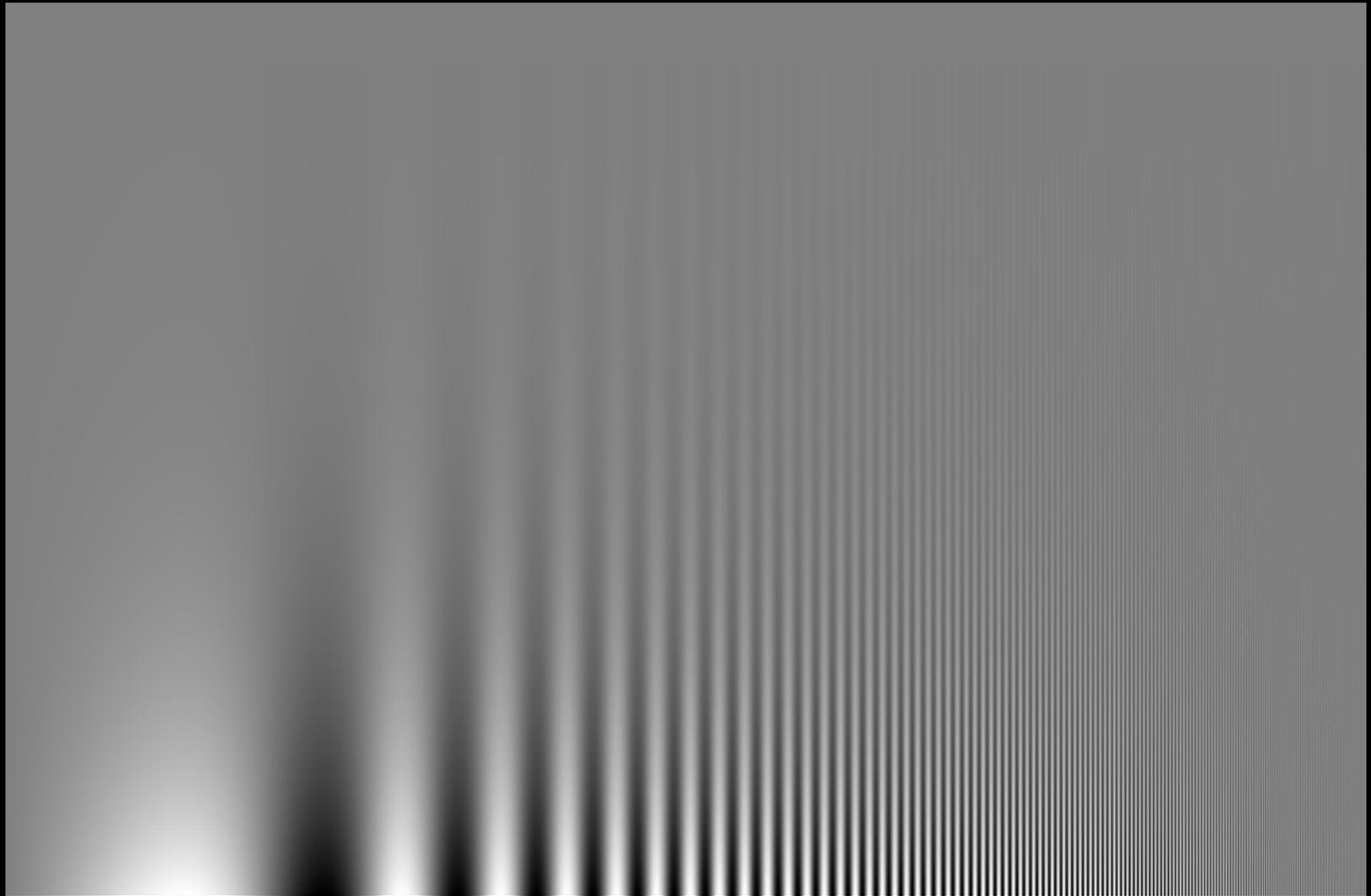


Increasing contrast

Spatial MTF

Spatial frequency in this image increases in the horizontal direction and modulation depth decreases in the vertical direction.

Increasing contrast



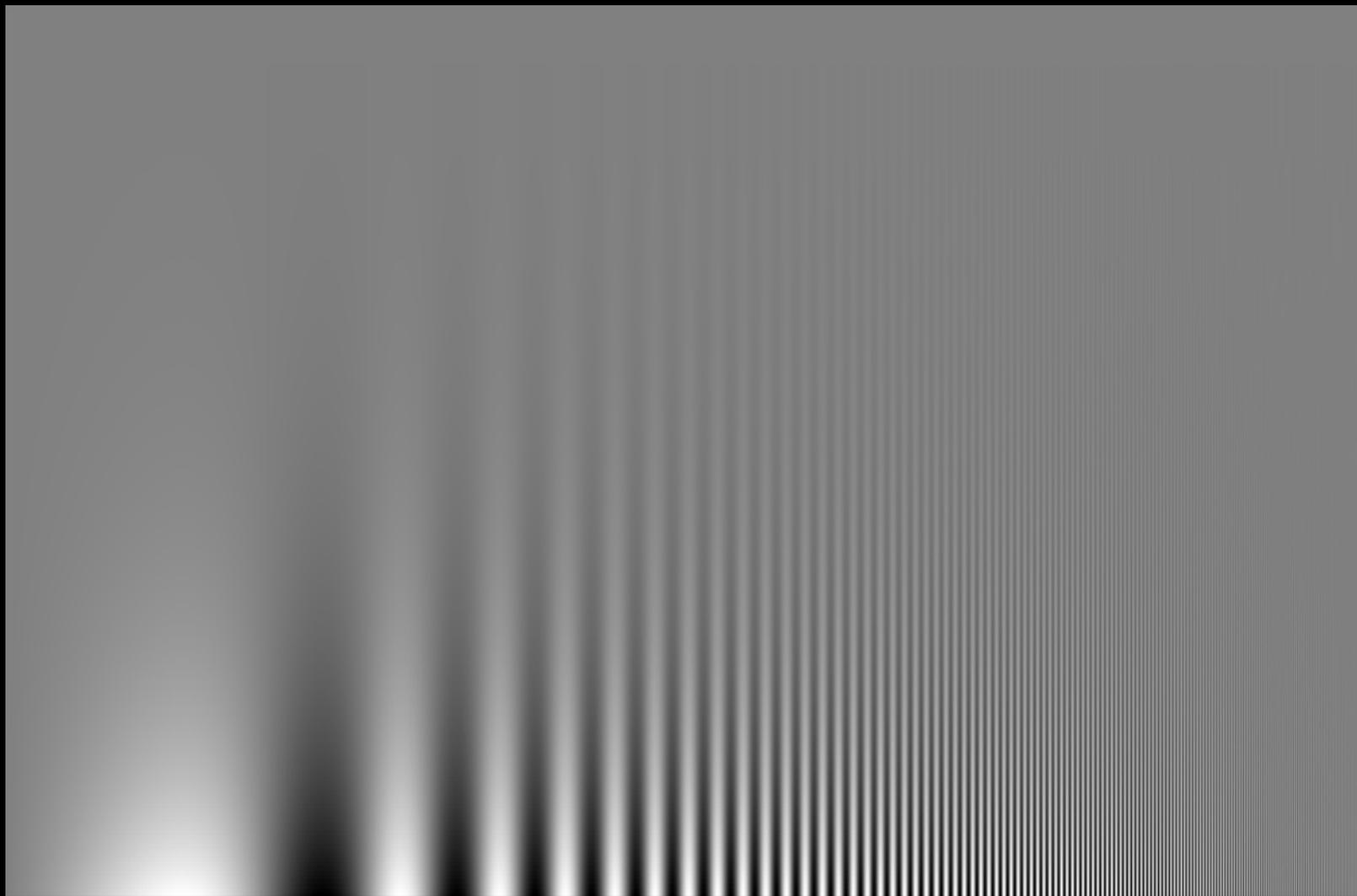
Increasing spatial frequency



Spatial MTF

The apparent border between visible and invisible modulation corresponds to your own visual modulation transfer function.

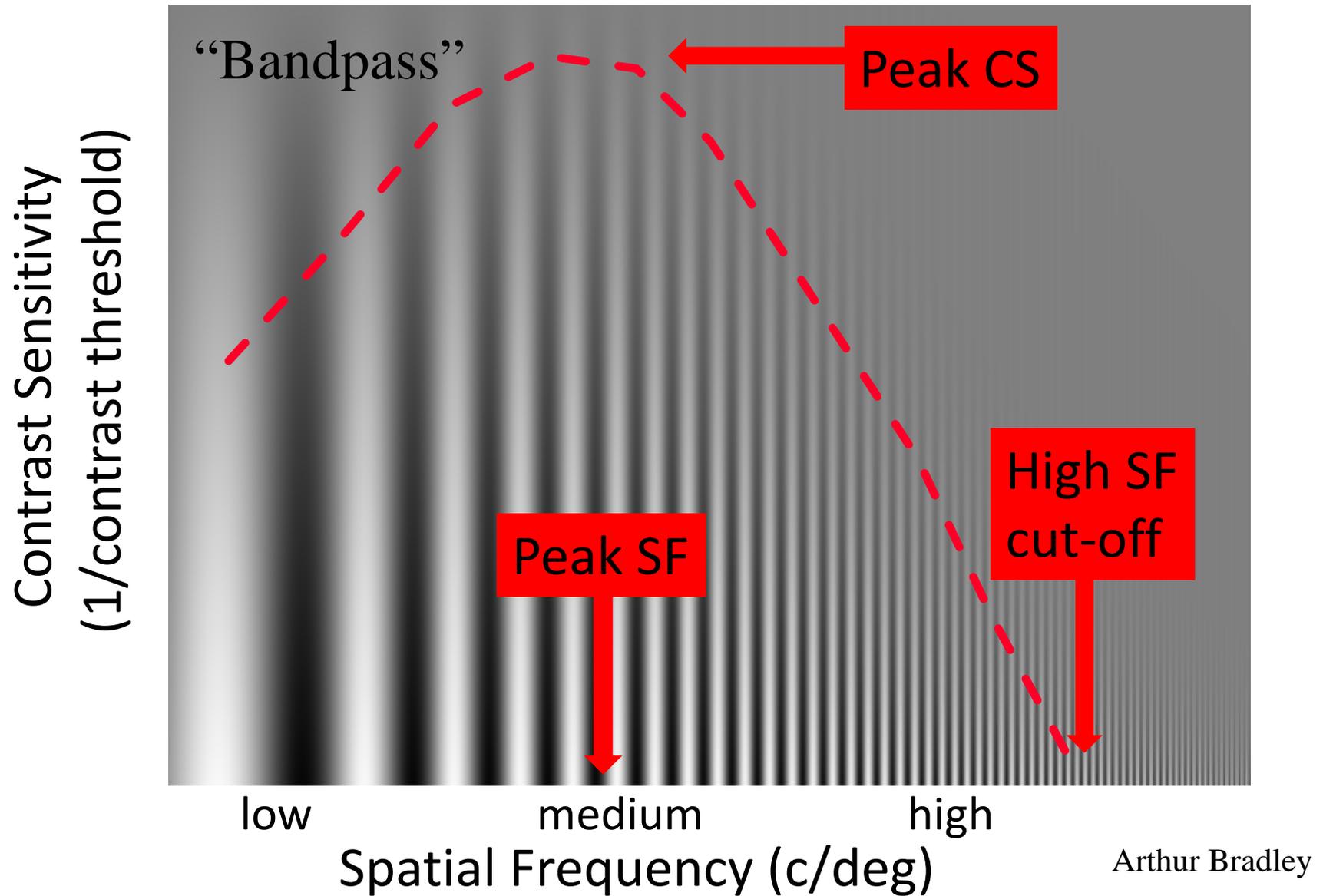
Increasing contrast



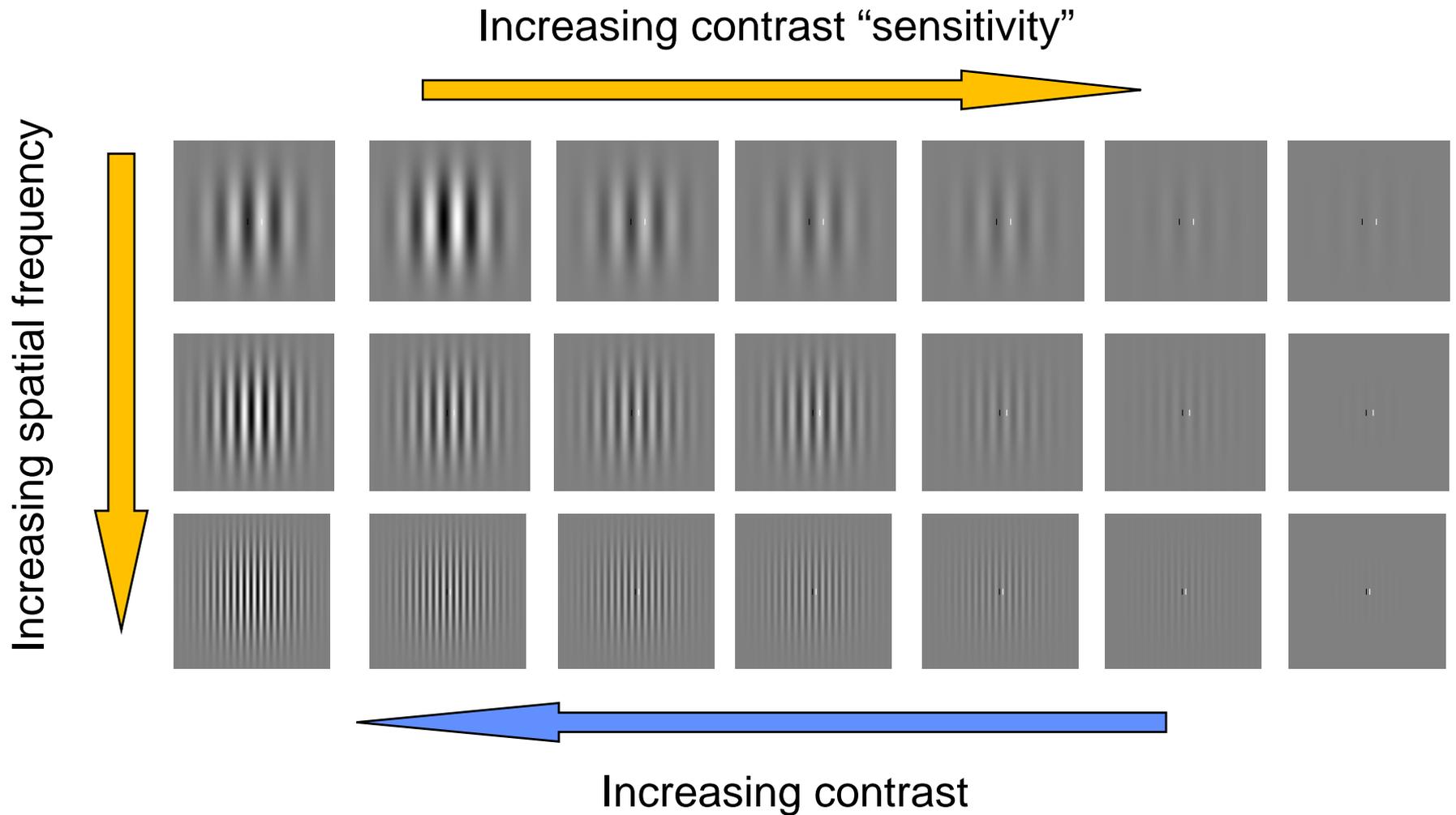
Increasing spatial frequency

2. Grating Contrast Sensitivity

Contrast Sensitivity Function (CSF)



Example of grating contrast sensitivity test using printed gratings



Spatial CSFs

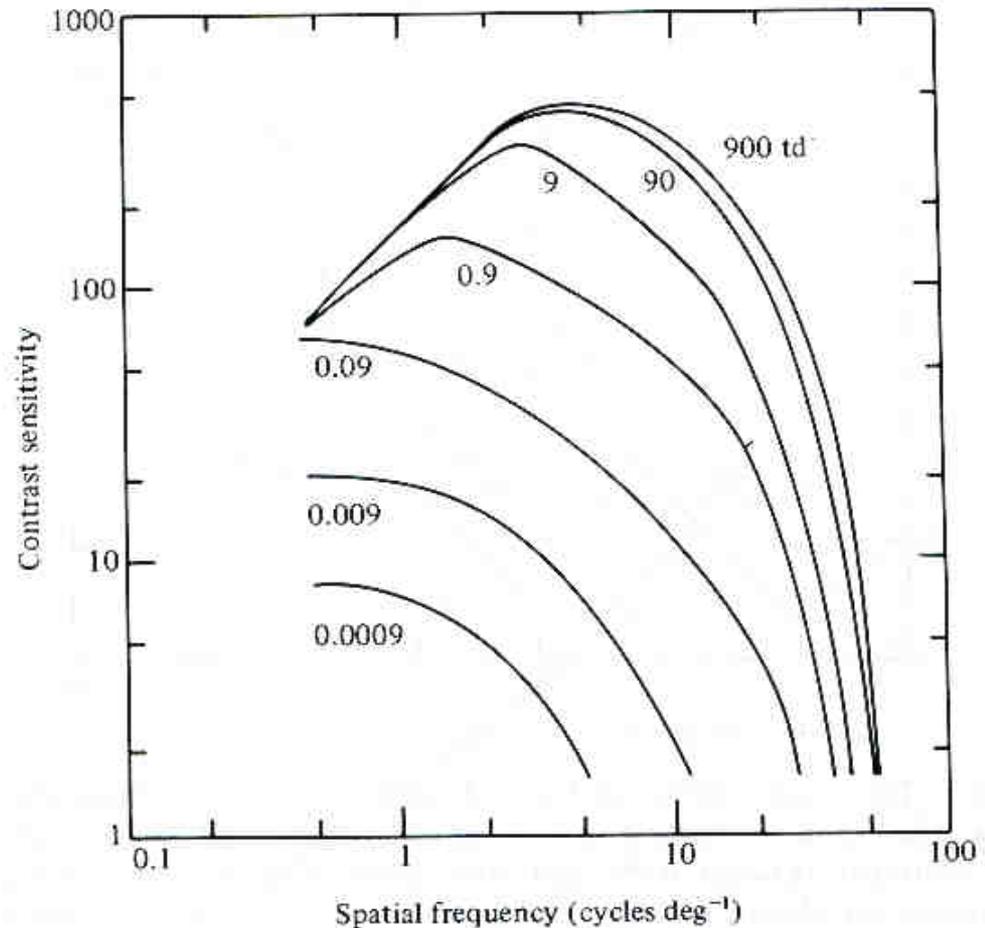
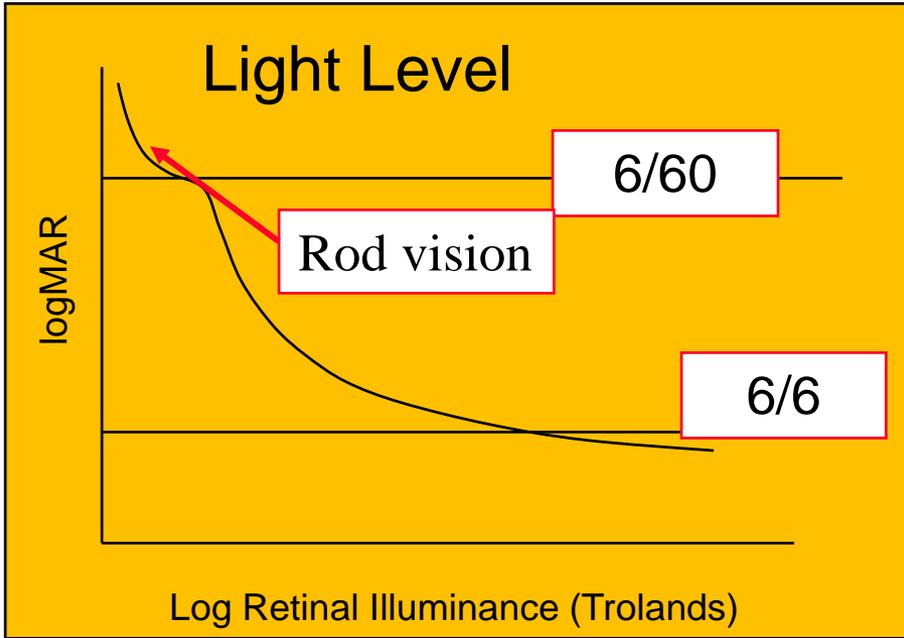
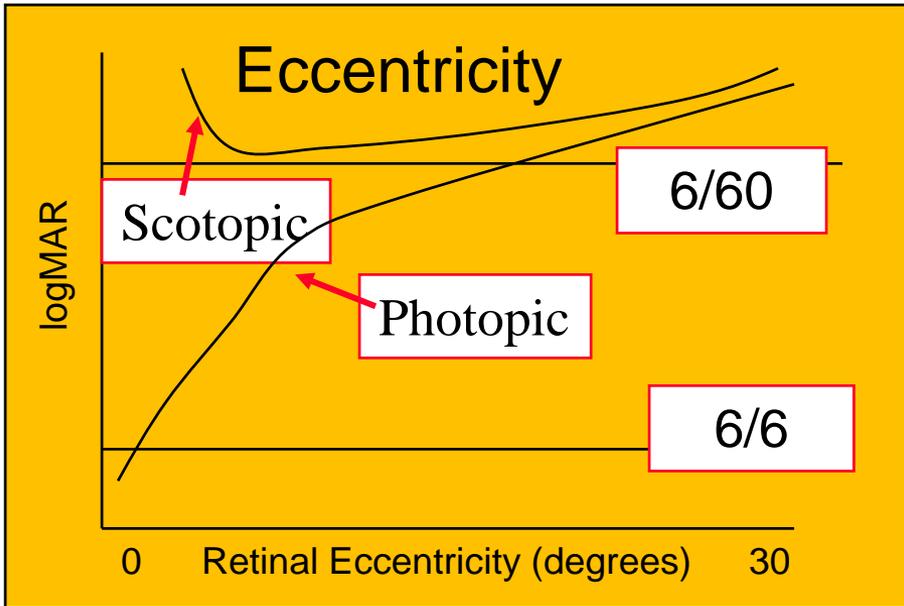


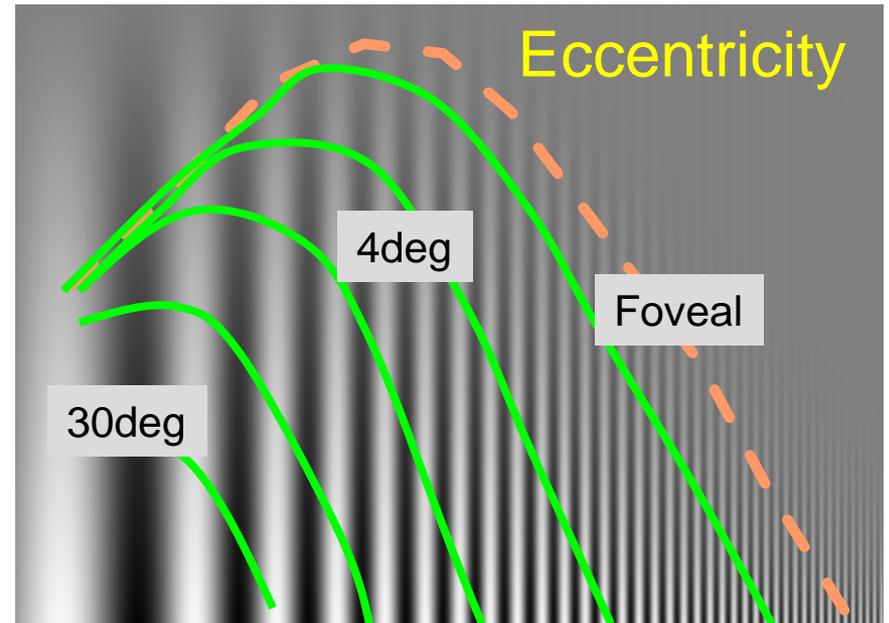
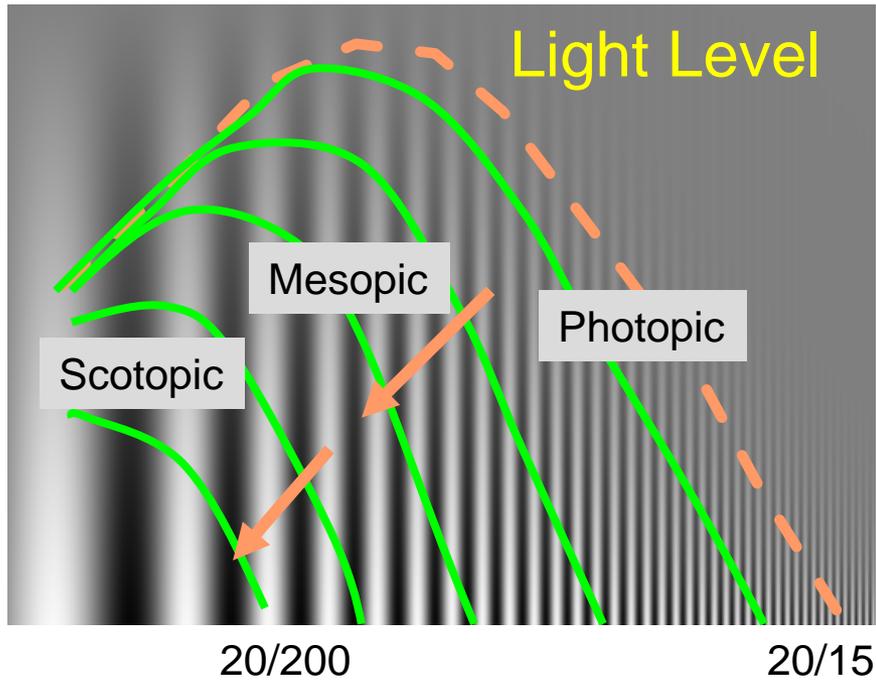
Fig. 8.4. Spatial contrast sensitivity curves at seven different retinal illuminance levels between 0.0009 and 900 trolands. The subject viewed the gratings through a 2 mm diameter artificial pupil. The wavelength of the light was 525 nm. Notice the loss of sensitivity for medium and high frequencies as the retinal illumination is decreased. (Adapted from Van Nes & Bouman, 1967.)



Vision is not always 6/6!

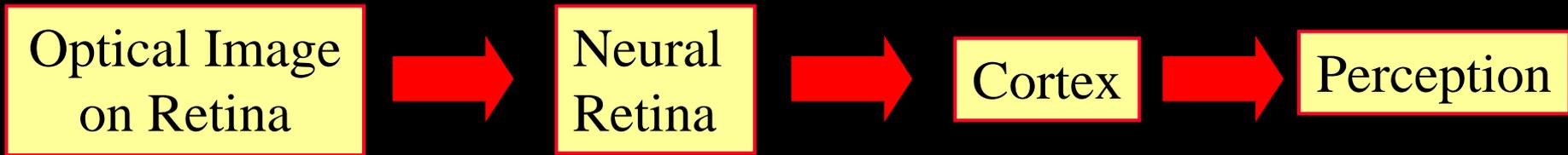


Contrast Sensitivity is not constant!



What limits visual
performance?

Stages



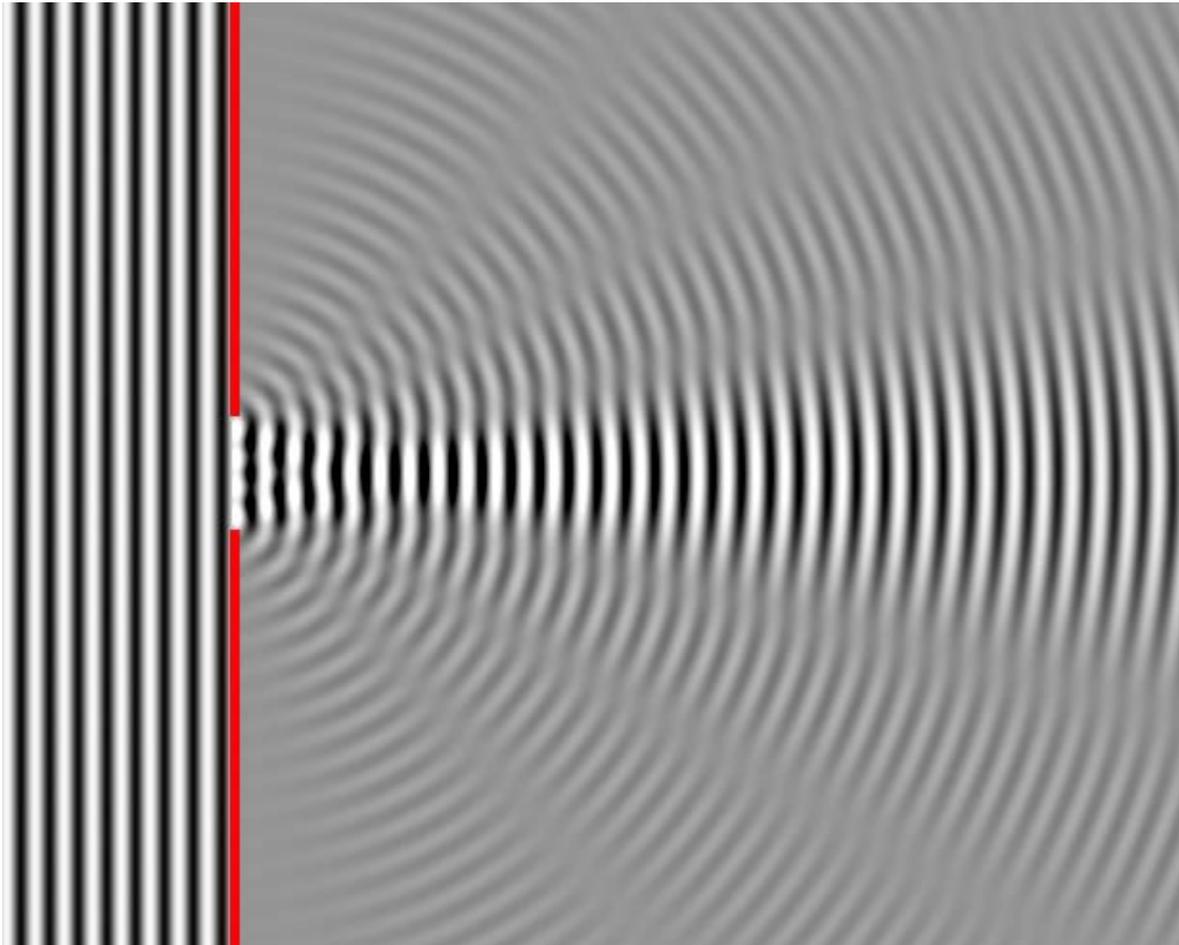
Stages

Optical Image
on Retina



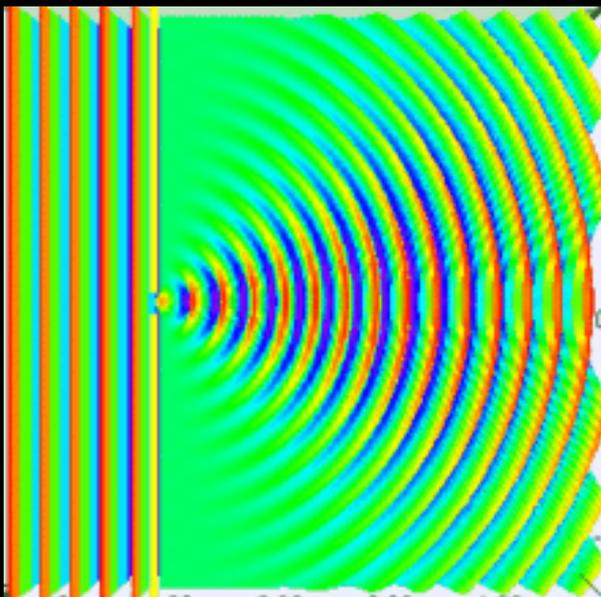
Consider optical limits first

The visual image is diffraction limited

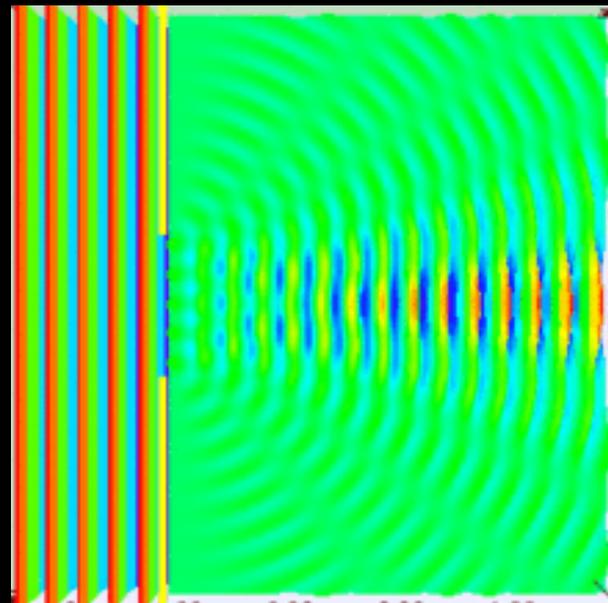


Approximation of diffraction pattern from a slit of width four wavelengths with an incident plane wave. The main central beam, nulls, and phase reversals are apparent (Wikipedia).

1-wavelength slit



5-wavelength slit



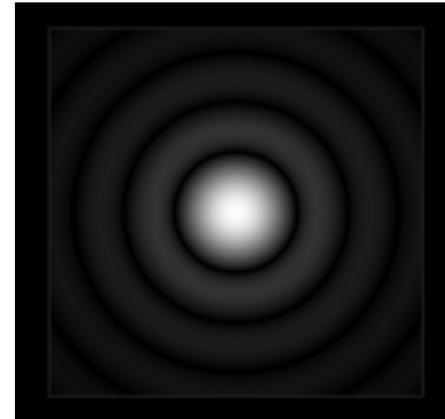
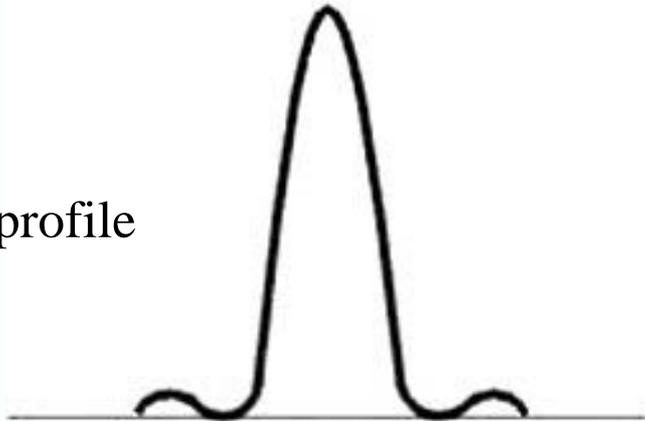
Airy disc (PSF)

For a diffraction-limited image an Airy disk pattern is formed on the retina from a point source due to the diffraction at the pupil.

Perception



2D profile



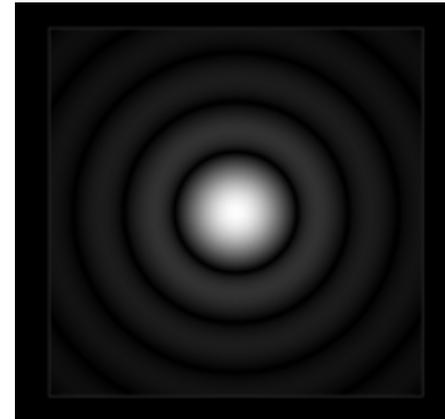
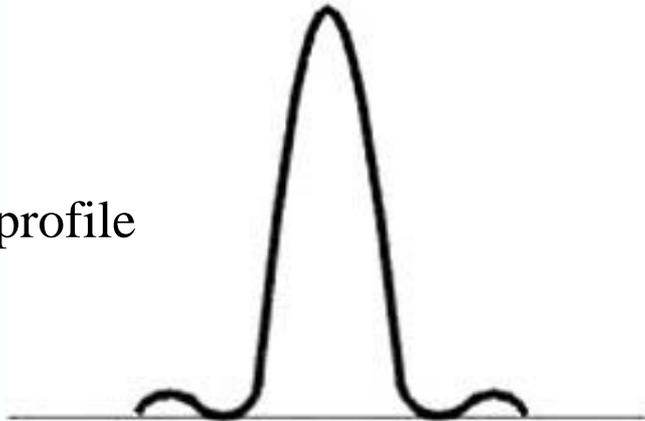
Airy disc (PSF)

How does this affect spatial resolution?

Perception

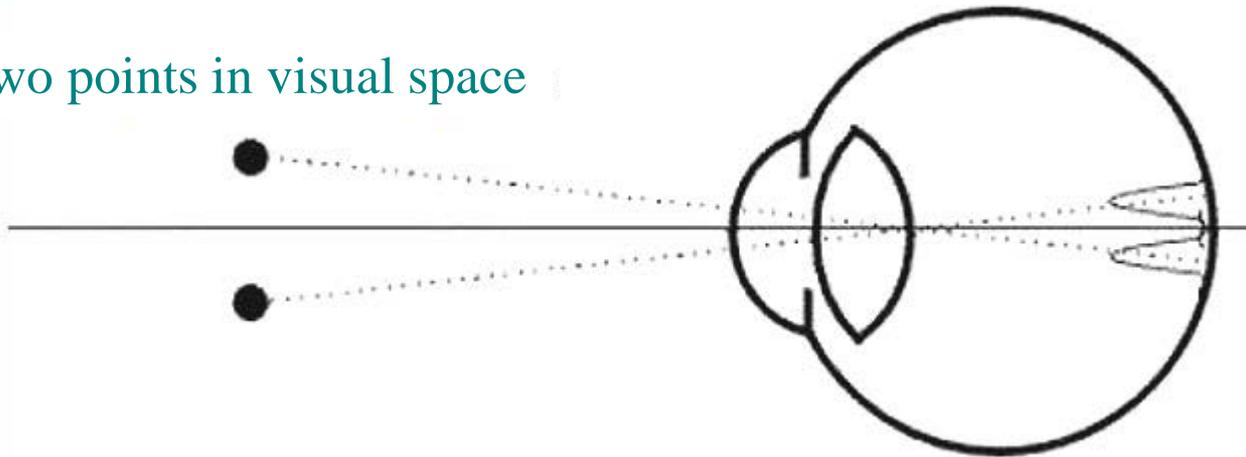


2D profile



Overlapping point spread functions (PSF)

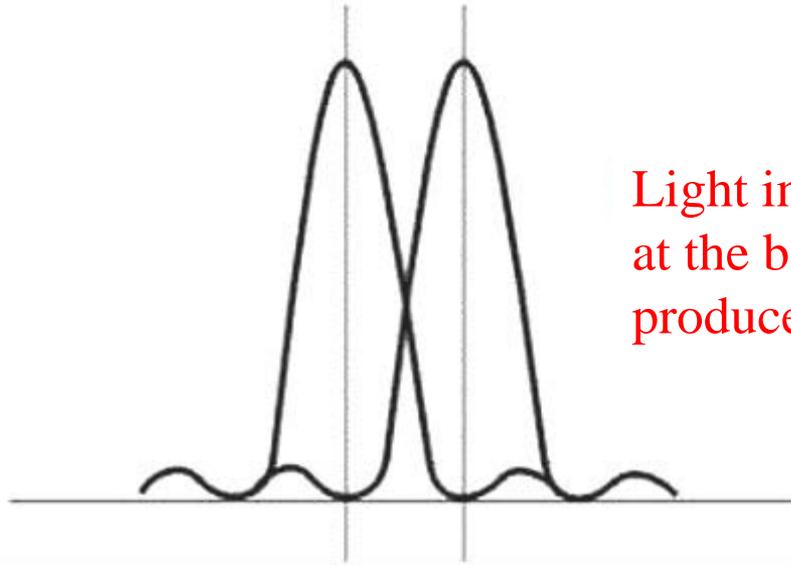
Two points in visual space





Two points in visual space

From Webvision,
Michael Kalloniatis



Light intensity profile (PSF)
at the back of the eye
produced by the points

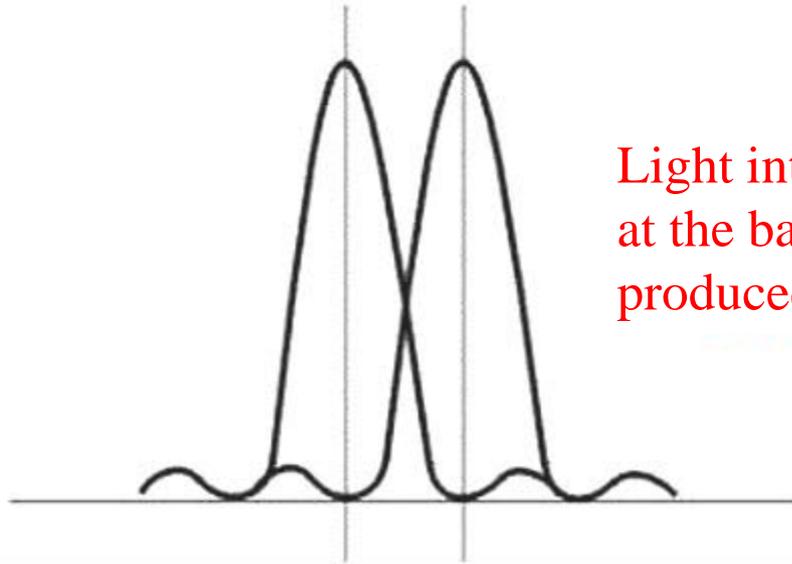
The **Rayleigh criterion** for resolving two point sources of equal brightness is when the peak of one diffraction pattern lies upon the first minimum of the other. This yields a theoretical maximum angular resolution referred to as *diffraction-limited resolution* given by:

$$\Delta\theta = 1.22 \frac{\lambda}{D}$$

where $\Delta\theta$ is in radians, D is the diameter of the aperture (i.e. the pupil in this case) in the same units as the wavelength λ of the light.



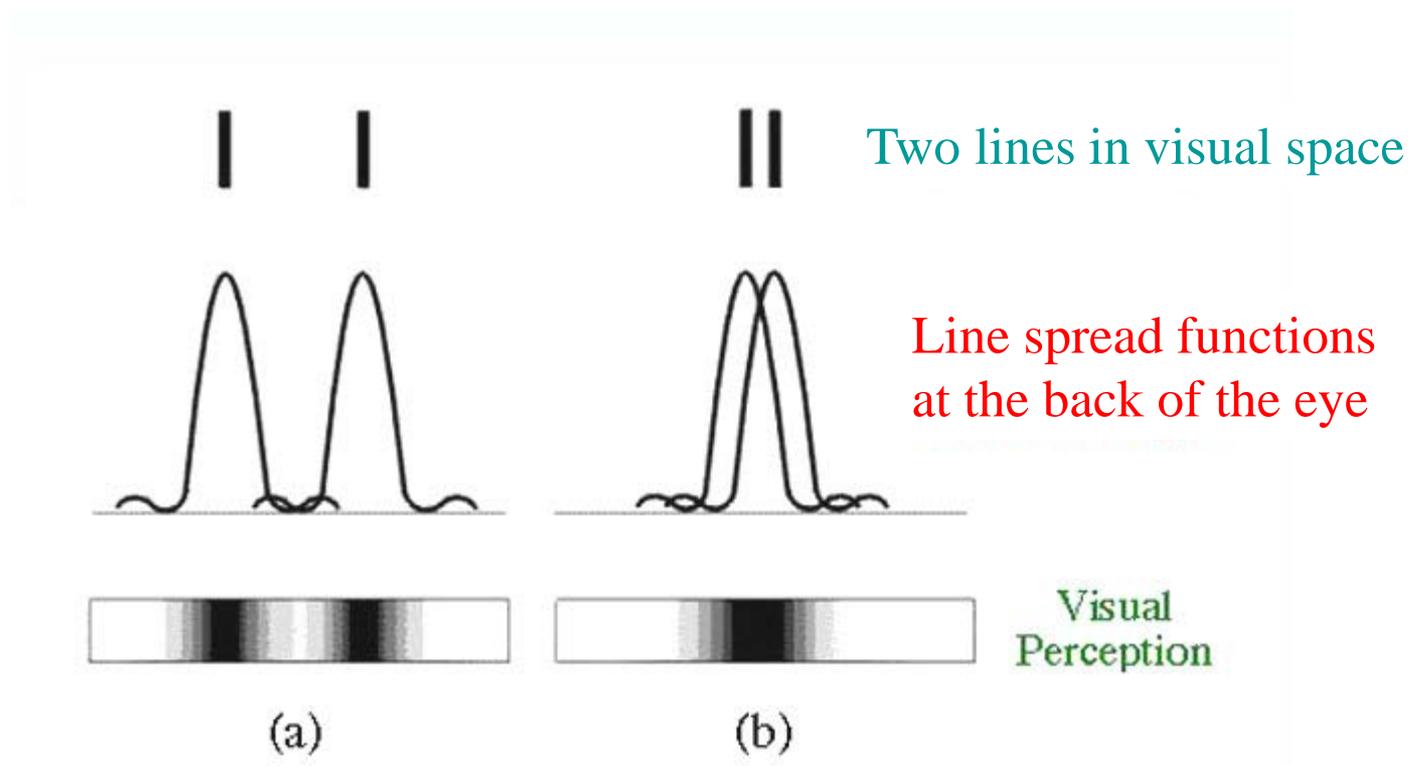
Two points in visual space



Light intensity profile (PSF)
at the back of the eye
produced by the points

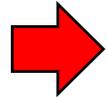
$$\Delta\theta = 1.22 \frac{\lambda}{D}$$

So, for a 550 nm light and a 3 mm diameter pupil, $\Delta\theta = 0.77$ min of arc.



The two lines (a) can be perceptually resolved, but the two lines (b) cannot and are perceived as a single line.

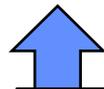
Comparison of seven different visual acuity measures



DIFFRACTION
LIMIT

Snellen	Metric Snellen	MAR in arc minutes	LogMAR	Decimal	Grating VA c/deg	Jaeger Near VA
20/10	6/3	0.5	-0.3	2.0	60	NA
20/15	6/4.5	0.75	-.12	1.33	40	NA
20/20	6/6	1	0.0	1.0	30	J1+
20/25	6/7.5	1.25	0.1	0.8	24	J1
20/30	6/9	1.5	0.18	0.7	21	J2
20/40	6/12	2	0.3	0.5	15	J3
20/50	6/15	2.5	0.4	0.4	12	J5
20/70	6/21	3.5	0.54	0.3	9	J7
20/100	6/30	5	0.7	0.2	6	J10
20/200	6/60	10	1.0	0.1	3	J16

Snellen	Metric Snellen	MAR in arc minutes	LogMAR	Decimal	Grating VA c/deg	Jaeger Near VA
20/20	6/6	1	0.0	1.0	30	J1+



Normal acuity is well matched to the diffraction limited resolution for a 550 nm light and a 3 mm diameter pupil of 0.77 min of arc.

Pupil size

The size of the pupil is an important factor affecting visual acuity.

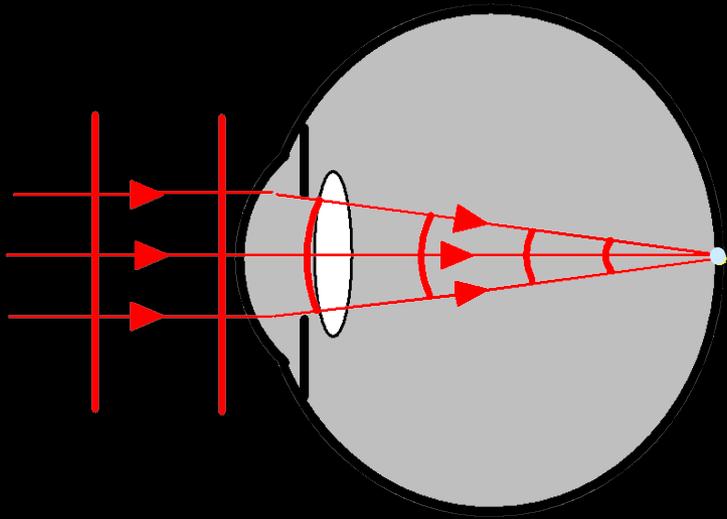
A large pupil allows more light to reach the retina and reduces diffraction but resolution is reduced because the optical aberrations are greater (a greater area of the lens and cornea are used and they are imperfect).

A small pupil reduces optical aberrations but resolution is then diffraction limited.

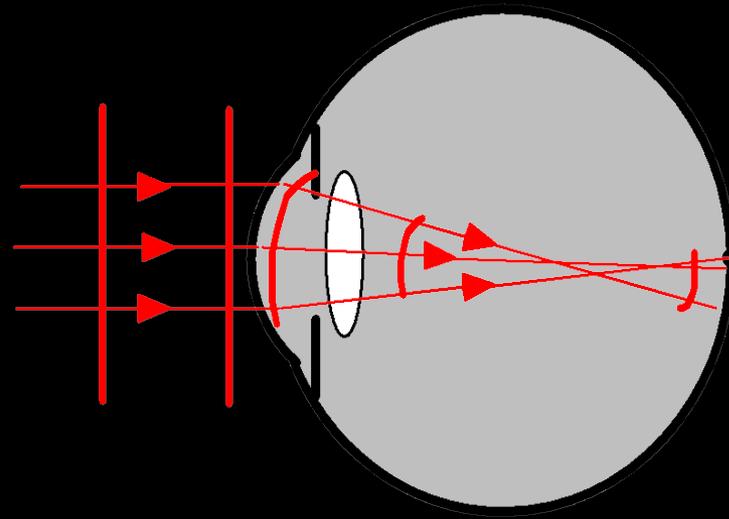
A mid-size pupil of about 3 mm to 5 mm represents a compromise between the diffraction and aberration limits

Aberrations of the Eye

Perfect optics



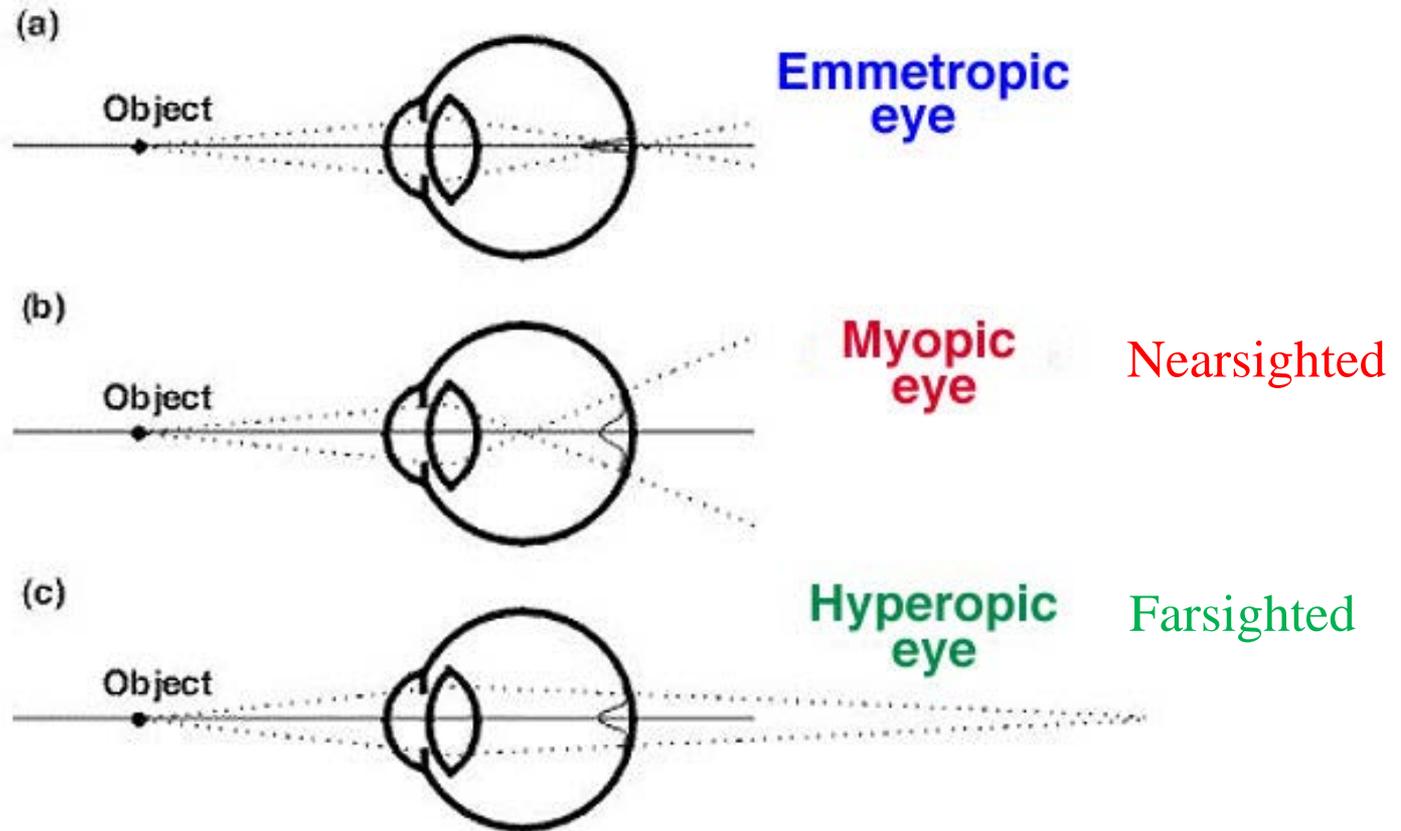
Imperfect optics

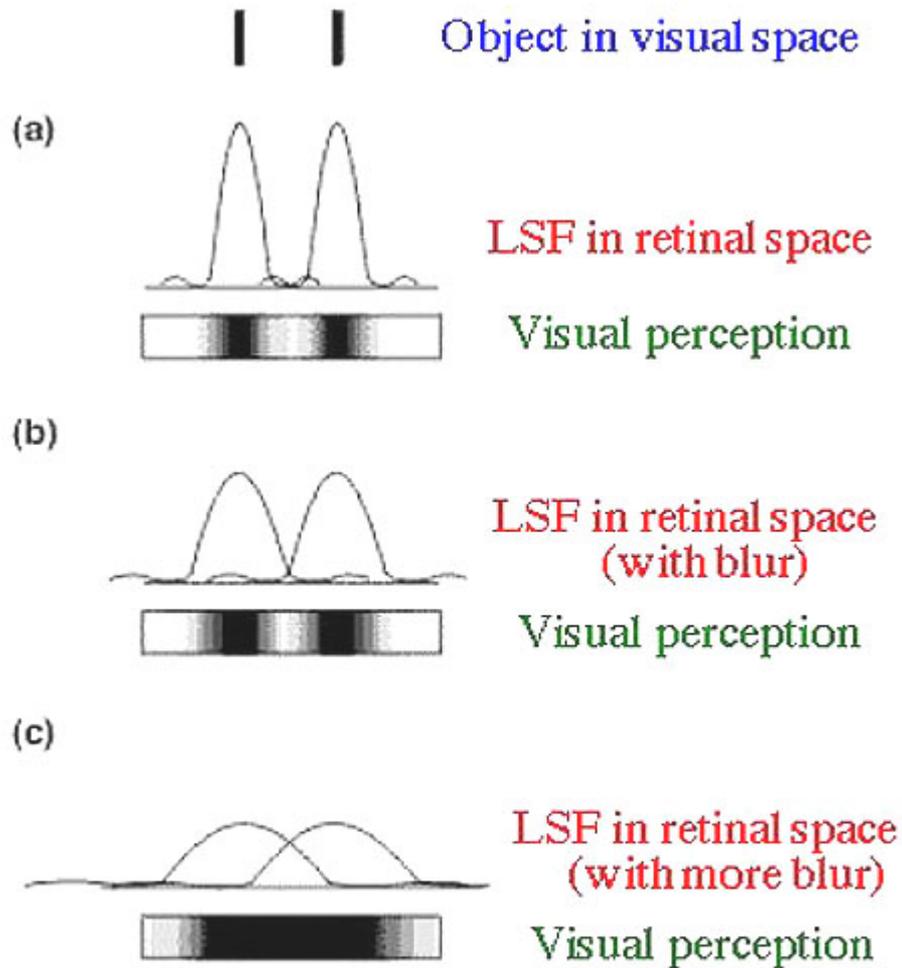


So far we have been talking about
foveal vision at optimal light levels
with optimal refraction...

Refractive errors

PSFs for different refractive errors

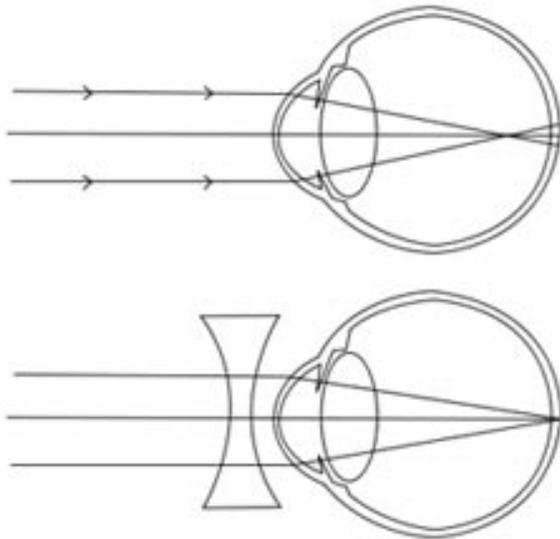




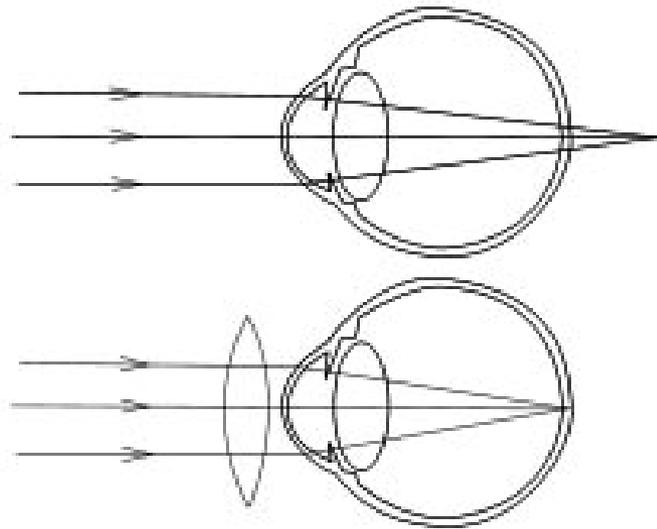
Line spread function (LSF) of two lines with varying amounts of blur. With increasing blur, the discrimination of the two lines is lost.

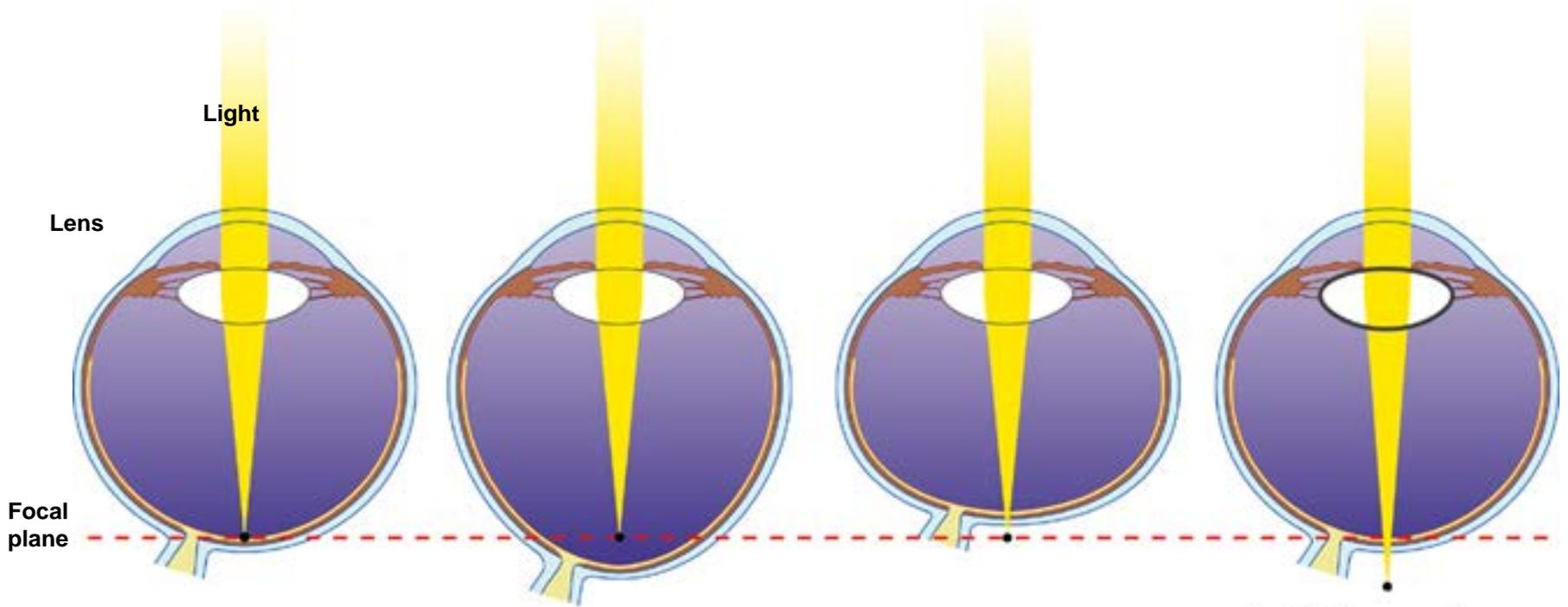
Corrective lenses

Myopia



Hyperopia





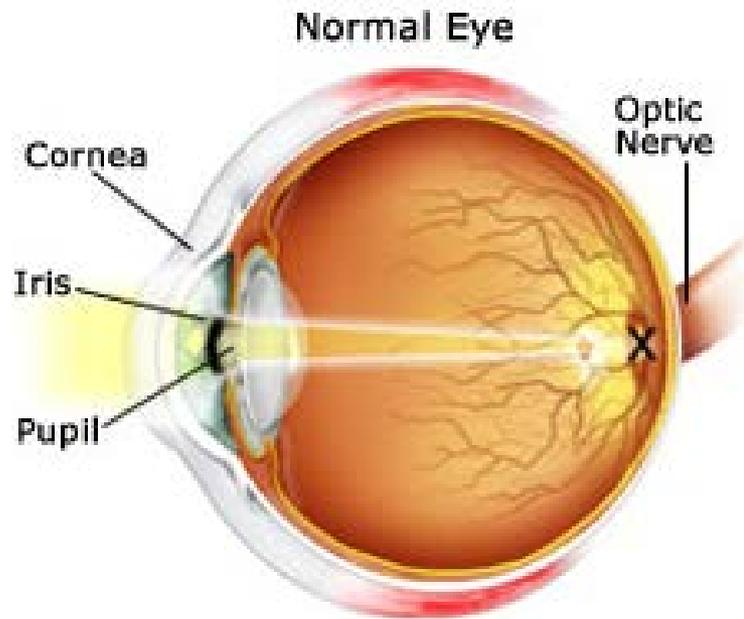
**Emmetropia
(normal)**

**Myopia
(nearsightedness)**

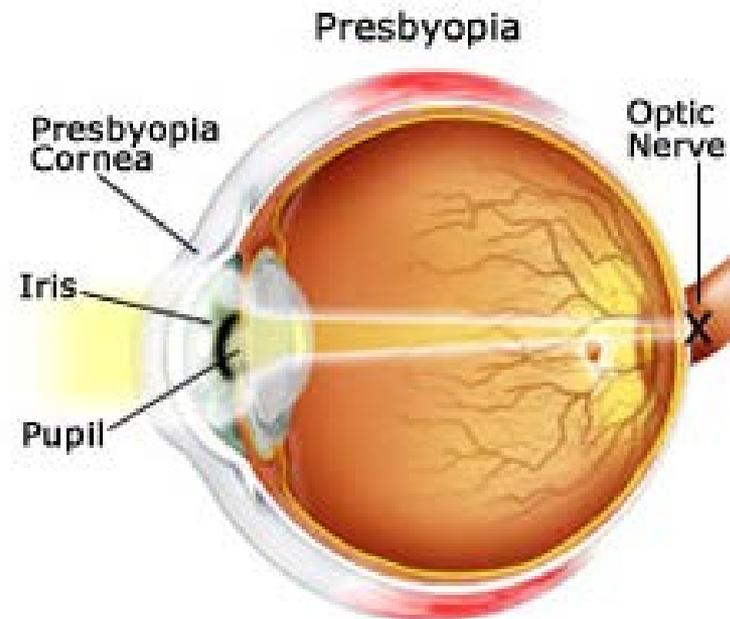
**Hyperopia
(farsightedness)**

**Presbyopia
(aged)**

Presbyopia (age related far-sightedness)



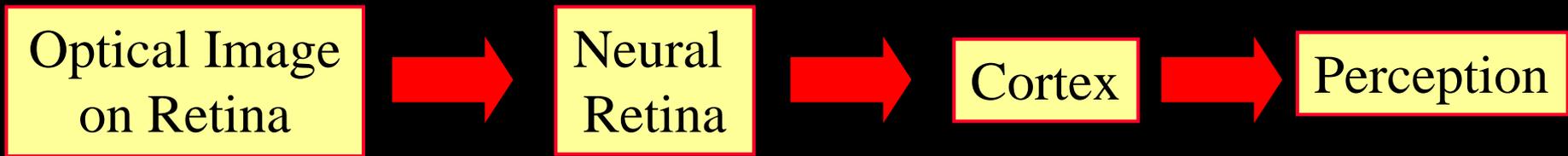
Images are formed directly on the retina creating good close up vision.



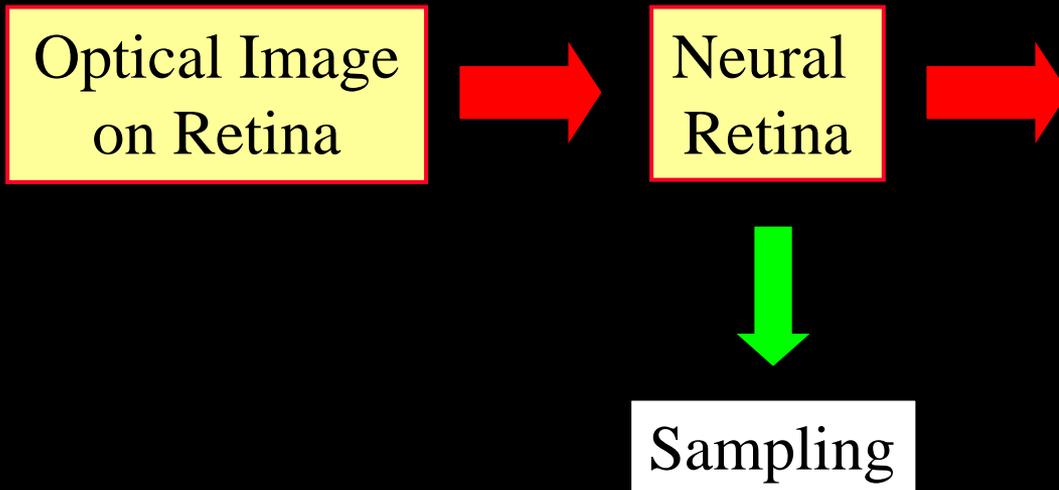
The lens ages and stiffens. Images are formed behind the retina causing blurry close up vision.

What else limits visual
performance?

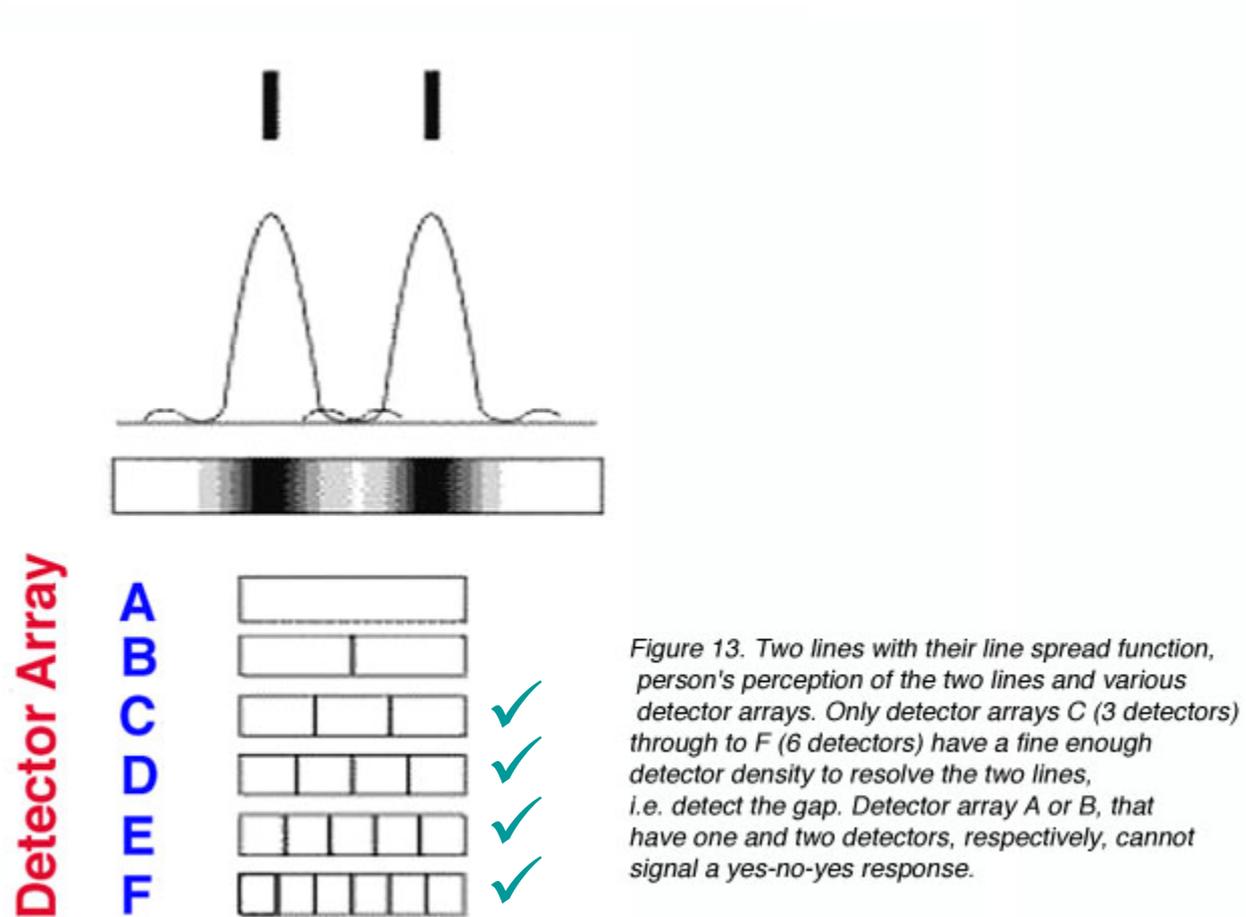
Stages

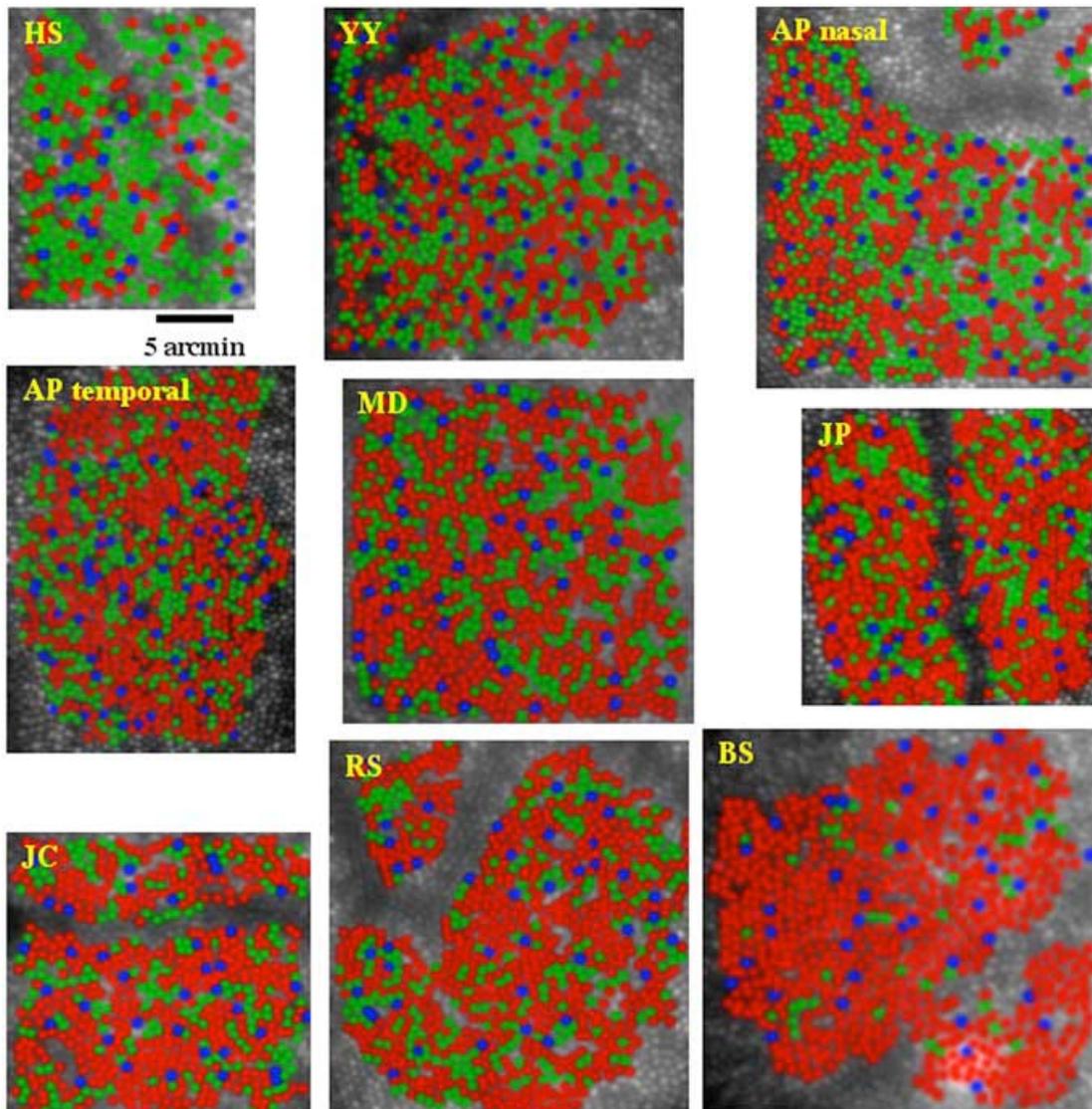


Stages



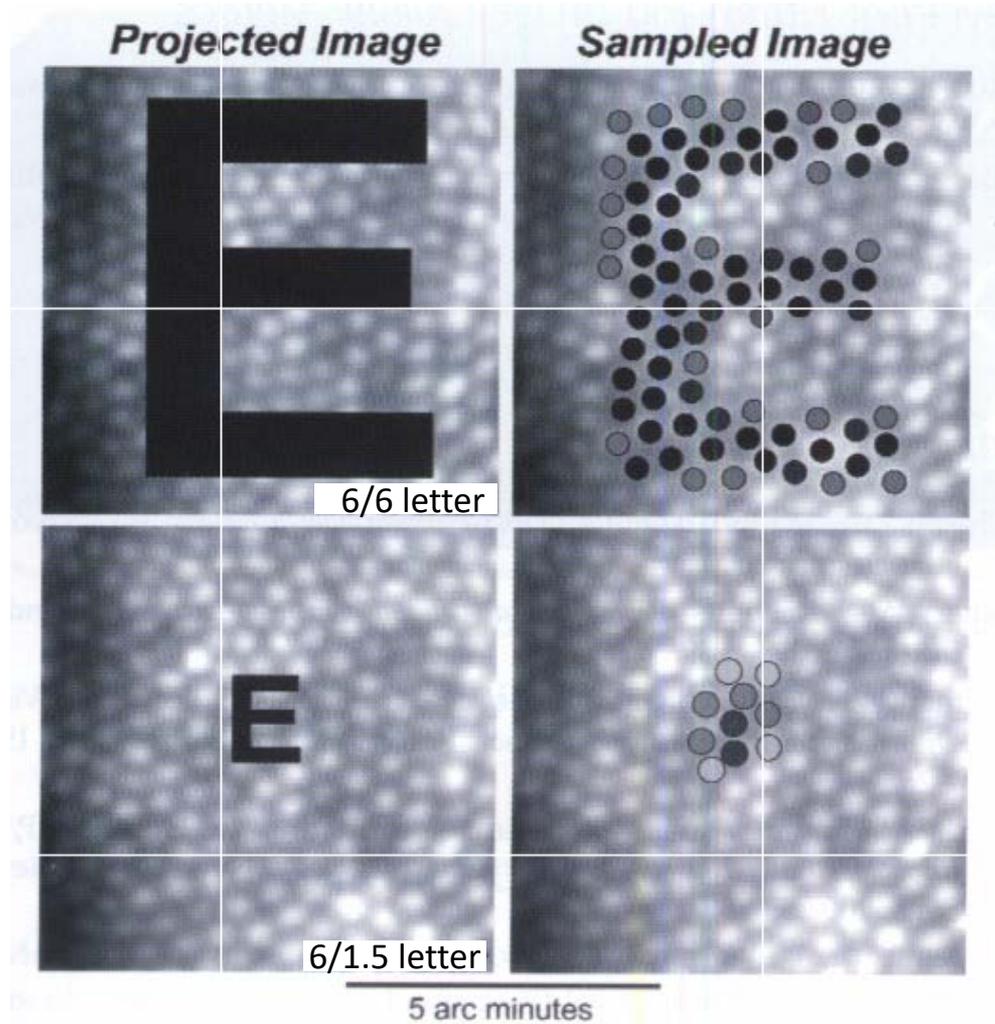
Retinal sampling





False color images showing the arrangement of L (red), M (green), and S (blue) cones in the retinas of different human subjects. All images are shown to the same scale.

Impact of sampling on letter visual acuity: Notice that the foveal sampling is perfectly adequate to represent a 6/6 (20/20) letter, but inadequate to represent a 6/1.5 (20/5) letter.



Human photoreceptors

Rods

- Achromatic night vision
- 1 type



Rod

Cones

- Daytime, achromatic *and* chromatic vision
- 3 types



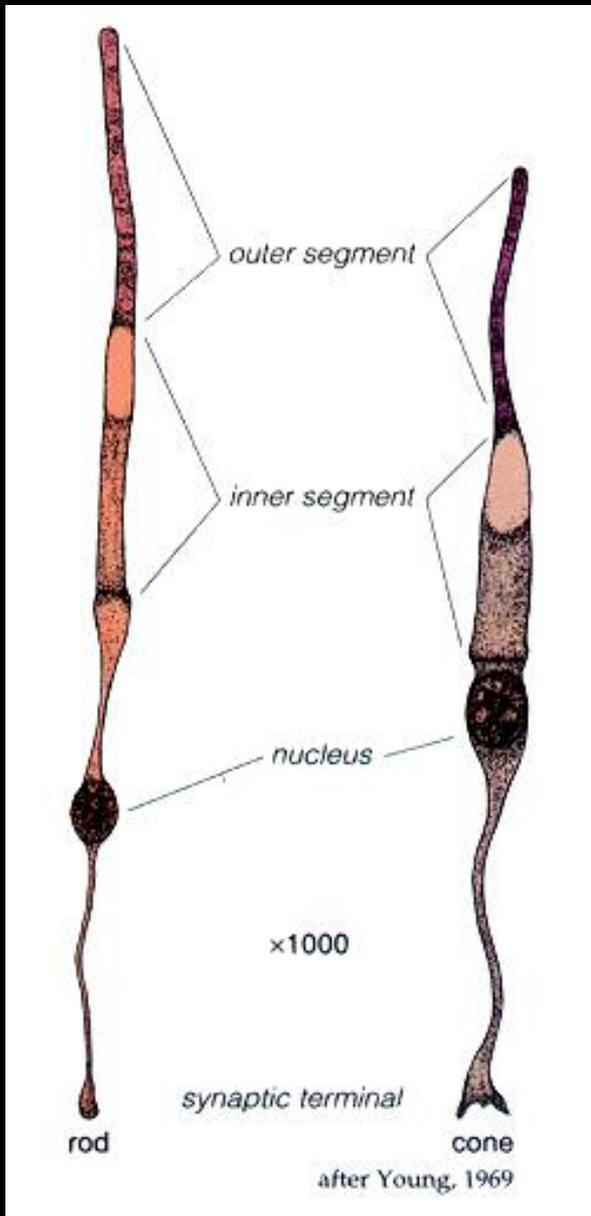
Long-wavelength-sensitive (L) or "red" cone



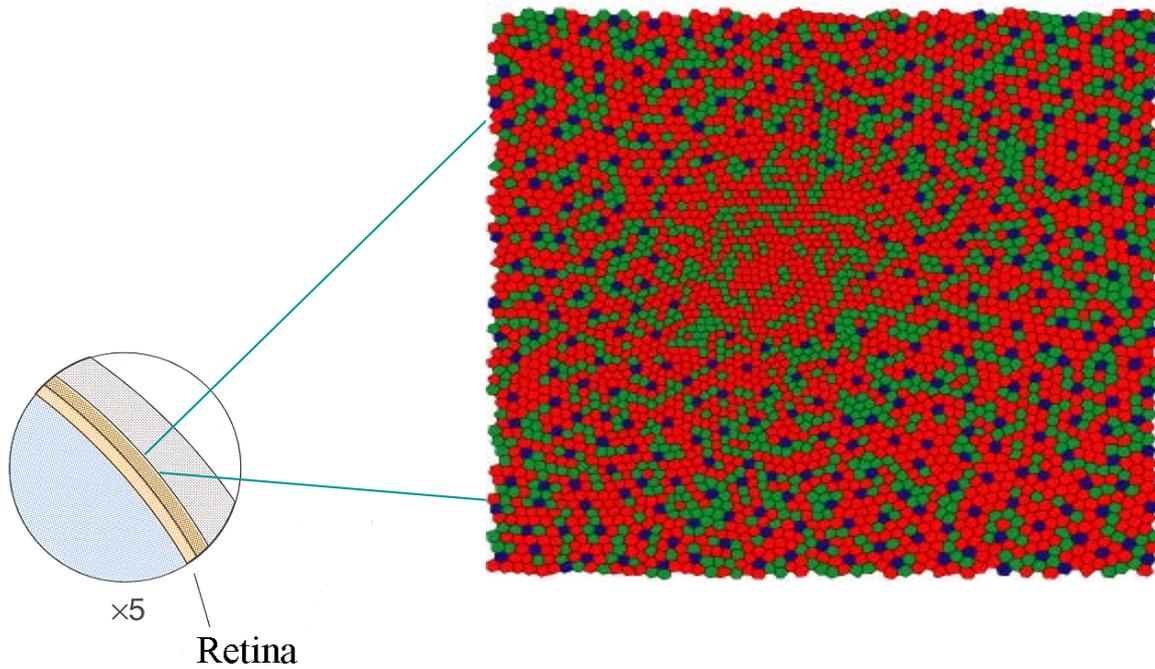
Middle-wavelength-sensitive (M) or "green" cone



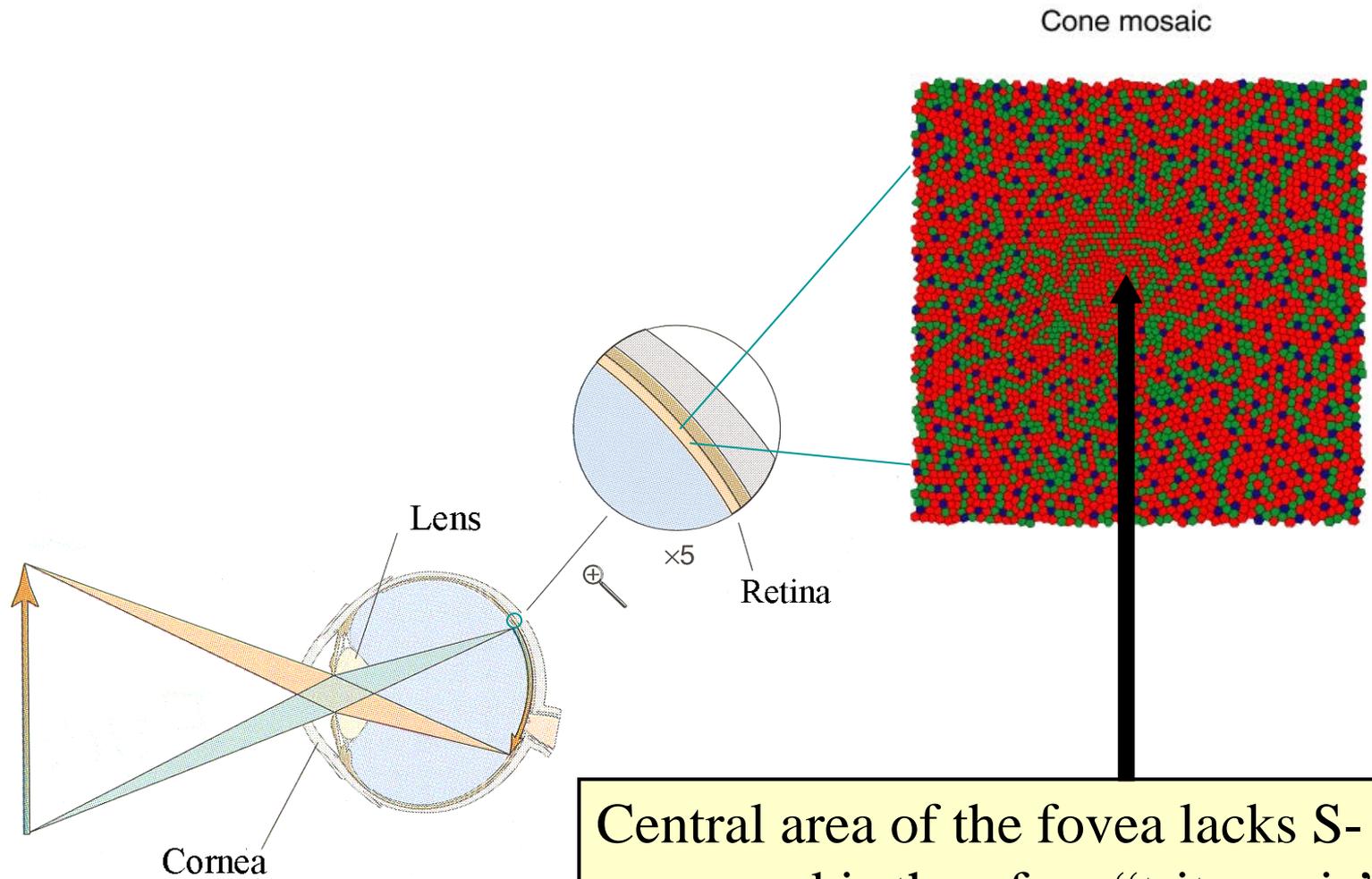
Short-wavelength-sensitive (S) or "blue" cone



Cone mosaic

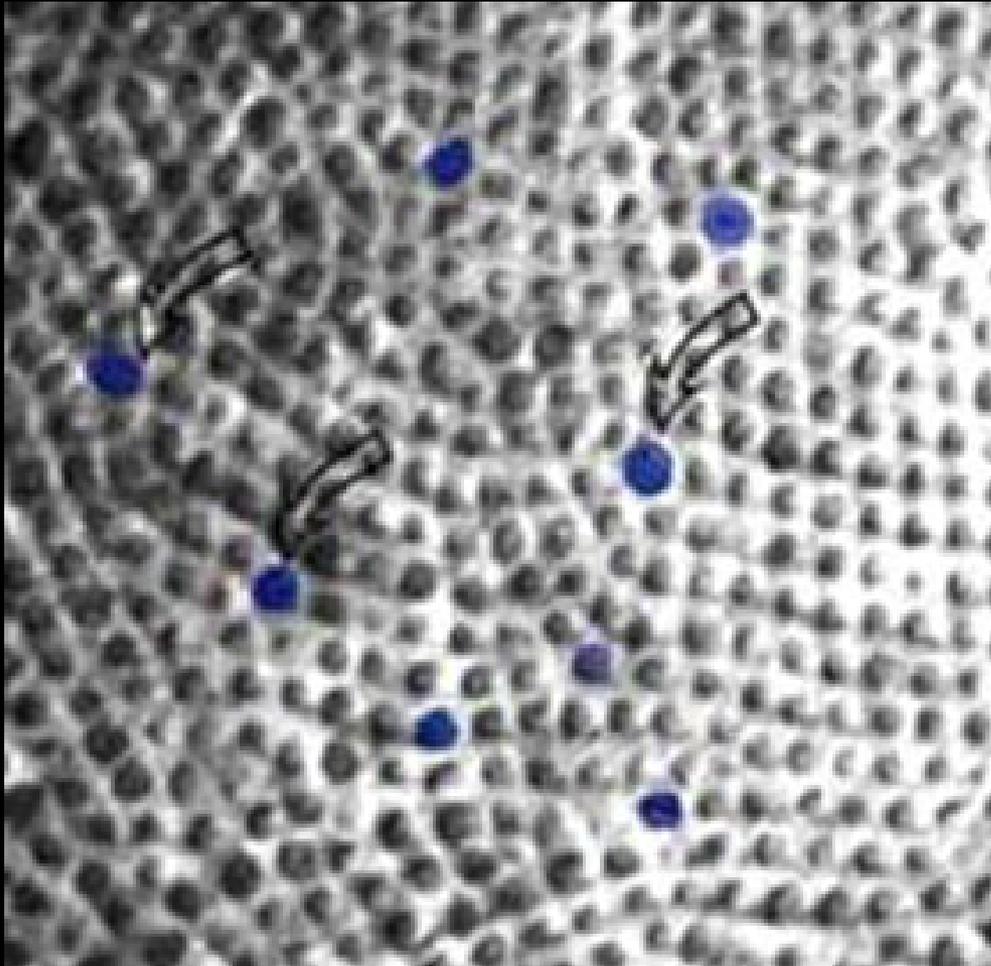


Central fovea is rod-free, and the very central foveola is rod- and S-cone free



Central area of the fovea lacks S-cones and is therefore “tritanopic”.

In other retinal regions, the S-cone mosaic remains sparse.

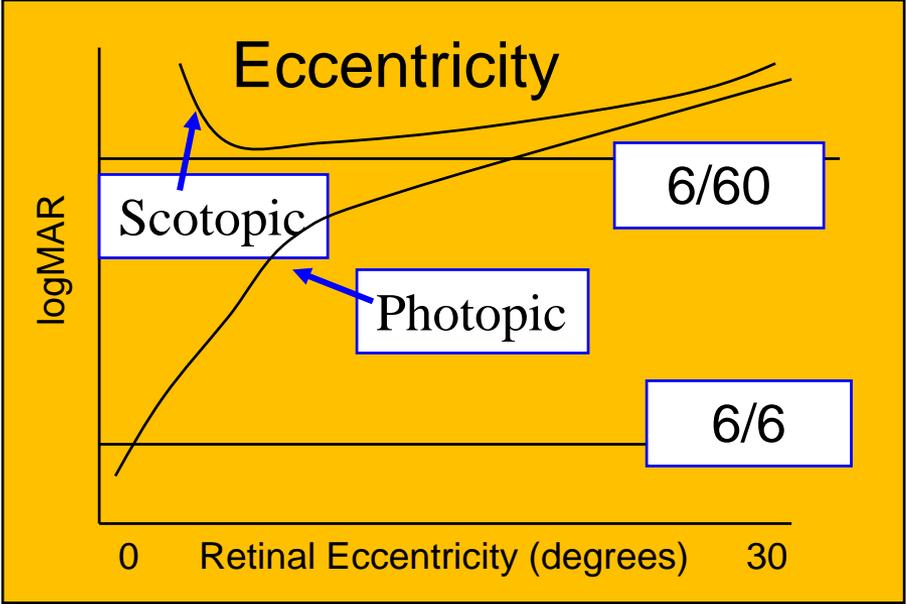


S-cones form
between 5 and
10% of the cone
population.

Small field tritanopia



Changes with eccentricity



Human photoreceptors

Rods

- Achromatic night vision
- 1 type



Rod

Cones

- Daytime, achromatic *and* chromatic vision
- 3 types



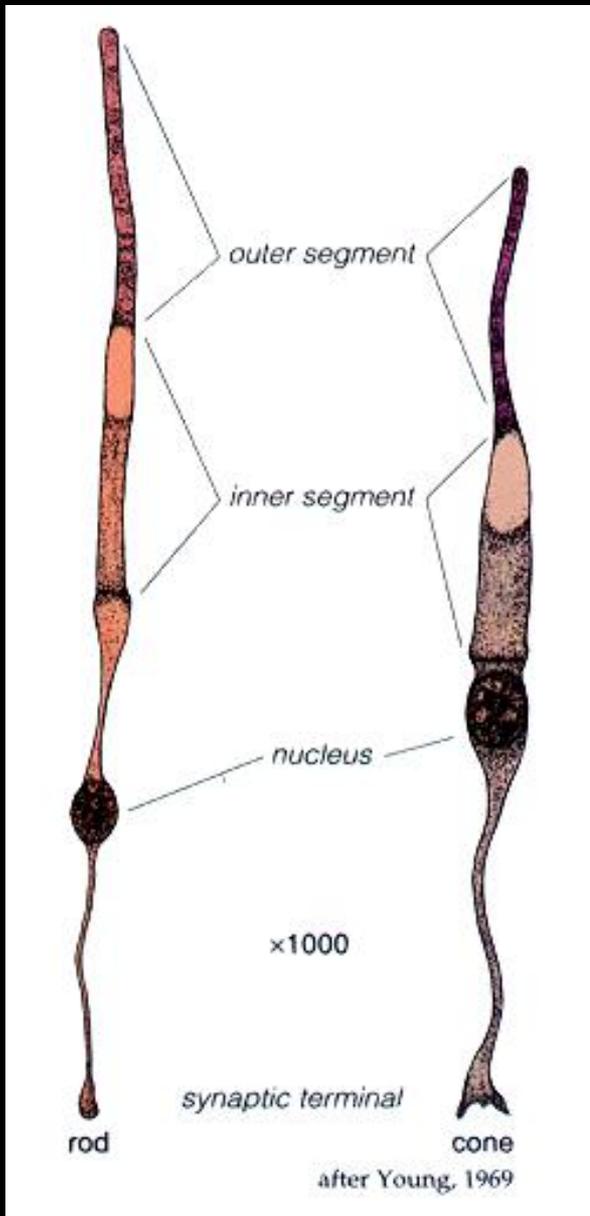
Long-wavelength-sensitive (L) or "red" cone



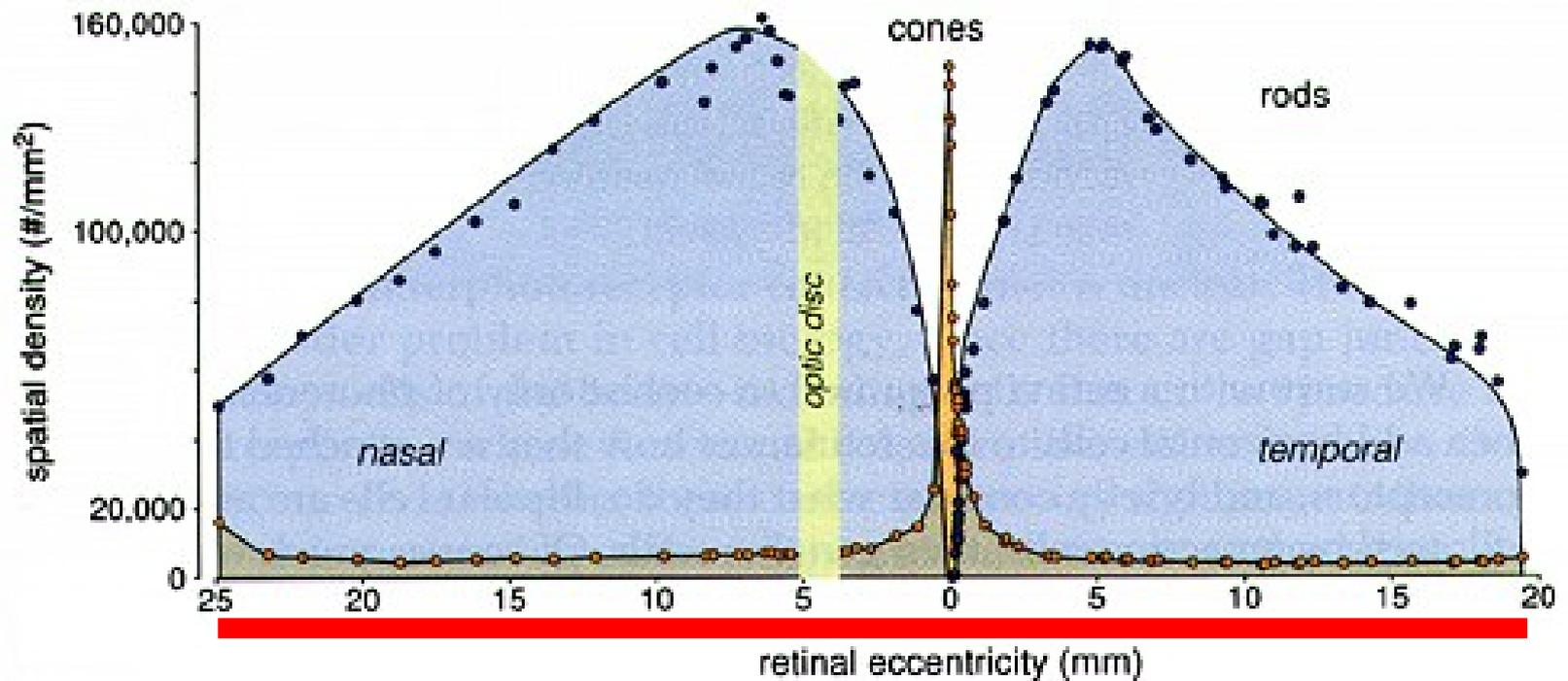
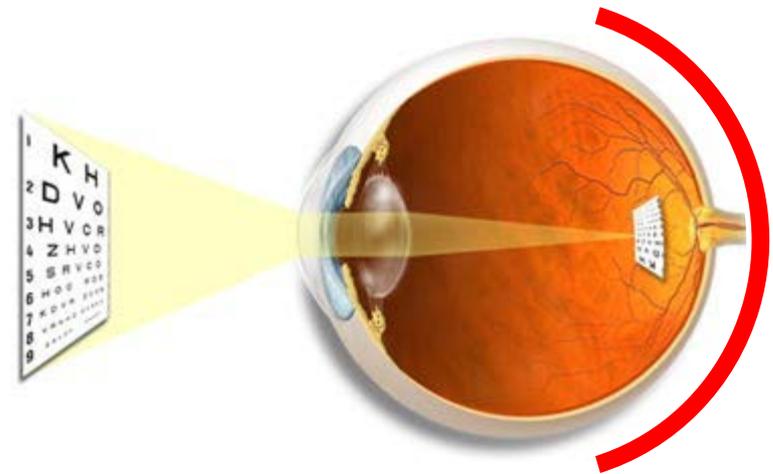
Middle-wavelength-sensitive (M) or "green" cone



Short-wavelength-sensitive (S) or "blue" cone



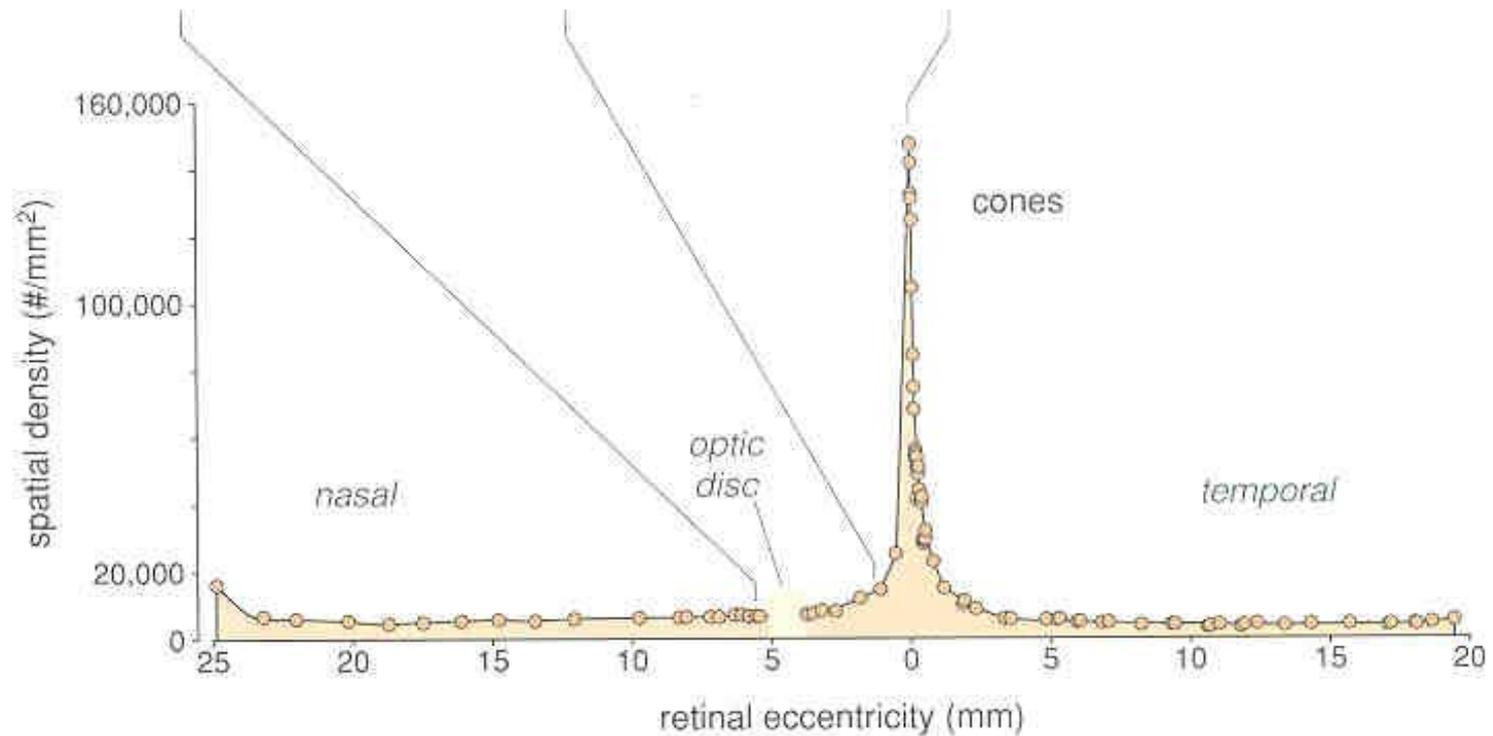
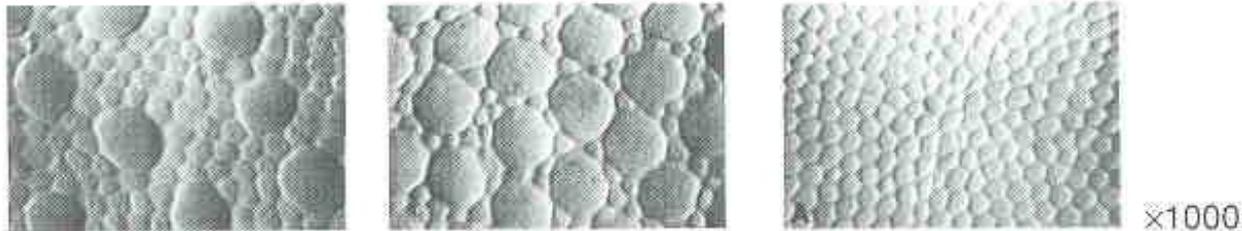
Rod and cone distribution



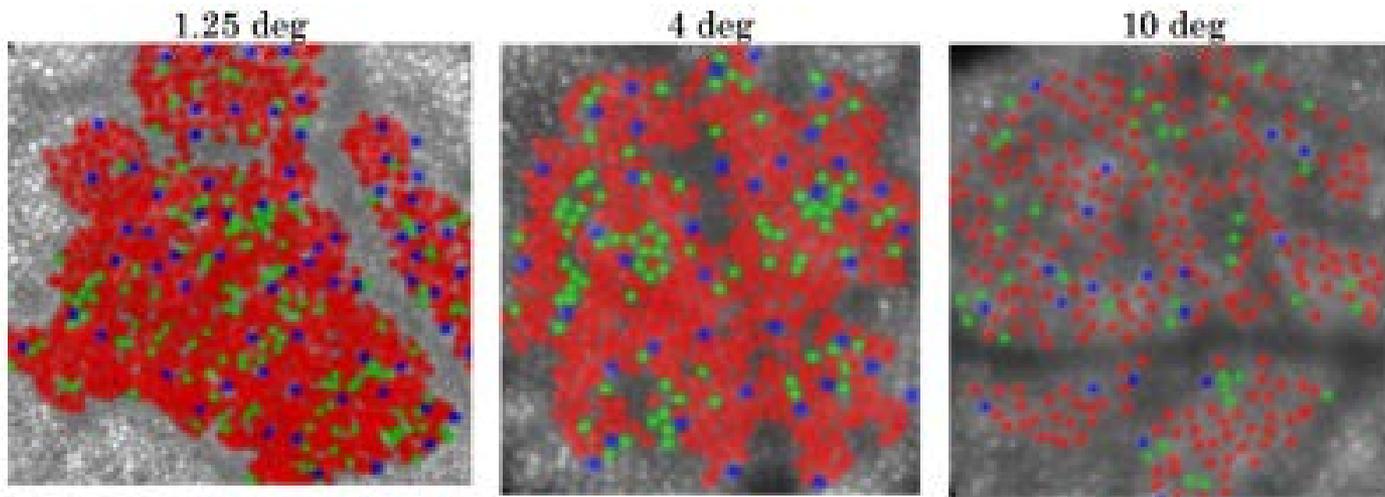
0.3 mm of eccentricity is about 1 deg of visual angle

after Österberg, 1935; as modified by Rodieck, 1988

Cone distribution and photoreceptor mosaics



after Østerberg, 1935; as modified by Rodieck 1988;
micrographs from Curcio et al., 1990



Primate retina

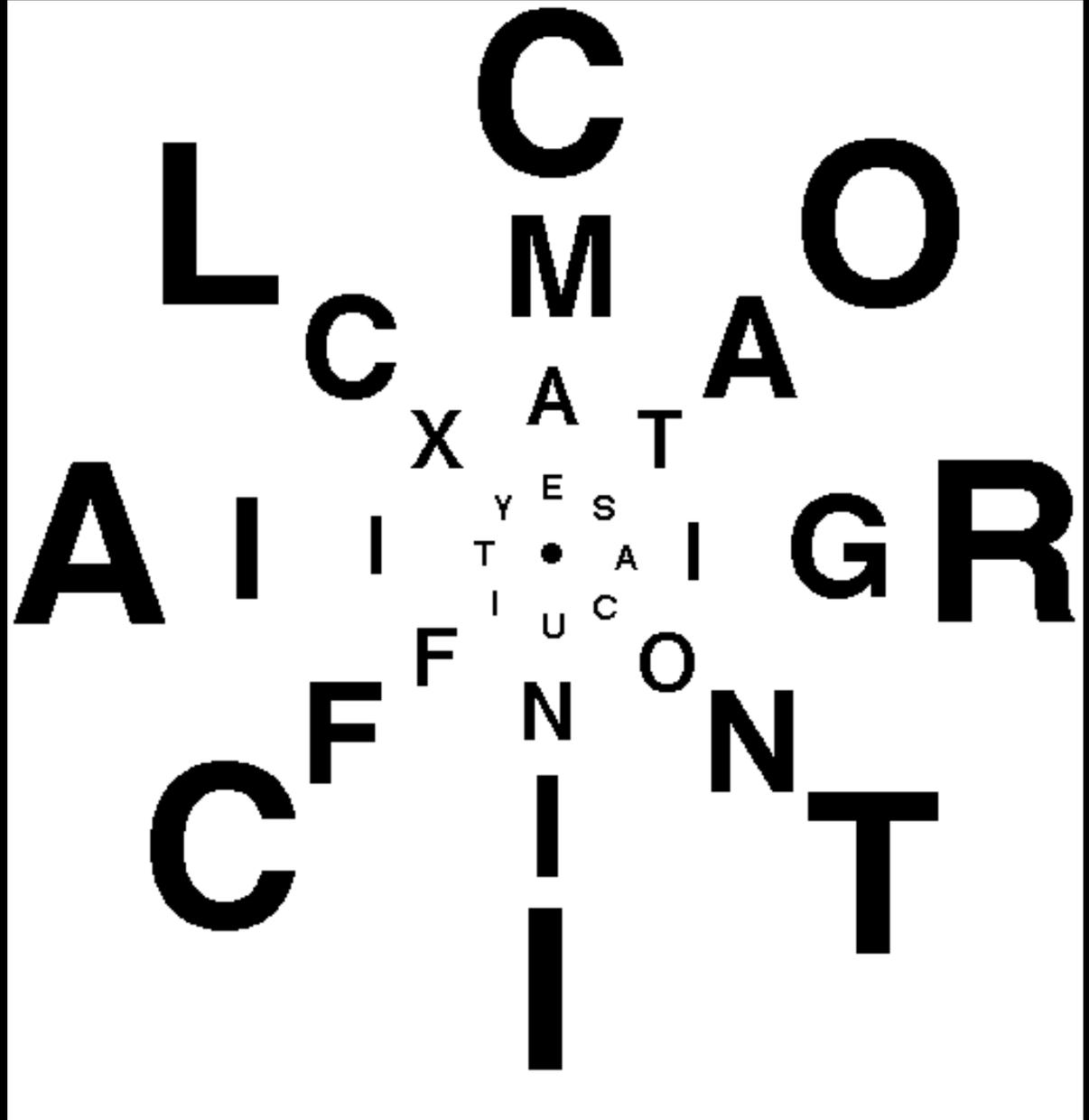
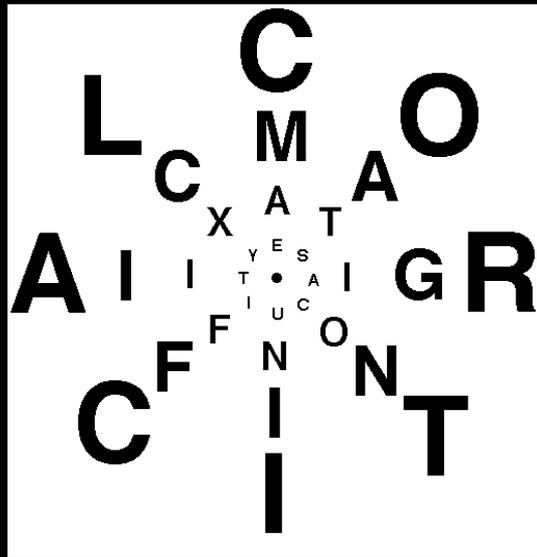
Original photograph



The human visual system is a foveating system

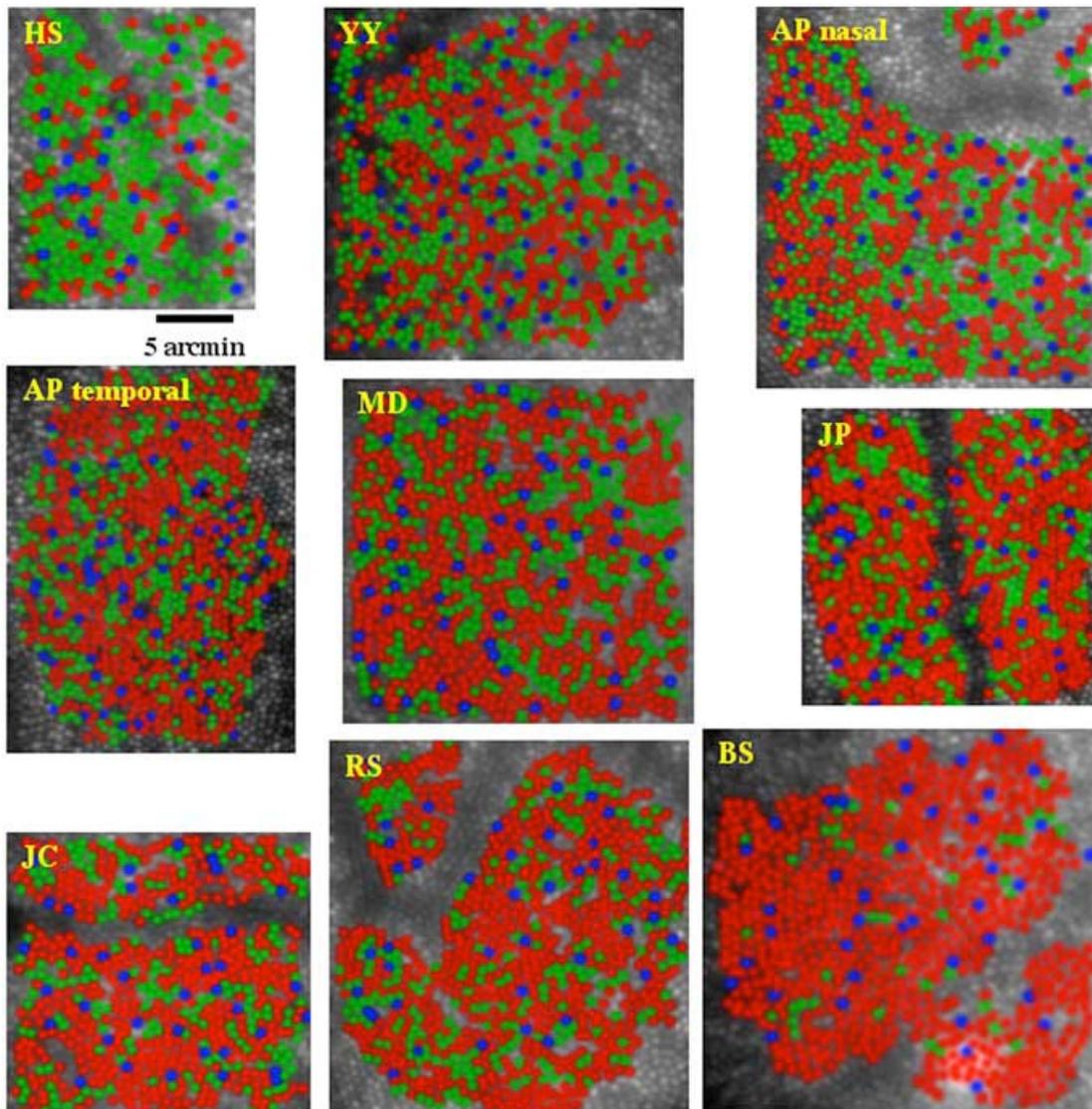
Simulation of what we see when
we fixate with cone vision.





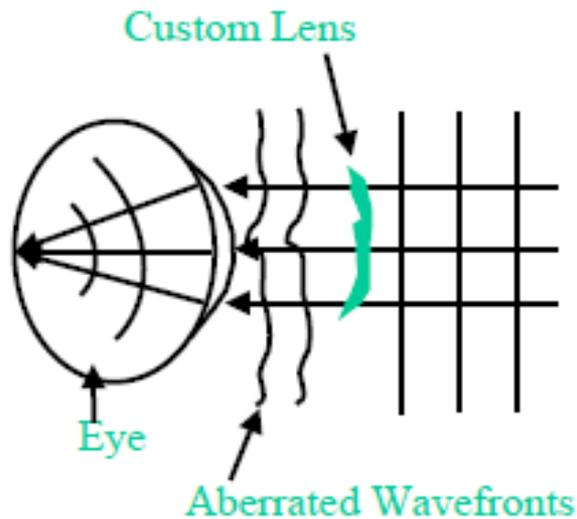
Visual acuity gets much poorer with eccentricity

Adaptive optics: viewing the
retina through the eye's optics



False color images showing the arrangement of L (red), M (green), and S (blue) cones in the retinas of different human subjects. All images are shown to the same scale.

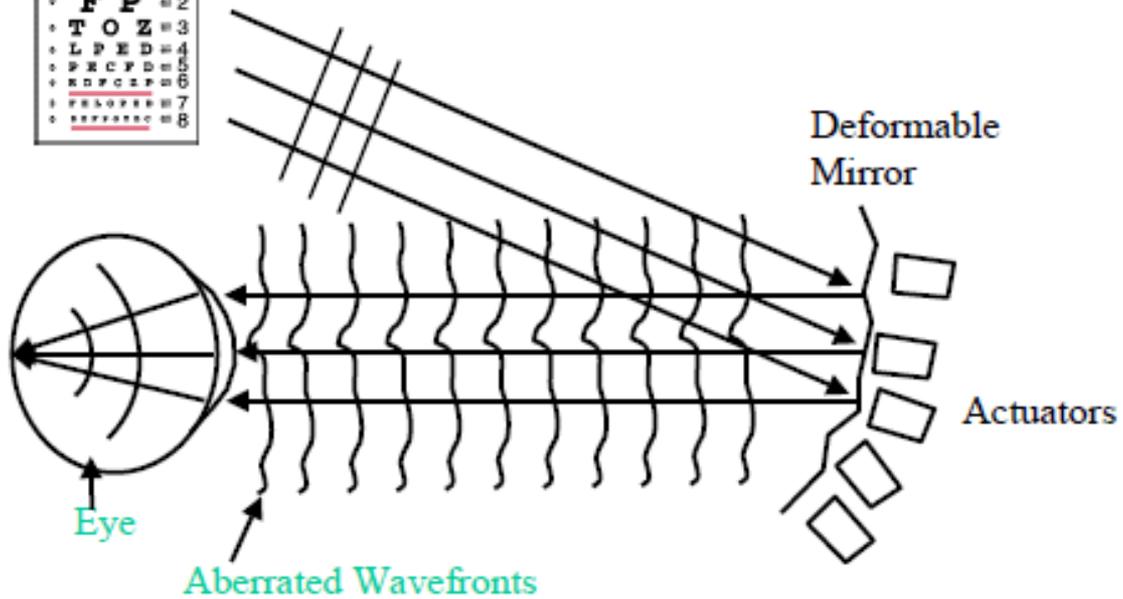
Diffraction-Limited Eye



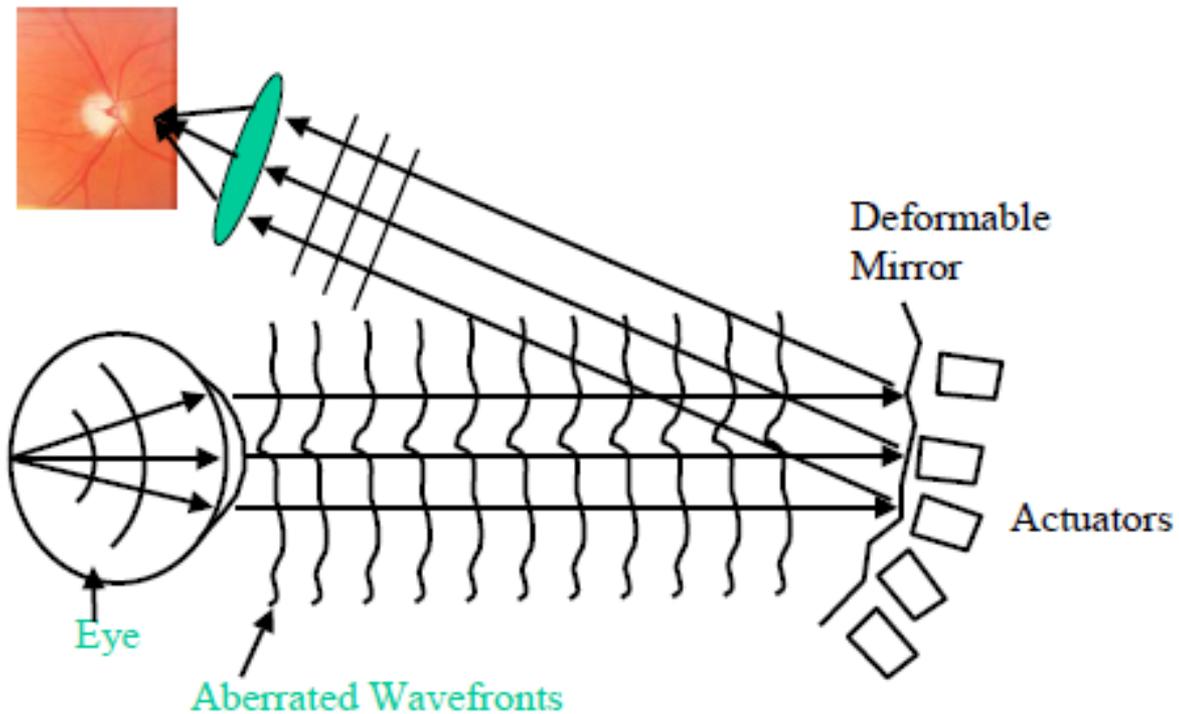
Knowledge of the aberration of the eye allows us to calculate a custom lens, which will compensate for the aberrations of the eye and form a diffraction-limited image on the retina. The results are improved visual acuity and contrast sensitivity.

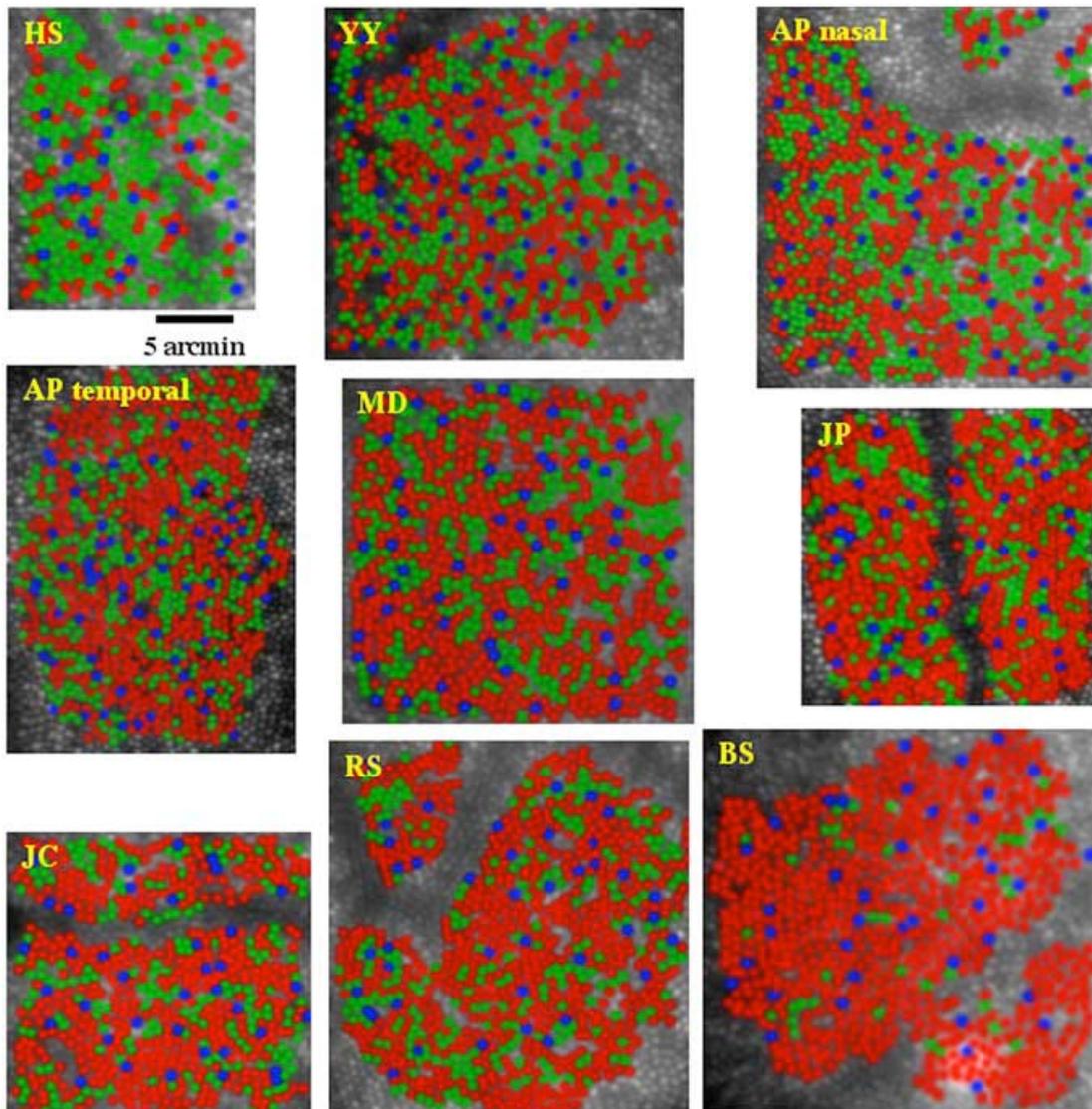
Improvements to Visual Performance

• E	= 1
• F P	= 2
• T O Z	= 3
• L P E D	= 4
• P R C F D	= 5
• K D F C Z F	= 6
• P L O O P P	= 7
• P P P P P P C	= 8

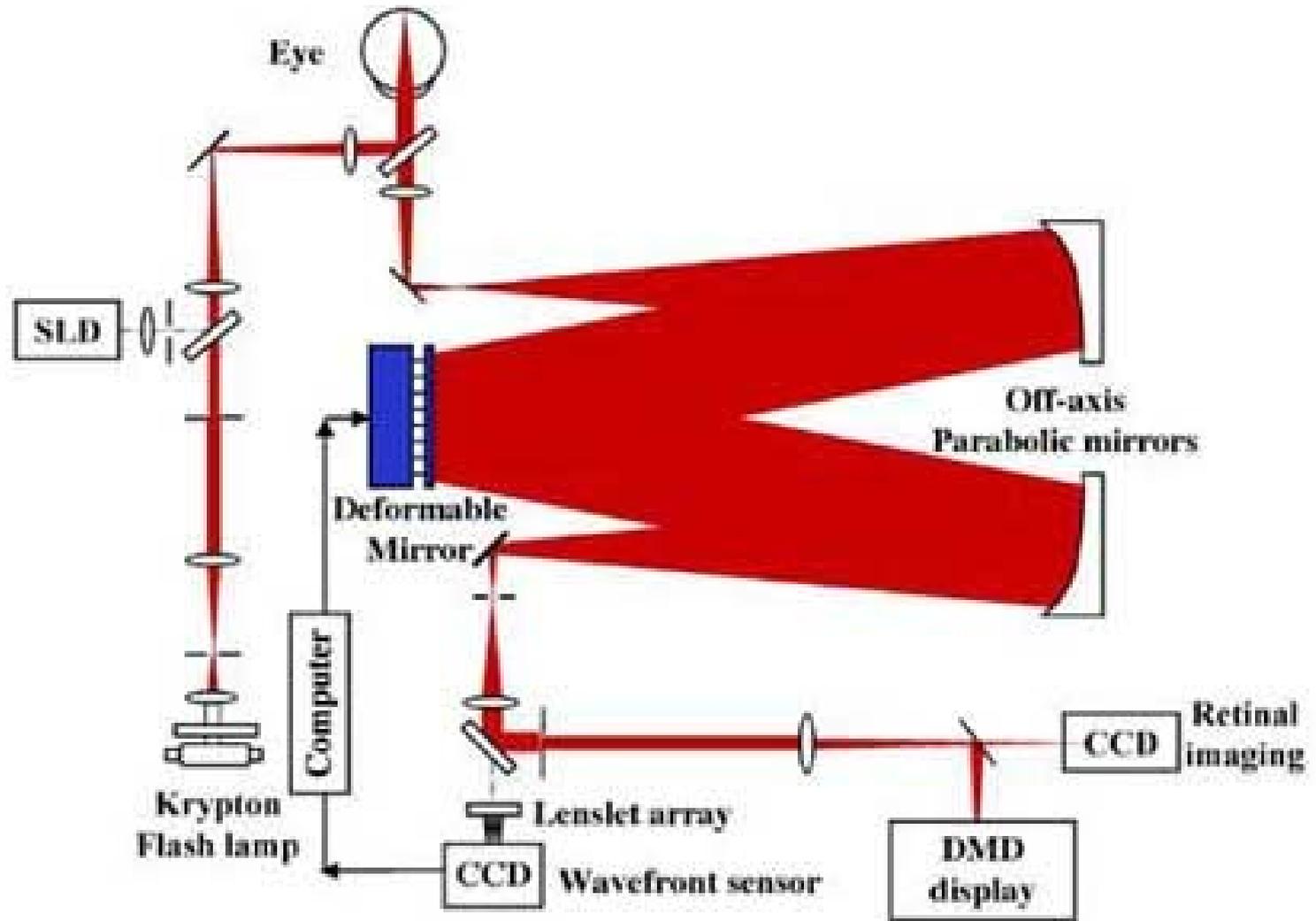


Improvements to Retinal Imaging

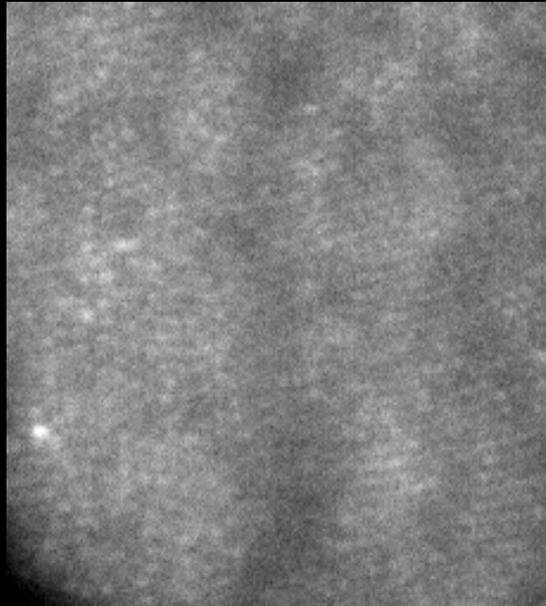




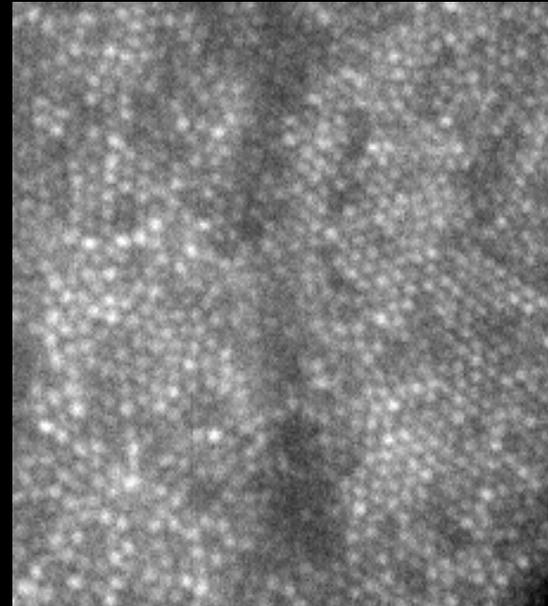
False color images showing the arrangement of L (red), M (green), and S (blue) cones in the retinas of different human subjects. All images are shown to the same scale.



Uncorrected



Corrected



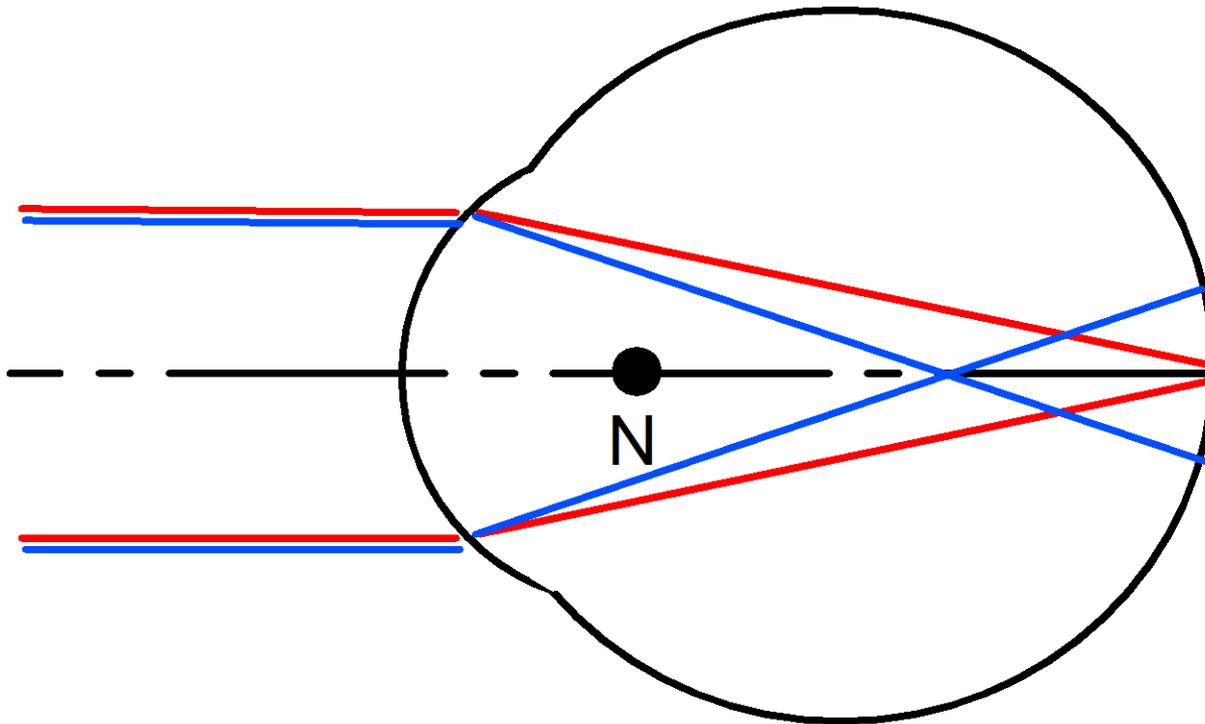
10 arc min

Photos courtesy of A. Roorda, D. Williams, U. Rochester

Chromatic aberrations

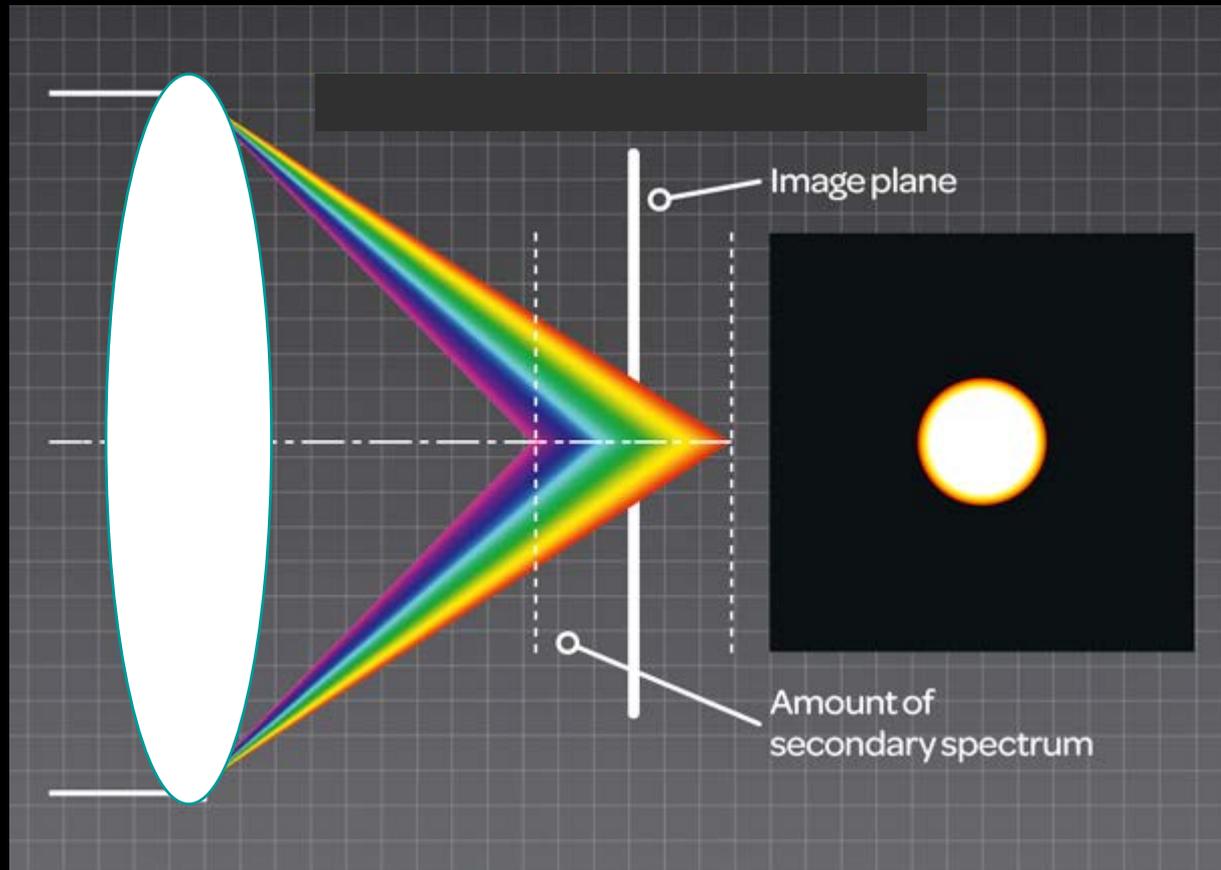
Chromatic aberration

The focusing power of the eye varies with wavelength.



This phenomenon is called longitudinal (or axial) chromatic aberration (LCA)

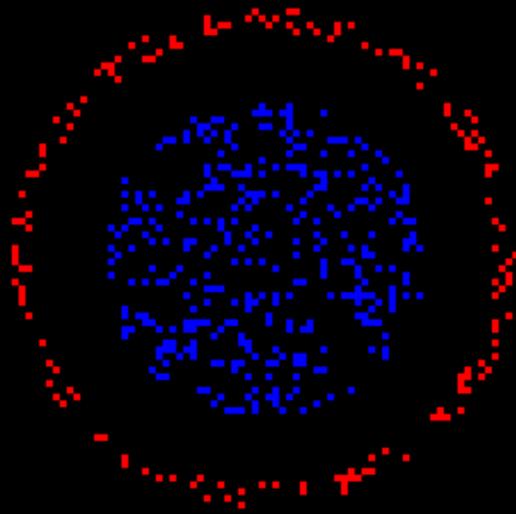
Chromatic aberration



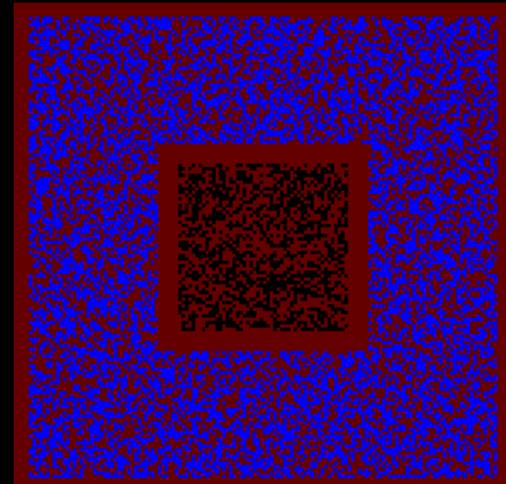
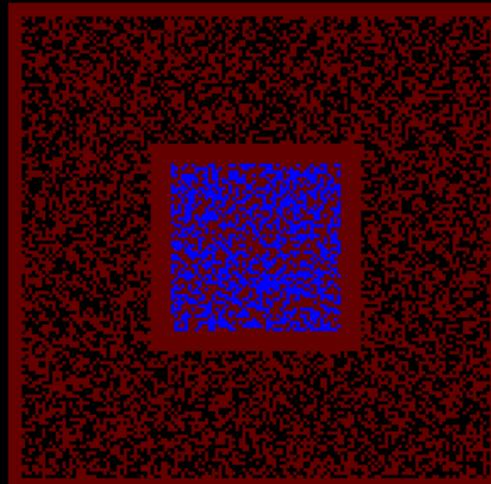
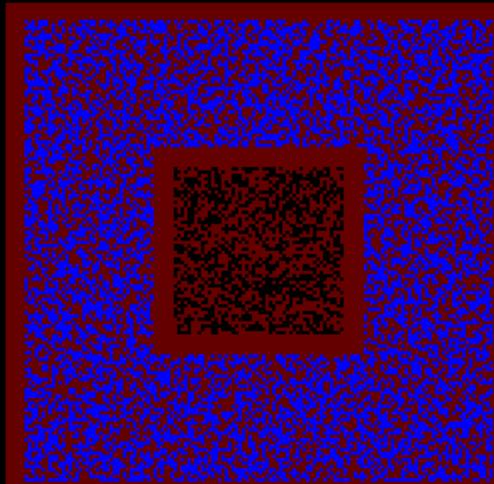
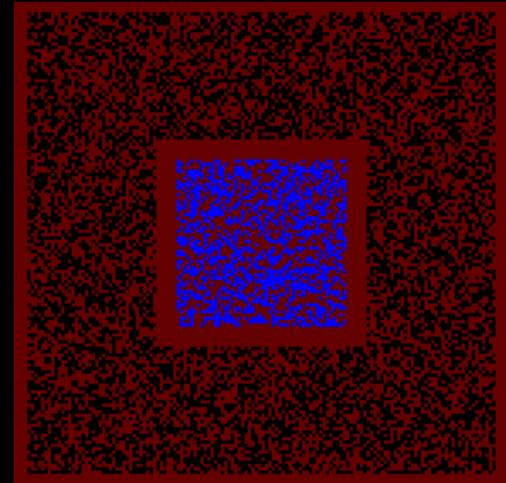
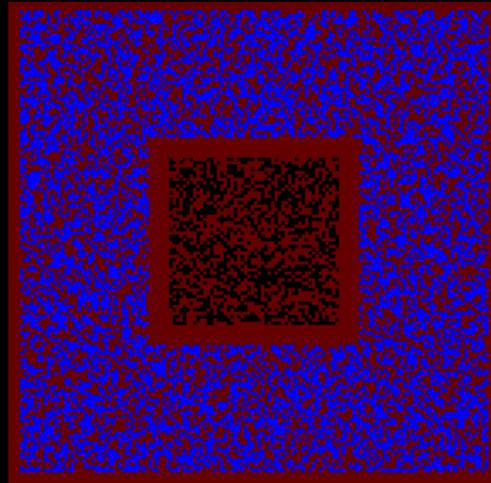
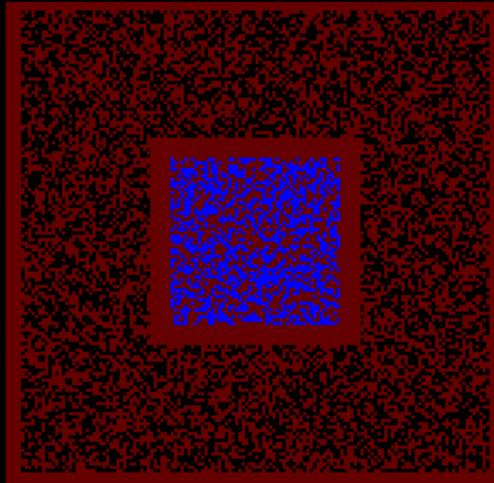
Base picture: Digital camera world

Effect of chromatic blur on eye chart





Chromostereoscopic windows



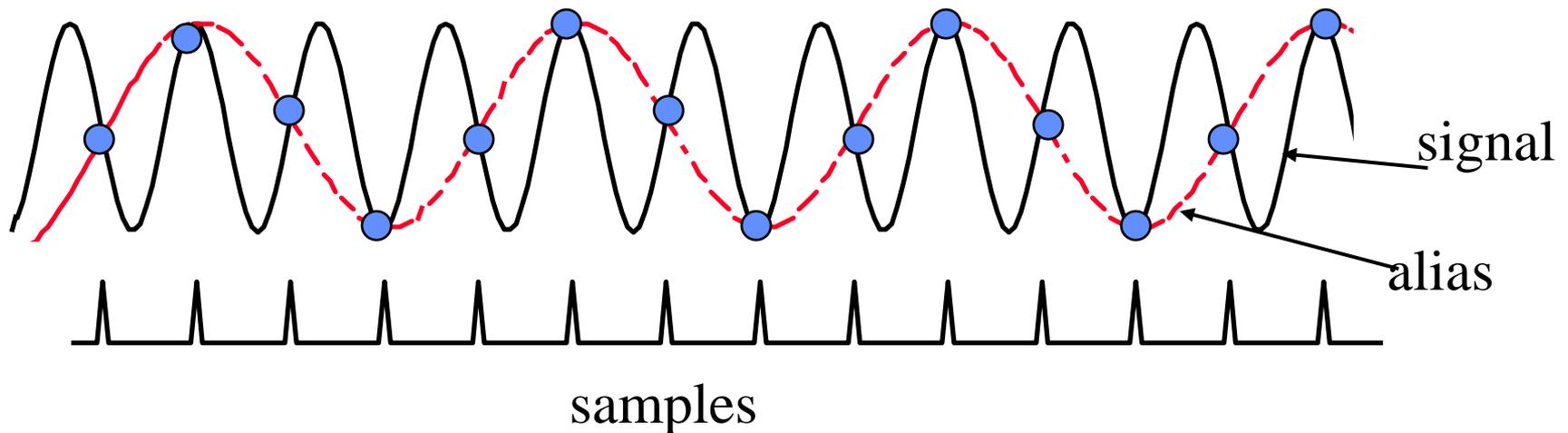
EXTRA SLIDES (not presented)

Why visual acuity should be limited by the optics and sampling

Undersampling and Aliases

Repetitive Grating Stimulus

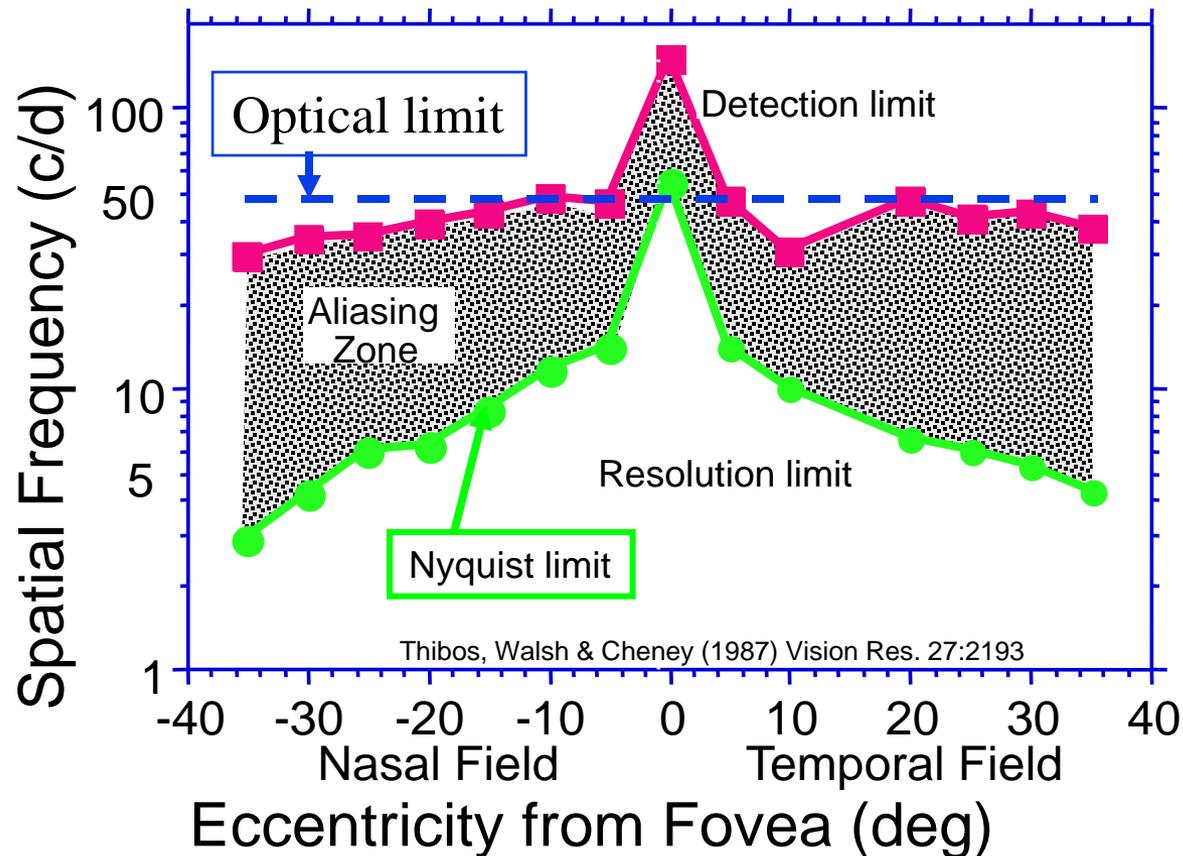
If there are **less than 2 samples per period** of a repetitive signal, it will be **undersampled** by the array, and the resulting output will be indistinguishable from a lower frequency signal.



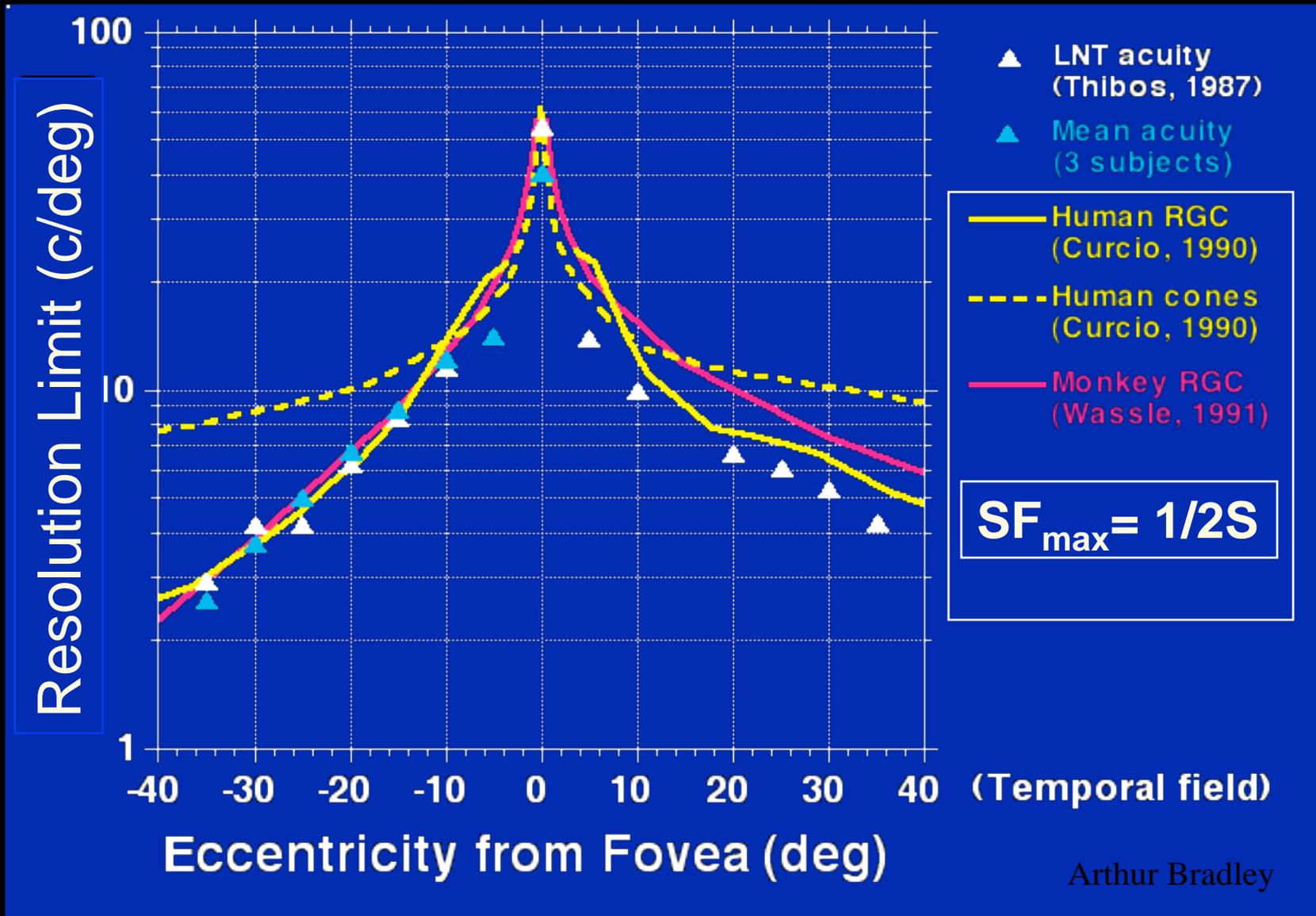
For resolution: sample separation(s) must be $\leq \text{period}/2$.

For human fovea: cones separated by $1/2$ arc minute, thus minimum resolvable period is 1 minute, or 60 c/deg. Above 60 c/deg, see aliases if these high frequencies existed in retinal image.

The eye's optics filters out all SF above Nyquist limit in fovea, since foveal nyquist (60 c/deg) is slightly higher than optical cut-off (about 50 c/deg). This is not so in the peripheral retina where the optical cut-off is higher than the nyquist limit, thus aliases can be seen.

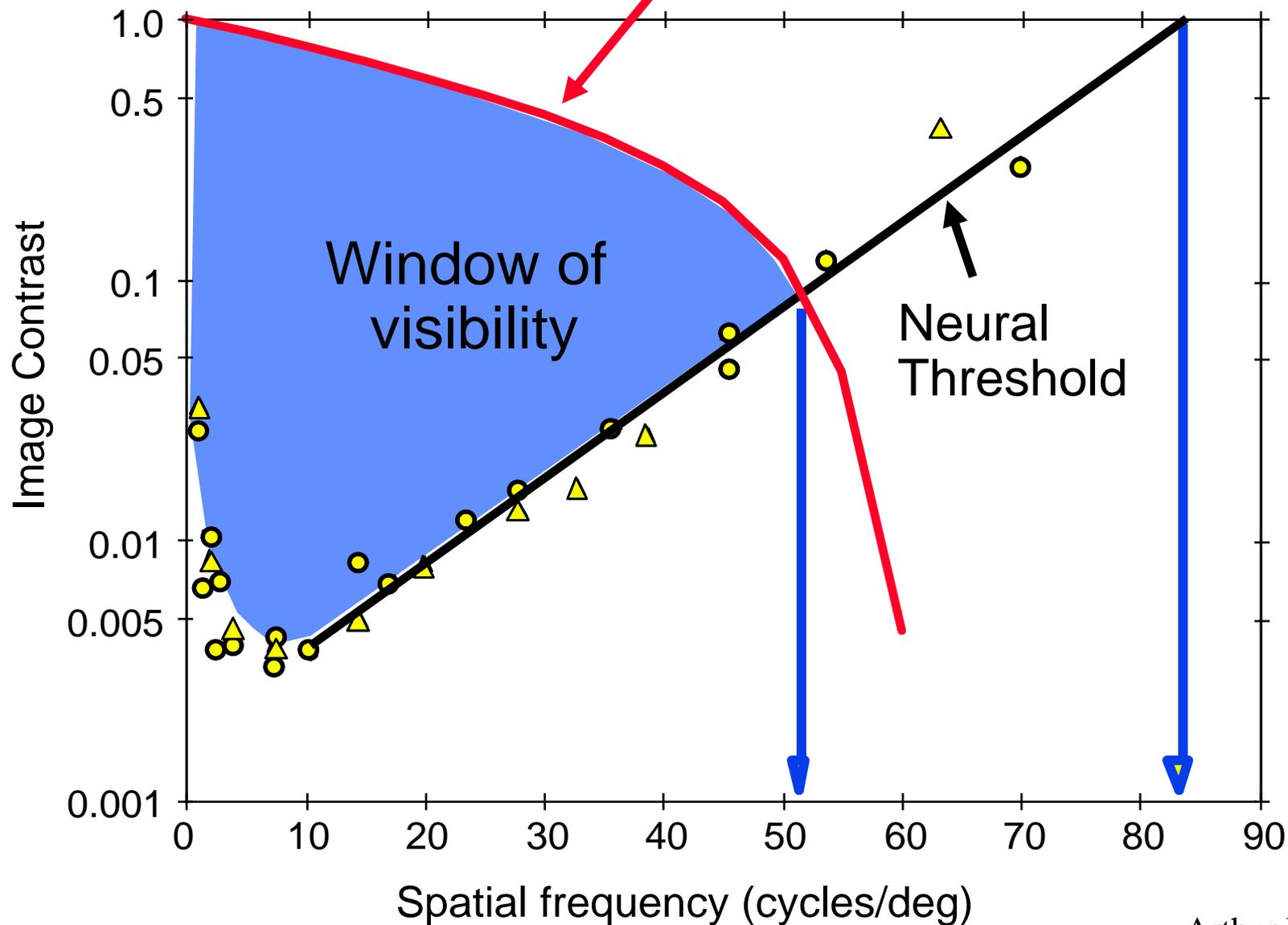


Human peripheral resolution acuity matches RGC sampling density predictions



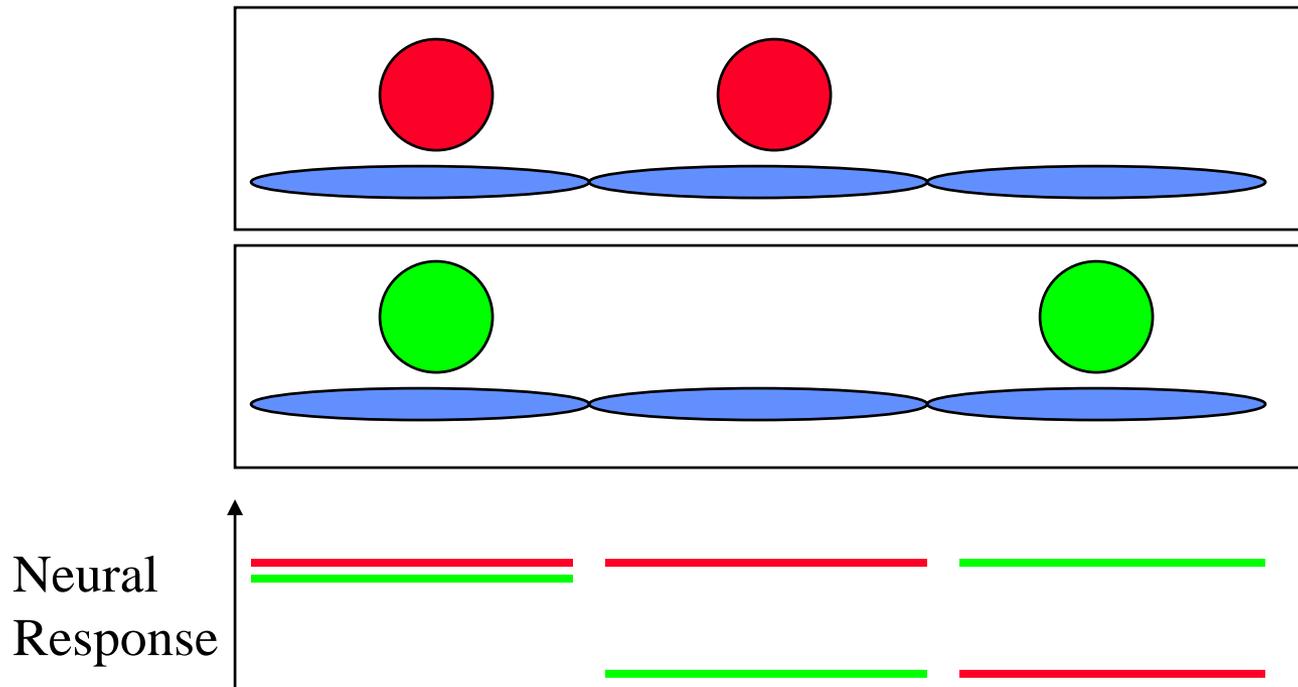
Foveal VA and CS are both limited by optical and neural factors

Optical Transfer Function



Impact of sampling on spatial resolution: Helmholtz

Two point Resolution:

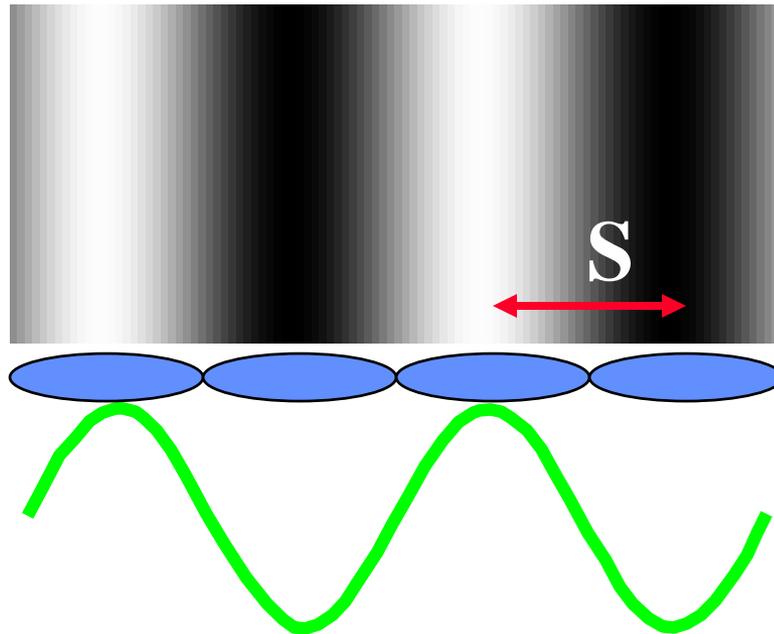


Must have sample between images of two points in order to know that there is a gap between the stimuli and thus be able to identify two points as two.

Sampling and periodic patterns.

Shannon's sampling theorem: basically same idea as Helmholtz (need one sample between each line)

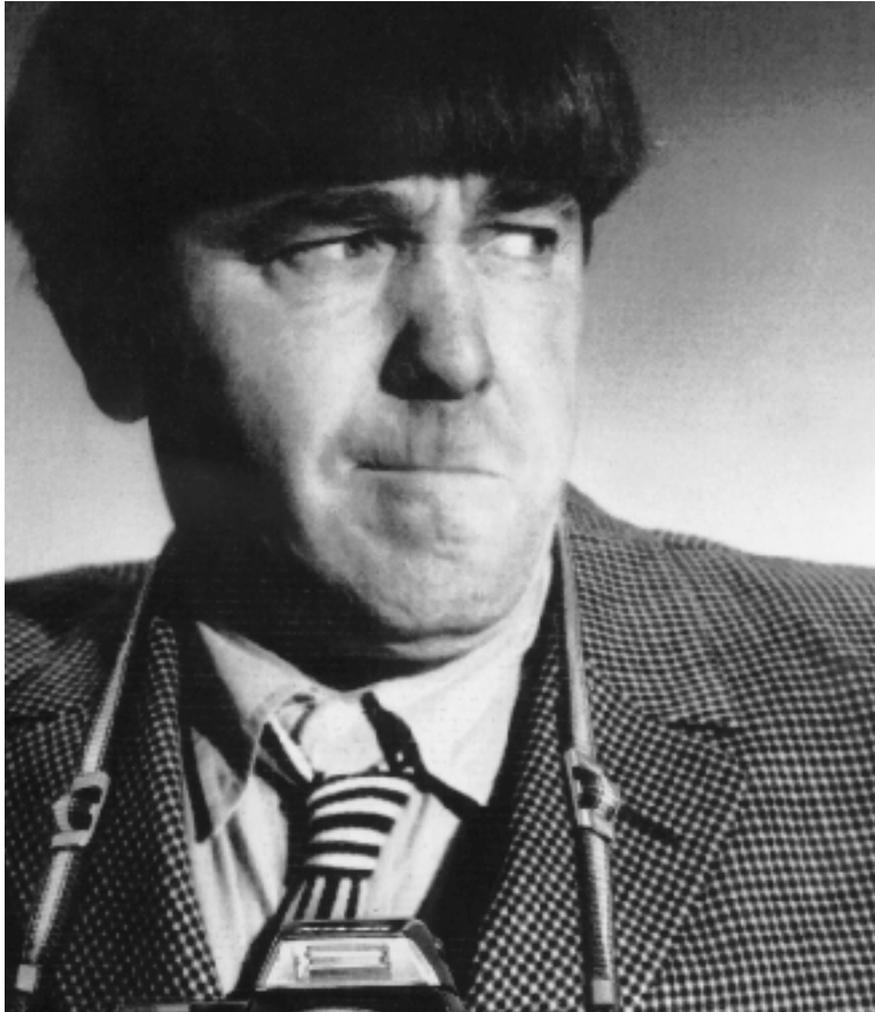
Notice that, at limit of just one sample between each bright line of grating, there will be exactly 2 samples per period of the grating.



In order to resolve a periodic pattern there must be at least 2 samples per period. Therefore, if we know the spacing between samples, we know the maximum resolvable spatial frequency = $f_{\max} = 1/(2s)$, where s = separation between samples.

Miscellaneous

What limits resolution acuity?

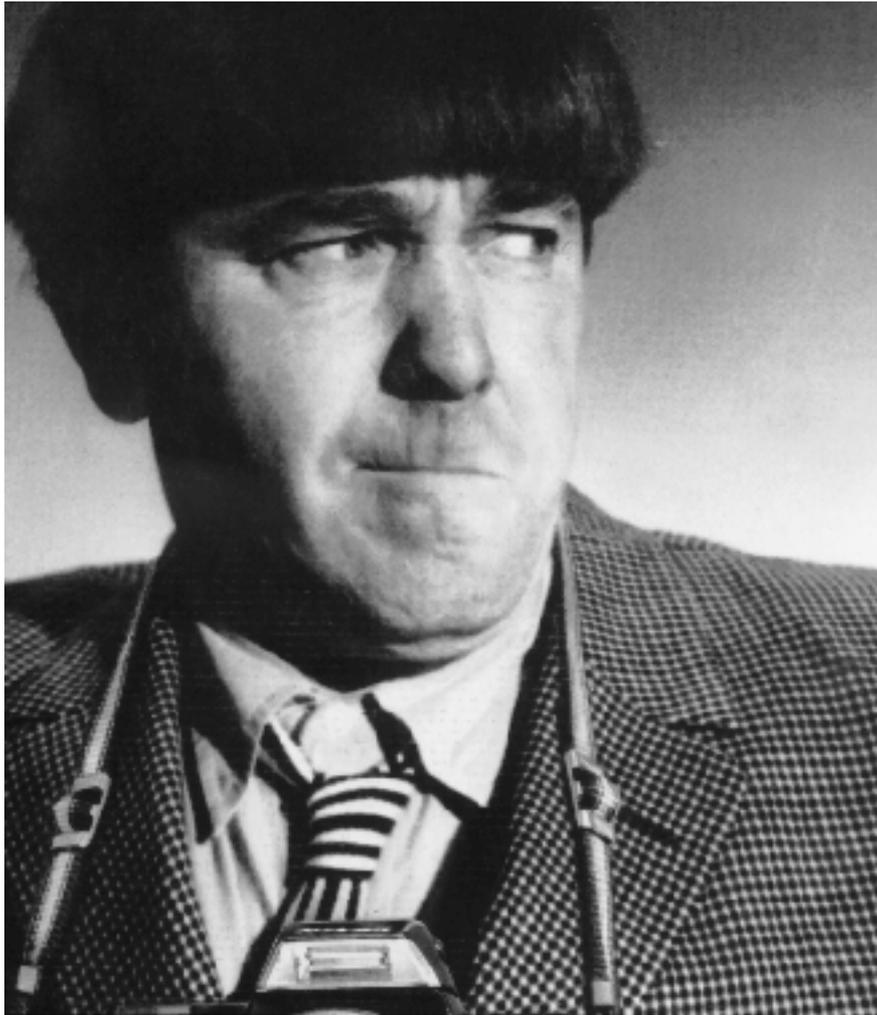


Two candidate mechanisms:

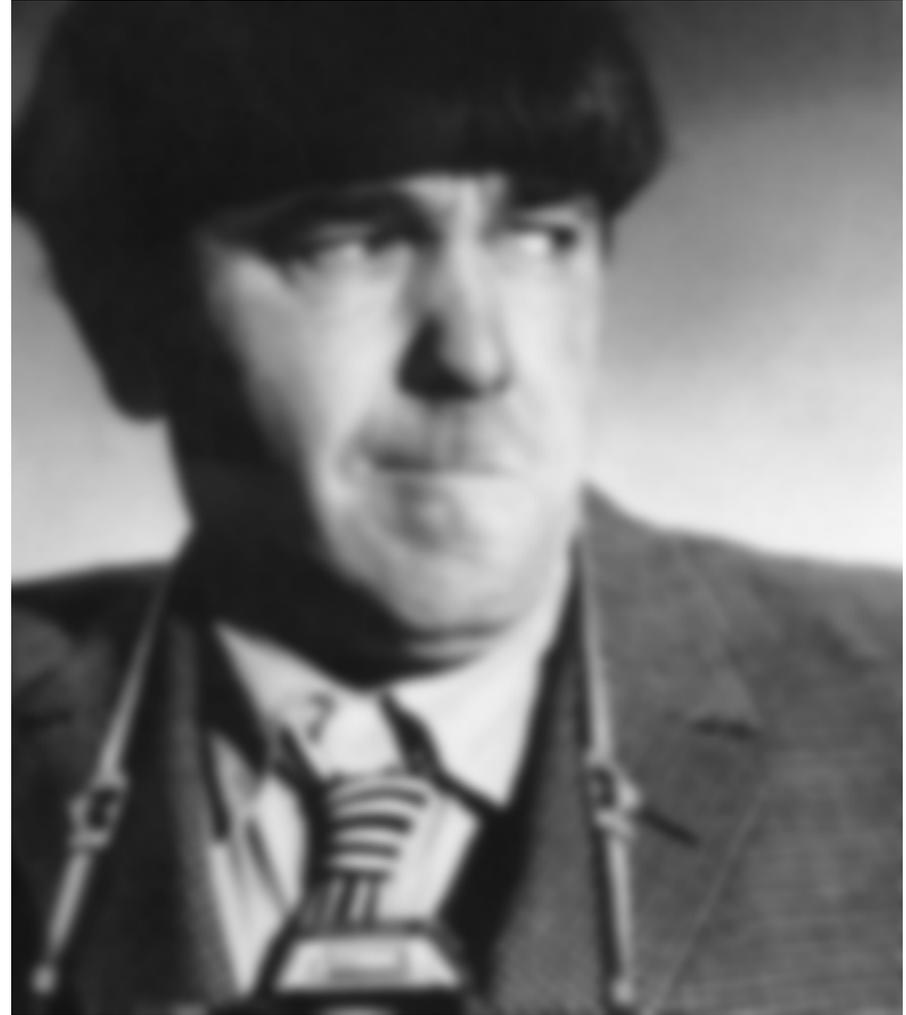
- filtering (optical or neural)
- undersampling

Filtering Limit to Visual Resolution

Original



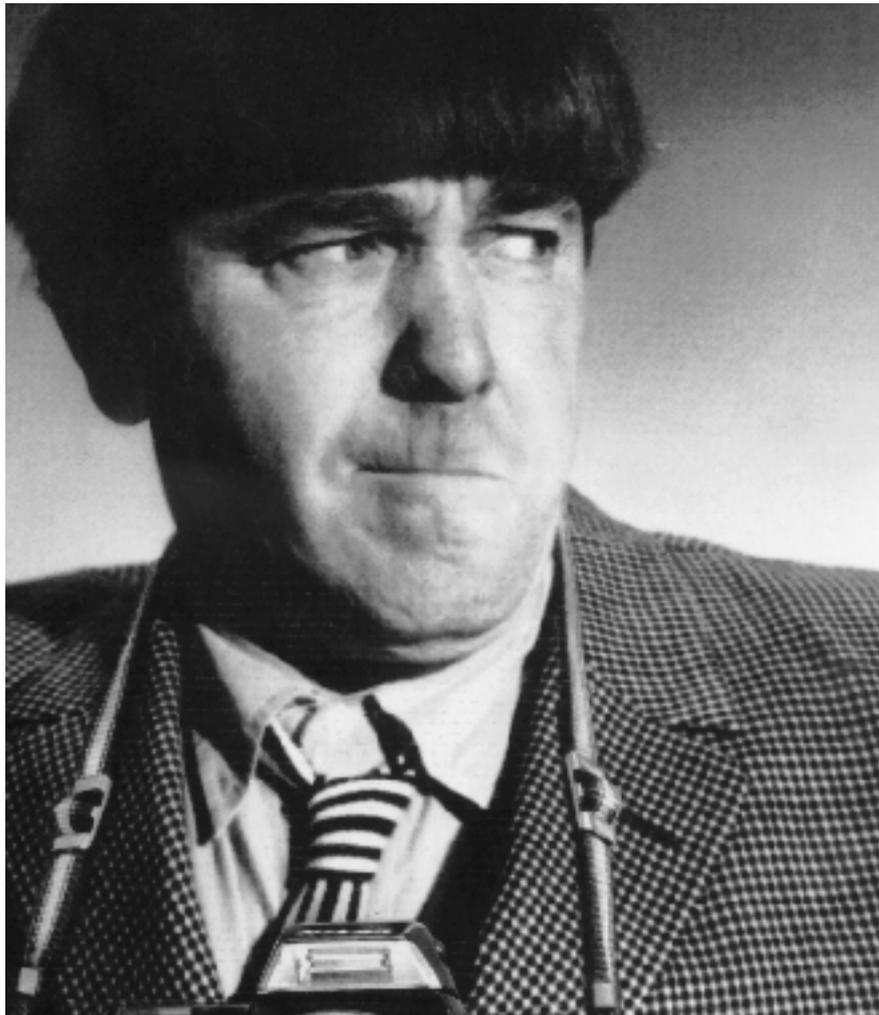
Low-pass Filtered



Arthur Bradley

Sampling Limit to Visual Resolution

Original

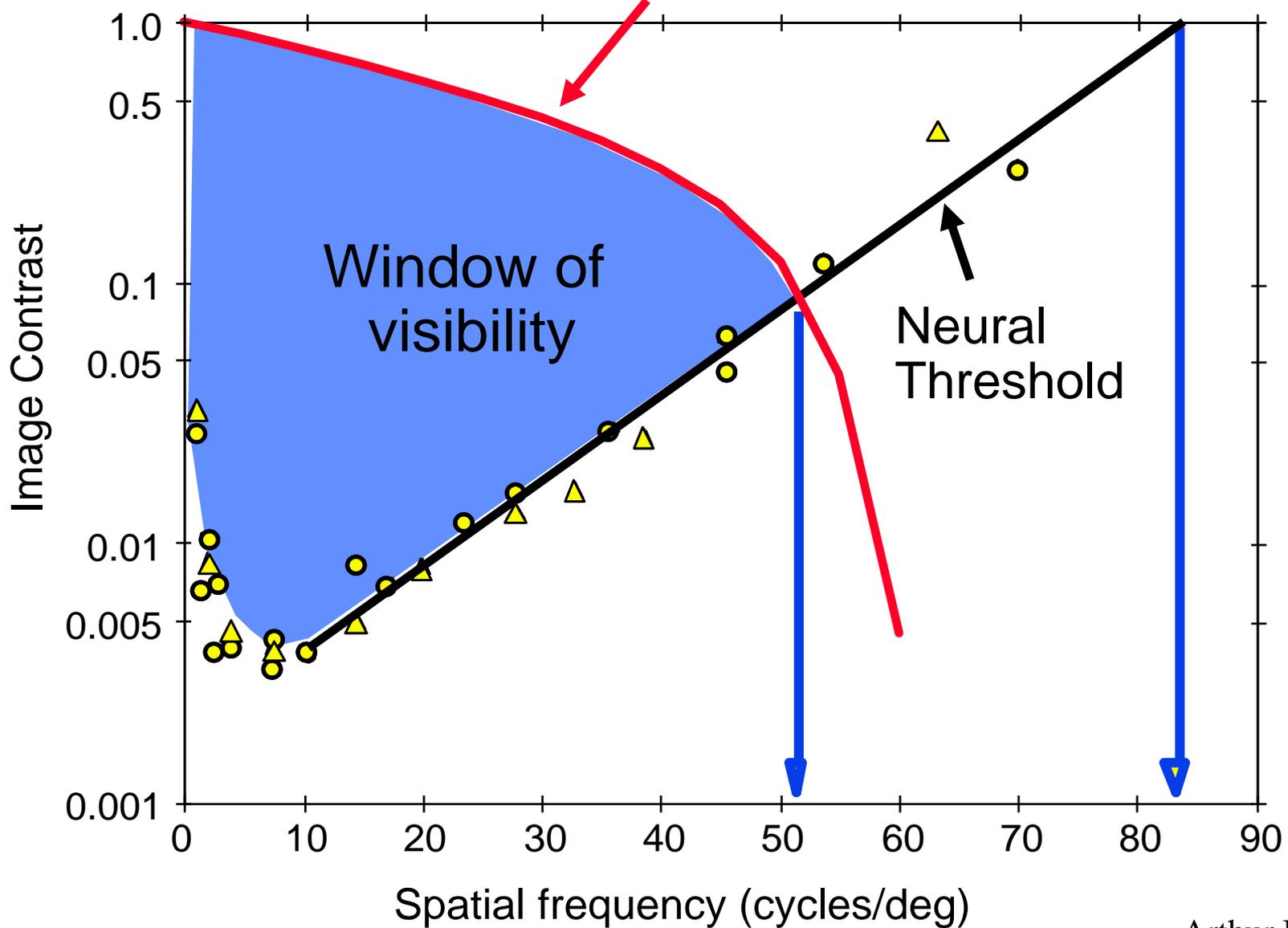


Undersampled

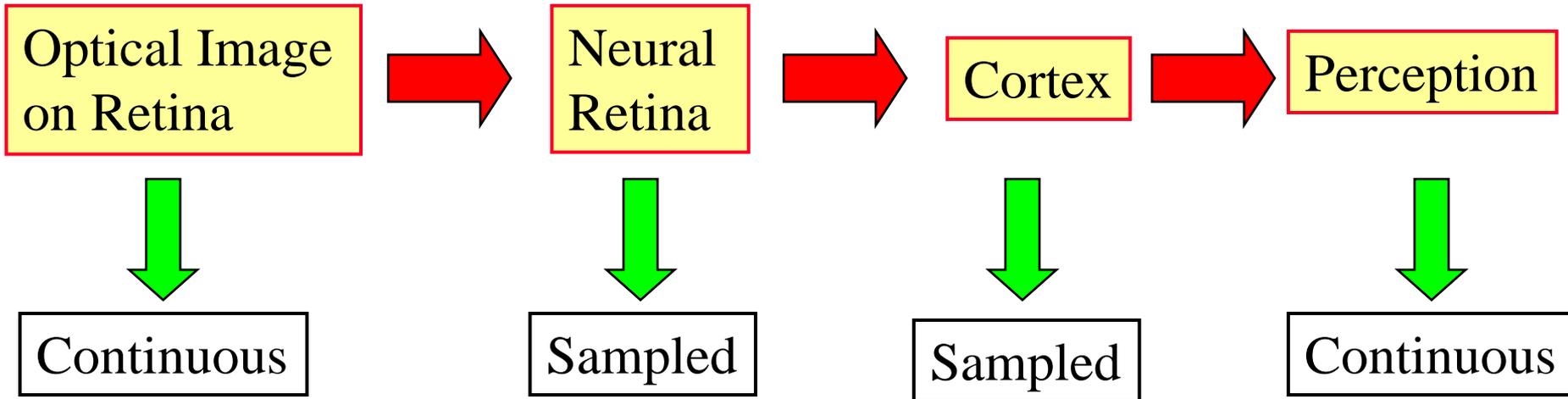


Foveal VA and CS are both limited by optical and neural factors

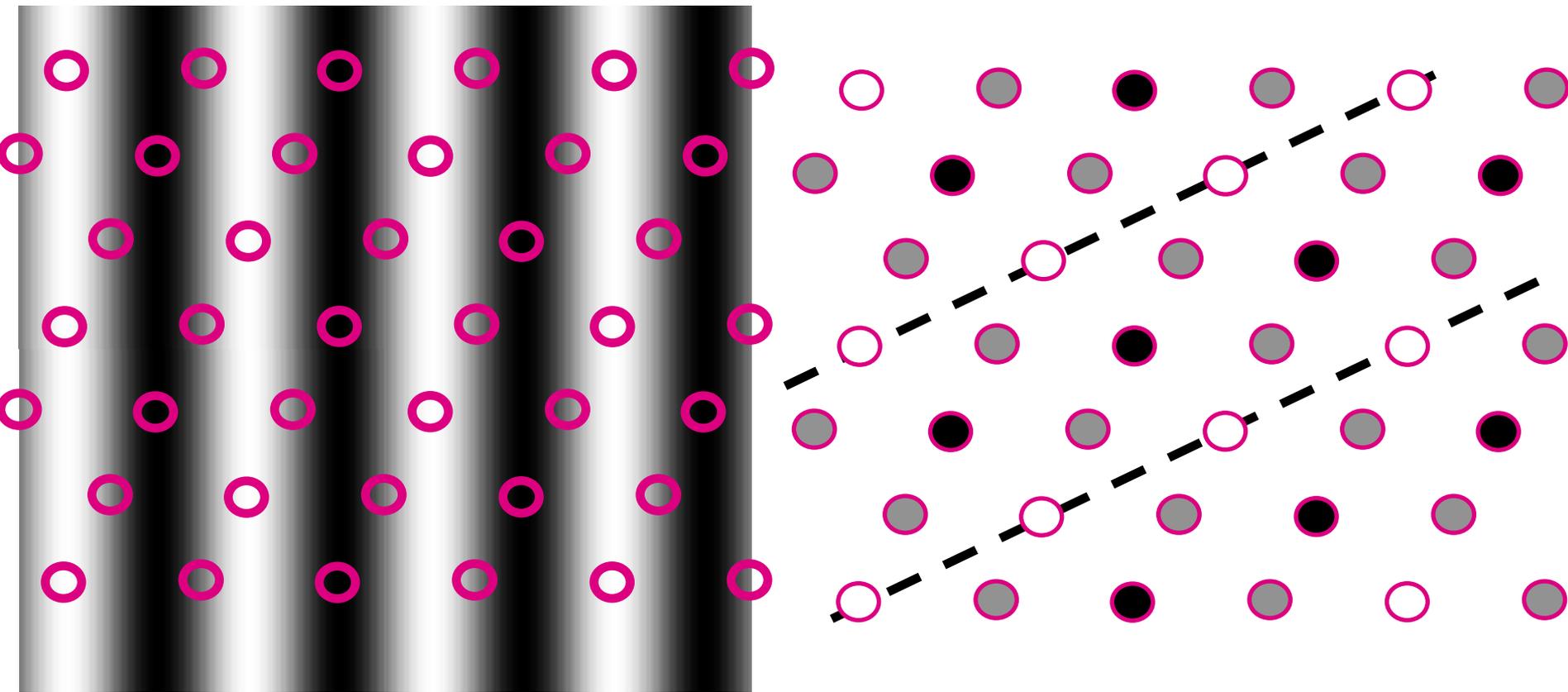
Optical Transfer Function



Neural sampling



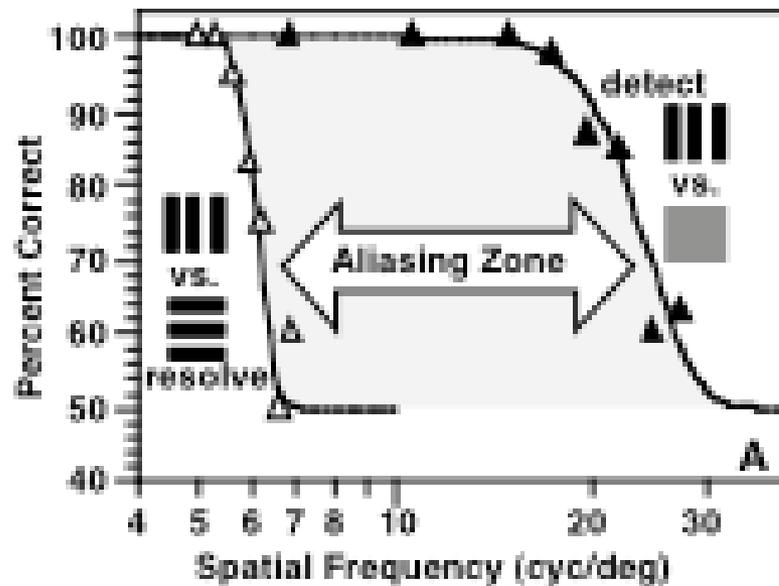
2-dimensional undersampling misrepresents spatial frequency and orientation of patterns



Example with less than 2 samples per period

Psychophysical acuity data and perceived aliases from normal peripheral retina.

2AFC psychometric functions



Subjective appearance of vertical gratings

